Package paracol:

Yet Another Multi-Column Package to Typeset Columns in Parallel

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PART I

User's Manual

Abstract

This package provides a LATEX environment named **paracol** in which you may *switch* and *synchronize* columns by a command \switchcolumn and by internal environments column, nthcolumn, leftcolumn and rightcolumn.

1 Introduction

This document describes the usage of yet another multi-column package named **paracol**. The unique feature of the package is that columns are typeset *in parallel*.

Suppose you are writing a bilingual document whose left column is written in a language, say English, and right column has the translation of the left column in another language, e.g., Japanese. With the **paracol** package you may write an English part of arbitrarily length and then *switch* to its Japanese counterpart to place both parts side by side. Of course you may return to the English writing similarly.

The *column-switching* is always allowed when you complete an outermost level paragraph. You may be unaware whether a column is broken into multiple pages before switching because the package automatically goes back and forward to the correct page and vertical position when you switch the column. Moreover, you may *synchronize* columns so that the tops of the first paragraphs after switching in all columns are vertically aligned. At a synchronization point, you may give a single-column text, for example a common section header, optionally. You may also switch single-column and multi-column in a page arbitrary.

This manual itself is an example of two-column

\begin{paracol}{2}[\section{Introduction}]
\hbadness5000

This document describes the usage of yet another multi-column package named \textsf{paracol}. The unique feature of the package is that columns are typeset {\em in parallel.}

Suppose you are writing a bilingual document whose left column is written in a language, say English, and right column has the translation of the left column in another language, e.g. Japanese. With the \textsf{paracol} package you may write an English part of arbitrary length and then {\em switch} to its Japanese counterpart to place both parts side by side. Of course you may return to the English writing similarly.

The column switching is always allowed when you complete an outermost level paragraph. You may be unaware whether a column is broken into multiple pages before switching because the package automatically goes back and forward to the correct page and vertical position when you switch the documents typeset by paracol. Since the author is not familiar with languages other than English and Japanese and the latter should be hardly understood by most of readers, the right column is the translation of the left English column into a computational language. That is, the right column is the LATEX source code of the left column¹.

2 Basic Usage

Loading the package is very simple. What you have to do is \usepackage{paracol} in the preamble. Or write \usepackage{paracol}[=2018-12-31] to get the last version authored by Hiroshi Nakashima, if this is your wish.

The fundamental means of parallel-column typesetting are the environment paracol and the command \switchcolumn. The paracol environment needs an argument to specify the number of columns. Thus the following is the basic construct for twoparallel-column documents.

\begin{paracol}{2}
left column text
\switchcolumn
right column text

column. Moreover, you may {\em synchronize} columns so that the tops of the first paragraphs after switching in all columns are vertically aligned. At a synchronization point, you may give a single-column text, for example a common section header, optionally. You may also switch single-column and multi-column in a page arbitrary.

This manual itself is an example of two-column documents typeset by \textsf{paracol}. Since the author is not familiar with languages other than English and Japanese and the latter should be hardly understood by most of readers, the right column is the translation of the left English column into a computational language. That is, the right column is the \LaTeX{} source code of the left column% \footnote{Not really but its essence is shown.}.

\switchcolumn

\begin{verbatim}
Here is the source of above.
\end{verbatim}¹

\switchcolumn*[\section{Basic Usage}]
Loading the package is very simple. What
you have to do is |\usepackage{paracol}|
in the preamble. ...²
\switchcolumn
source
\switchcolumn*
The fundamental means of parallel-column
typesetting are the environment |paracol|
and the command |\switchcolumn|. ...
\switchcolumn
source

¹Not really but its essence is shown.

 $^{{}^{}I}\operatorname{This}$ verbatim construct is simply referred as to "source" hereafter.

 $^{^2\}mathrm{Hereafter},$ a part of the source code may be omitted like this.

The \switchcolumn command may have an optional argument to specify the column number (zero origin) to start. That is, \switchcolumn[0] means to switch to the leftmost column, \switchcolumn[1] is to start the second column and so on. Thus the \switchcolumn without the optional argument may be considered as \switchcolumn[$i+1 \mod n$] where i is the ordinal of the column you are leaving from and n is the number of columns given to paracol environment.

3 Column Synchronization

The \switchcolumn command may also be followed by a '*' to synchronize columns. After you switch from a column to another by \switchcolumn* (or \switchcolumn[i]*), all the columns are vertically aligned at the bottom of the *deepest* one preceding the command. For example, the previous section has three \switchcolumn* commands at which left and right columns are vertically aligned.

The *starred* version of \switchcolumn may have an optional argument to specify a single-column *spanning text* whose bottom is the vertical alignment point of columns. For example, \section commands in this manual are given as optional arguments of \switchcolumn* like;

\switchcolumn*[\section{Basic Usage}]
The paracol environment may also start with a
spanning text by specifying it as the optional argument of \begin{paracol}. For example, at the
beginning of this document, the author put;

\begin{paracol}{2}[\section{Introduction}]

4 Environments for Columns

4.1 Environment column

The \switchcolumn is simple but you may prefer to pack the contents of a column in an environment. The column environment is available for this

```
\switchcolumn[1]*
source
\switchcolumn[0]
The |\switchcolumn| command may have an
optional argument to specify the column
number (zero origin) to start. ...
```

```
\switchcolumn[0]*[%
 \section{Column Synchronization}
 \label{sec:sync}]
The |\switchcolumn| command may also be
followed by a '|*|' to {\em synchronize}
columns. ...
```

The {\em starred} version of |\switchcolumn| may have an optional argument to specify a multi-column text whose bottom is the vertical alignment points of the columns. ... \switchcolumn source

4.1 Environment column

```
\begin{column*}[%
  \section{Environments for Columns}
  \label{sec:env}]
```

well-structuralization of $L^{A}T_{E}X$ sources for parallelcolumned documents. A construct;

\begin{column}
text for a column
\end{column}

is (almost) equivalent to;

\switchcolumn text for a column

The column* environment is also available for the column synchronization and may have an optional argument for spanning text.

4.2 Environment nthcolumn

The \switchcolumn can start an arbitrarily specified column with the column number given through its optional argument, but the column environment cannot do it. If you want to start *i*-th column, you have to do \begin{nthcolumn}{i} (or nthcolumn* with an optional argument to synchronize).

4.3 Environments leftcolumn and rightcolumn

The environments leftcolumn and rightcolumn (and their starred versions with an optional argument) are available as more convenient means than saying \begin{nthcolumn}{0} to switch to the left(most) column and \begin{nthcolumn}{1} to the right (but may not be rightmost) one.

\subsection{Environment \texttt{column}}
The |\switchcolumn| is simple but you may
prefer to pack the contents of a column in
an environment. ...
\end{column*}
\begin{column}
source
\end{column}

4.2 Environment nthcolumn

\begin{nthcolumn*}{1}
source
\end{nthcolumn*}

\begin{nthcolumn}{0} \subsection{Environment \texttt{nthcolumn}} The |\switchcolumn| can start an arbitrarily specified column with the column number given through its optional argument, but the |column| environment cannot do it. ... \end{nthcolumn}

4.3 Environment leftcolumn and rightcolumn

```
\begin{leftcolumn*}
\subsection{%
  Environments \texttt{leftcolumn} and
  \texttt{rightcolumn}}
The environments |leftcolumn| and
|rightcolumn| (and their starred versions
with an optional argument) are available as
more convenient means than saying
|\begin{nthcolumn}{0}| to switch to the
left(most) column and ...
\begin{figure*}...\end{figure*}
\begin{figure}[t]...\end{figure}
\end{leftcolumn*}
\begin{rightcolumn}
source and a figure environment
\end{rightcolumn}
```

double-column figure #1

Figure 1: A Double-Column Figure

single-column figure #1

single-column figure #2

Figure 3: Another Single-Column Figure

Figure 2: A Single-Column Figure

5 Floats, Footnotes and Counters

5.1 Figures and Tables

As shown in this page, double-column figures/tables (or those spanned multiple columns if you have three or more) may be placed by figure* and table* environments as usual². A single-column figure/table will be placed in the column in which you put figure and table. For example, the body of a figure environment in a leftcolumn environment is *always* placed in a left column. That is, even if the column of the *current* page does not have enough room to place the figure, it will not be thrown to the right column but will be placed in the left column of the next page³.

Another caution about float placement is that you have to be careful when you try to put a topfloat explicitly with t-option or implicitly without placement option (i.e., tbp in most classes) and to synchronize columns. The rule is as follows; after you synchronize columns in a page, the page cannot have top-floats any more. When you synchronize columns, paracol fixes a virtual horizontal line in the page as the synchronization barrier. Thus no top-floats can-

 $^3 \mathrm{Or}$ some farther page if $\mathrm{IAT}_{\ensuremath{\underline{\mathrm{F}}}\xspace X}$ cannot solve the placement problem wisely.

Table 1: A Single-Column Table

An	example	of
single	column	table

5.1 Figures and Tables

\begin{leftcolumn*}[\section{% Floats, Footnotes and Counters}] \begin{table}[b] \caption{A Single-Column Table} \centerline{\begin{tabular}[t]{|1|c|r|} \hline An&example&of\\\hline single&column&table\\\hline $\end{tabular}$ \end{table} \subsection{Figures and Tables} As shown in this page, double-column figures\slash tables (or those spanned multiple columns if you have three or more columns) may be placed by |figure*| and table* environments as usual³.

5.2 Footnotes and Marginal Notes

Footnotes are also put at the bottom of the column in which |\footnote| commands and their references reside (like this\footnote{...}), as shown in page~2 and this page. Marginal notes behave similarly

³Another example of footnote.

Table 2: Another Single-Column Table

Another	example
of	single
column	table

 $^{^2 \}mathrm{See}$ Section 11 for the appearance order issue of double-column floats.

not be added above the line⁴. Therefore, the author put two figure environments for the figures shown in this page into the leftcolumn* and rightcolumn environment for the previous section.

5.2 Footnotes and Marginal Notes

Footnotes are also put at the bottom of the column in which footnote commands and their references reside (like this⁵), as shown in page 6 and this page. Marginal notes behave similarly like what you are

An example seeing in the left margin of this sentence and the of marginal right marginal note in this page⁶.

5.3 Local and Global Counters

You probably found that the numbering of figures and tables is *global* while that of footnotes are *local*. That is, the figure in the right column of the previous page has number 3 following its left-column counterpart Figure 2. The tables in the page are also numbered as 1 and 2 crossing the column boundary. However, the footnotes in each column have their own numbering sequence. Moreover, the footnote numbers in left columns are typeset in roman font while those in right columns have italic shapes. Similarly, subsection numbering is local and the headings in right columns have typewriter-face numbers.

This happens because the author declared the counters figure and table are *global* in the preamble of this document by saying;

\globalcounter{figure} \globalcounter{table}

and do nothing about footnote and subsection counters. By default, all the counters except for page are local to columns. The value of a local counter of a column is saved somewhere when you leave the column, and it is restored when you revisit the column. The initial values of the local counters are the values they have at \begin{paracol}. After you close the paracol environment, the values of the leftmost



Figure 4: Another Figure with [t] Option

like what you are seeing in the left margin of this sentense\marginpar{\raggedright An example of marginal note.} and the right marginal note in this page\footnote{...}. Another example of Local and Global Counters 5.3 marginal You probably found that the numbering of note. figures and tables is \emph{global} while that of footnotes are \emph{local}. ... \end{leftcolumn*} \begin{rightcolumn} source.

\end{rightcolumn}

a figure with [b] option to fill space

Figure 5: A Figure with [b] Option

⁴Even if you have enough space above, sorry.

 $^{{}^{5}}$ Unless you specify to make footnotes *page-wise* as explained in Section 7.6 and 8.

⁶If you have three or more columns, marginal notes of the second or succeeding columns are placed in the right margin in default setting. The **paracol** package solves the placement problem of marginal notes from two or more columns sharing a side margin by moving some of them down if they conflict over the space with each other.

column are used for the rest of your document until you start new paracol environment. On a restart, local counters in a column have the values they had at the last \end{paracol}, except for those which have been modified outside the environment because the modifications are *broadcasted* to local counters in all columns. You will see the effect of this interenvironment counter value conservation in the footnote numbers in the right column in page 9 and 13.

This broadcasting of a local counter value can be done explicitly in paracol environments by a command \synccounter{*ctr*}. This command makes *ctr* in all columns have the value of that in the column in which the command appears. In addition, another command \syncallcounters performs this broadcasting for all local counters.

If you make a counter global by the command \globalcounter, the save/restore operations are not performed to the counter and thus it is globally incremented by \[ref]stepcounter or commands such as \caption and \section. Note that the value of a global counter depends on the place where it is incremented (or set) in the source code rather than where it appears in the output. Thus if the author put a table environment here to increment table counter, the right-column table at the bottom of page 9 would be Table 3 because its table environment does not appear yet in the source code. Note that, however, though the counter page is global as expected, its numbering is consistent among all columns as far as you refer to the value by \pageref{label} and/or see the values in table of contents, etc.

Another counter which the author made global in this document is section. As explained in Section 3, an optional spanning text of column-switching is considered as in the leftmost column. Since \section commands in this document are always given in spanning texts, so far, it seems unnecessary to make section global because it is incremented correctly in the leftmost column. However, the stepping section has a side effect to reset its descendent counter subsection and referred to from \thesubsection command. Thus if section were local, the rightcolumn subsections in Section 4 would be numbered as "0.1", "0.2" and "0.3" because the local value of section would be zero. Moreover, the right-column subsections of this section would be "0.4", "0.5" and "0.6" because stepping section local to the left column would not reset subsection local to the right column.



Figure 6: A Figure with [p] Option

another figure with [p] option to fill space

Figure 7: Another Figure with [p] Option

yet another figure with [p] option to fill space

Figure 8: Yet Another Figure with [p] Option

fourth figure with [p]
option to fill space

Figure 9: Forth Figure with [p] Option

You may give a local appearance to a counter ctr for the *i*-th column (zero origin) by a command;

$\det efine the counter {ctr}{i}{def}$

where *def* is to be the body of the local definition of \the*ctr*. For example, the preamble of this document has the following to give non-default defitions to \thefootnote and \thesubsection for right columns.

```
\definethecounter{footnote}{1}{%
   \textit{\arabic{footnote}}}
\definethecounter{subsection}{1}{%
   \texttt{%
      \arabic{section}.\arabic{subsection}}}
```

yet another figure with [t] option to fill space

Figure 10: Yet Another Figure with [t] Option

6 Closing paracol Environment and Page Flushing

The final example shown here is this single-column text which the author put after the **paracol** environment above is closed. As you are seeing, a **paracol** environment can be finished at any vertical position in a page and can be followed by ordinary single column texts.

The environment may also be restarted anywhere

you like as shown here. The last issue is to flush a page. The ordinary

\newpage command works as you expect. If you say **\newpage** in the left column in a page, the contents following it will appear in the left column in the next page. Note that this does not affect the layout of the right column.

To flush all columns in a page, a command \flushpage is available. This command in *i*-th column is almost equivalent to;

$\switchcolumn[i]*[\newpage]$

but more robust⁷. The ordinary page breaking command **\clearpage** may also be used to flush all columns and to start a fresh page, but it has a side effect to put all figures and tables which are not yet output. \begin{paracol}{2}
\begin{leftcolumn}
The environment may also be restarted
anywhere you like as shown here. ...
\end{leftcolumn}
\begin{rightcolumn}
source
\end{rightcolumn}
\end{paracol}
Now the aurthor will do ...

Now the author will do \flushpage shortly to start a real binlingual example from the next page, after showing another example of closing paracol environments in this sentence and of restarting in the next one, in which unbalanced column width is demonstrated using \columnratio command shown in Section 7.3.

O.K., we have restarted **paracol** environment and we will see the effect of **\flushpage** now!!

```
\columnratio{0.6}
\begin{paracol}{2}
\begin{leftcolumn}
O.K., ...
\end{leftcolumn}
\begin{rightcolumn} source
\end{rightcolumn}
```

⁷For example \switchcolumn* may flush a page for the synchronization and thus \newpage may leave an empty page.

An Die Freude/To Joy Friedrich Schiller

The following is the libretto of the fourth movement of Beethoven's Ninth Symphony, his adaptation of Schiller's ode "An Die Freude" (or "To Joy" in English). Beethoven's additions and revisions are indicated in italics.

O Freunde, nicht diese Töne! Sondern laßt uns angenehmere anstimmen und freudenvollere ⁸.

Freude!

Freude, schöner Götterfunken Tochter aus Elysium, Wir betreten feuertrunken, Himmlische, dein Heiligtum! Deine Zauber binden wieder, *Was die Mode streng geteilt; Alle Menschen werden Brüder*⁹, Wo dein sanfter Flügel weilt

Wem der große Wurf gelungen, eines Freundes Freund zu sein;Wer ein holdes Weib errungen, mische seinen Jubel ein!Ja, wer auch nur eine Seele sein nennt auf dem Erdenrund!Und wer's nie gekonnt, der stehle weinend sich aus diesem Bund!

Freude trinken alle Wesen an den Brüsten der Natur;Alle Guten, alle Bösen folgen ihrer Rosenspur.Küsse gab sie uns und Reben, einen Freund, geprüft im Tod;Wollust ward dem Wurm gegeben, und der Cherub steht vor Gott.

Froh, wie seine Sonnen fliegen durch des Himmels prächt'gen Plan,

Laufet, Brüder, eure Bahn, freudig, wie ein Held zum Siegen.

Oh friends, no more of these sad tones! Let us rather raise our voices together In more pleasant and joyful tones⁴.

Joy!

Joy, thou shining spark of God, Daughter of Elysium, With fiery rapture, goddess, We approach thy shrine. Your magic reunites That which stern custom has parted; All humans will become brothers⁵ Under your protective wing.

Let the man who has had the fortune To be a helper to his friend, And the man who has won a noble woman, Join in our chorus of jubilation! Yes, even if he holds but one soul As his own in all the world! But let the man who knows nothing of this Steal away alone and in sorrow.

All the world's creatures drink From the breasts of nature; Both the good and the evil Follow her trail of roses. She gave us kisses and wine And a friend loyal unto death; She gave the joy of life to the lowliest, And to the angels who dwell with God.

Joyous, as his suns speed Through the glorious order of Heaven, Hasten, brothers, on your way, Joyful as a hero to victory.

⁸If I had been a good student in my German class, I could find the German translation of the right column footnote 4 is "Dieser Teil wurde von Beethoven hinzugefügt" by myself without the kind help from a user. ⁹Original: Was der Mode Schwert geteilt;

Bettler werden Fürstenbrüder,

⁴This part was added by Beethoven.

⁵Original: What custom's sword has parted; Beggars become princes' brothers

Seid umschlungen, Millionen! Diesen Kuß der ganzen Welt! Brüder, über'm Sternenzelt muß ein lieber Vater wohnen.

Ihr stürzt nieder, Millionen? Ahnest du den Schöpfer, Welt? Such'ihn überm Sternenzelt! Über Sternen muß er wohnen.

Be embraced, all ye millions! With a kiss for all the world! Brothers, beyond the stars Surely dwells a loving Father.

Do you kneel before him, oh millions? Do you sense the Creator's presence? Seek him beyond the stars! He must dwell beyond the stars.

7 Reference Manual

7.1 Environment paracol

\begin{paracol}{num}[text] body \end{paracol}

The environment **paracol** contains *body* typeset in *num* columns in parallel. The optional *text* is put spanning all columns prior to the multi-columned *body*.

- The environment may start from any vertical position in a page, i.e., not necessary at the top of a page. The single-column pre-environment stuff of the starting page in which \begin{paracol} lies are naturally connected to the beginning part of body in each column, unless the page has footnotes¹⁰ or bottom floats. If these kinds of bottom stuff exist, they are put above the multi-columned body, or the spanning text if provided, with a vertical skip of \textfloatsep separating them if bottom floats exist, or of \belowfootnoteskip described in Section 7.6 if only footnotes exist. The deferred floats which have not yet appeared in the starting page and thus will appear in the next or succeeding pages are considered as page-wise floats given in the environment.
- The environment can be enclosed in a list-*like environment* such as enumerate, itemize and description. If so, \items in each column are typeset using the parameters of the surrounding environment such as \leftmargin and \rightmargin. For example, the following short paracol environment is included in an itemize for this and other \items in this page.
- This is the first \item in the left column.
- This is the second \item in the left column followed by a \switchcolumn¹¹.
- This is the first \item in the right column.
- This is the second *\item* in the right column.
- This is the third and last \item in the right column.

You are now seeing the switching to/from multi-columned and itemized texts are naturally connected with the last and this single-columned sentences. You may feel the space between two columns above is too large but it simply results from the large total \leftmargins of the outer description and this itemize, which make the right column shifted right. A simple remedy for this large space is to make \columnsep narrower, for example 0 pt as shown below.

- This \item is wider than the last \item above because \columnsep is 0 pt.
 Therefore, this \item is shifted left a little bit to make inter-column space narrower.
- All local counters in all columns are initialized to have the values at \begin{paracol} on its first occurrence. On the second and succeeding occurrences of \begin{paracol}, the local counters in each column have the value at the last \end{paracol}, unless they are modified after the \end {paracol}. If a counter is modified (or declared by \newcounter) after the \end{paracol}, the local versions of the counter in all columns commonly have the value at \begin{paracol}.
- The environment may end at *any* vertical position in a page, i.e., the *post-environment stuff* being the single-column texts and others following **\end{paracol}** in the *last page* of the environment may not start from the top of a page. If any columns don't have deferred column-wise floats and the most advanced *leading column* at **\end{paracol}** has neither of footnotes¹² nor bottom floats, its bottom is naturally connected to the post-environment stuff. If the leading column has these kinds of bottom stuff, they are put above the post-environment stuff, with a vertical skip of **\textfloatsep**

¹⁰With merged footnote layout shown in Section 7.6, the footnotes in the single-column contents are merged with those in **paracol** environment and are put at the bottom of the starting page together as shown in this page.

¹¹This footnote is to show the footnotes in this page are merged.

 $^{^{12}}$ With merged footnote layout shown in Section 7.6, the footnotes in the closing **paracol** environment are merged with those in post-environment stuff and are put at the bottom of the page together as shown in this page.

separating them if bottom floats exist. All deferred column-wise floats given in the environment are flushed before the post-environment stuff appears, possibly creating *float columns* only with floats. On the other hand, deferred page-wise floats given in the environment are considered as deferred (single-) column-wise floats given just after \end{paracol}.

- The values of all local counters in the leftmost column are used as the initial values of them in the post-environment stuff.
- The paracol environment cannot be nested, or you will have an error message of illegal nesting.
- The commands \switchcolumn, \synccounter, \syncallcounters and \flushpage, and environments column(*), nthcolumn(*), leftcolumn(*) and rightcolumn(*) are *local* to paracol environment and thus undefined outside the environment¹³. The command \clearpage is of course usable outside and inside the environment but its function inside is a little bit different from outside.

\begin{paracol}[numleft]{num}[text] body \end{paracol} \begin{paracol}[numleft]*{num}[text] body \end{paracol}

If a **\begin{paracol}** has the optional numleft argument to specify the number of leading columns n_l together with the total n given by num, columns in the environment are laid out across two adjacent pages. In this parallel-page typesetting, the first n_l columns are placed in the left page while remaining $n_r = n - n_l$ columns go to the next right page. The pair of left and right pages is considered as comprising a virtual paired page and thus shares a common page number, unless non-paired typesetting is specified by the optional '*' following the optional numleft argument. In the non-paired parallel-paging, when the leading n_l columns are put in a page p, the trailing n_r columns are in the page p + 1.

- All *page-wise stuff*, i.e., pre-environment and post-environment stuff, page-wise floats, spanning text and (merged or non-merged) page-wise footnotes, are placed only in left parallel-pages leaving corresponding regions in right parallel-pages blank¹⁴.
- A non-paired left parallel-page is not necessary to be even-numbered, though the printing tradition requires so if you naturally want to have a parallel-page pair in a double spread. The page number given to the first left parallel-page is simply the number of the page p_1 in which \begin{paracol} reside, and that for the k-th left parallel-page is $p_1 + 2(k-1)^{15}$. Therefore, to make it sure p_1 is even, you might need to have an ordinary page of blank, a title, etc., or to let page counter have an even number by \setcounter, etc., before starting a paracol environment.
- Section 9 shows examples of parallel-paging together with related issues on two-sided typesetting.

7.2 Column-Switching Command and Environments

\switchcolumn[col] \switchcolumn[col]*[text]

The command switches columns from i to j where i and j is the zero-origin ordinals of the columns from/to which we are leaving/visiting respectively. Without the optional col, $j = i + 1 \mod n$ where n is the number of columns given to \begin{paracol}, while j = col with the optional argument. If the command (or [col] if specified) is followed by a *, the column-switching takes place after synchronization and, if specified, the optional spanning text is put.

• Using \switchcolumn in a list-like environment *included* in a paracol environment causes an ugly result without any error/warning messages. This caution is effectual for all column-switching environments too.

 $^{^{13}\}mathrm{Unless}$ you dare to define them.

¹⁴Someday the author could devise an advanced mechanism to exploit the space in right parallel-pages.

¹⁵Unless you make some change to page counter.

- If $col \notin [0, n)$, an error is reported and, if you dare to continue, you will switch to the leftmost column 0.
- The synchronization point is set just below the last line of the leading column in a page p, partly taking deferred floats into account. That is, all deferred floats are put in the pages up to p-1 and at the top of p if possible. Then, if a non-leading column has footnotes and/or bottom floats and they cannot be pushed down below the synchronization point, the point is moved to the next page top¹⁶.
- In a page having one or more synchronization points, stretch and shrink factors of all vertical spaces, such as those surrounding sectioning commands, are ignored. Therefore, even if you specify \flushbottom, the page is typeset as if \raggedbottom were specified.
- After a synchronization point is set, no top floats will be inserted in the page having the point, thus they will be deferred to the next page or further one.

\begin{column} body \end{column} \begin{column*}[text] body \end{column*}

The environment column contains *body* for the column next to what we are in just before \begin{column}. The starred version column* does the same after synchronization and, if specified, the optional spanning *text* is put.

• The environments are almost equivalent to;

{\switchcolumn body \par}
{\switchcolumn*[text] body \par}

except for their first occurrences which don't switch to the column 1 (i.e., right column if twocolumned) but stay in the leftmost column 0. More precisely, \begin{column(*)} does not make column-switching if it is not preceded by \switchcolumn nor other column-switching environments.

- The *body* of the environments cannot have \switchcolumn nor column-switching environments including column(*) themselves, or you will have an error message of illegal use of command/ environment.
- Column-switching does not take place at \end{column(*)}. Therefore, texts following the environments are put in the column in which *body* resides until a column-switching command/environment is given.

\begin{nthcolumn}{col} body \end{nthcolumn} \begin{nthcolumn*}{col}[text] body \end{nthcolumn*}

The environment nthcolumn contains *body* for the column *col*. The starred version nthcolumn* does the same after synchronization and, if specified, the optional spanning *text* is put.

• The environments are equivalent to;

```
{\switchcolumn[col] body \par}
{\switchcolumn[col]*[text] body \par}
```

- The *body* of the environments cannot have \switchcolumn nor column-switching environments including nthcolumn(*) themselves, or you will have an error message of illegal use of command/ environment.
- Column-switching does not take place at \end{nthcolumn(*)}. Therefore, texts following the environments are put in the column in which *body* resides until a column-switching command/environment is given.

 $^{^{16}\}mathrm{Or}$ below top floats deferred to the page.

```
\begin{leftcolumn} body \end{leftcolumn}
\begin{leftcolumn*][text] body \end{leftcolumn*}
\begin{rightcolumn} body \end{rightcolumn}
\begin{rightcolumn*][text] body \end{rightcolumn*}
```

The environment leftcolumn contains *body* for the leftmost column 0, while rightcolumn for the column 1 being the right column in two-column typesetting. The starred versions leftcolumn* and rightcolumn* do the same after synchronization and, if specified, the optional spanning *text* is put.

• The environments leftcolumn(*) are equivalent to;

```
\begin{nthcolumn}{0} body \end{nthcolumn}
\begin{nthcolumn*}{0}[text] body \end{nthcolumn*}
while rightcolumn(*) are equivalent to;
  \begin{nthcolumn}{1} body \end{nthcolumn}
```

\begin{nthcolumn*]{1} boay \end{nthcolumn*}

\thecolumn

The command gives you the zero-origin ordinal of the column in which this command appears. Therefore, the following code snip;

```
\begin{paracol}{3}
Column-\thecolumn.\switchcolumn Column-\thecolumn.\switchcolumn Column-\thecolumn.
\end{paracol}
```

gives us the followings.

Column-0.

Column-1.

Column-2.

• The command is *neither* a IAT_EX's counter nor \count register of native T_EX, and thus the value it keeps cannot be modified. However, it can be used wherever an integer number is required or appropriate. Therefore for example, \setcounter{mycounter}{\thecolumn} works well to give the column ordinal to the counter mycounter.

\definecolumnpreamble{col}{pream}

The command is to define the column preamble *pream* for the column *col*, which is inserted at every column-switching to the column. More specifically, the command let \switchcolumn to *col* act as if you specify;

 $\operatorname{switchcolumn} \langle pream \ for \ col \rangle$

and column-switching environments such as nthcolumn act as if you specify;

 $\boldsymbol{col} \langle pream \ for \ col \rangle$

- The optional spanning text of \switchcolumn, column-switching environments and \begin{paracol} is considered to be in a virtual column -1, and thus if you need a preamble for spanning texts do \definecolumnpreamble{-1}{pream}.
- The command may appear in a paracol environment and, if so, *pream* is effective from the succeeding column-switching to *col*.
- The definition of *pream* is made globally.

\ensurevspace{len}

The command tells the first synchronizing column-switching command (i.e., \switchcolumn[col]*) or environment (i.e., column*, etc.) following this command that the page must be broken before synchronization unless the synchronization point has the space of *len* or more below it in the page. If a synchronization does not have the command after the previous synchronization, it is assumed that \ensurevspace{\baselineskip} is given.

- This command is to be used when a synchronization point would be placed near the bottom of a page p and the space below it is not sufficient for a column c to put anything in the page, while another column c' can have a few lines in the page. If this happens, the first line after the synchronization should start at the top of the page p+1 in the column c, while that of c' is still in the page p, giving you an impression that the synchronization fails to align the top of all columns below it. The fact is, however, the synchronization point is properly established near at the bottom of the page but the first line of c needs some large space due to, for example, the followings.
 - The line has unusually tall stuff including larger font letters.
 - The line has a footnote reference which is hardly apart from the footnote, and thus the line and the footnote go to the next page together.
 - The parameter \clubpenalty is too large (e.g., 10000) to break the first and second lines into separate pages.
 - The first line follows a vertical space.
- This manual itself has some instances of \ensurevspace command in the page 13 and 14 in which each German stanza is enclosed in verse and then leftcolumn* environments and has \ensurevspace{2\baselineskip} before the \begining of the outer leftcolumn* because the first line of the stanza is preceded by a vertical space inserted by \begin{verse}. In fact without \ensurevspace, the first two lines of the sixth English stanza would be in the page 13, while corresponding German stanza go to the next page 14 as a whole, due to the difference of the height of footnotes in each column, i.e., German ones are taller than English ones to narrow the space for the German column.
- As the author does in the "An die Freude/To Joy" example, it is a good tactics to have an \ensurevspace with some vertical space larger than the default \baselineskip if it is sure that a column has a feature shown above regardless of the position of the synchronization point in question, because the point goes up or down with revisions of your document and using an \ensurevspace for a synchronization far above the page bottom is perfectly harmless. Similarly, if you find a problem in a synchronization and add an \ensurevspace to solve it, keeping the command attached is recommended even when the synchronization point moves up or down to make the command unnecessary.

7.3 Commands for Column and Gap Width

 $columnatio{r_0, r_1, \cdots, r_k}[r'_0, r'_1, \cdots, r'_{k'}]$

The command defines the width of each column by the fraction r_i to specify the portion which *i*-th (i = 0 for the leftmost) column occupies. More specifically, the width w_i of the *i*-th column is defined as follows, where W is \textwidth, S is \columnsep, and n is the number of columns given to \begin{paracol}

$$\begin{split} W' &= W - (n-1)S \\ w_i &= \begin{cases} r_i W' & i \leq k \\ \frac{(1 - \sum_{j=0}^k r_j)W'}{n - (k+1)} & i > k \end{cases} \end{split}$$

For a paracol environment with parallel-paging, n is replaced with n_l for the columns in left parallel-pages, while n and w_i are replaced with n_r and w_{n_r+i} for those in right parallel-pages. Moreover, if the optional argument having $r'_0, r'_1, \dots, r'_{k'}$ is provided, w_{n_r+i} for a column in right parallel-pages is determined by r'_i and k' instead of r_i and k.

- The equations above imply that k < n 1, $r_i > 0$ and $\sum_{j=0}^k r_j < 1$. If $k \ge n 1$, k is assumed to be n 2 and all r_i such that $i \ge n 1$ are ignored. If r_i or its sum does not satisfy the conditions, you will have an ugly result with "Overfull" messages.
- The argument r_0, r_1, \dots, r_k can be empty to mean k = -1 to let all column widths be W'/n as default.
- The setting of column width by the command takes effect in the paracol environments following the command¹⁷. Therefore, though placing the command in the preamble is the most natural way¹⁸, you may place this command between two paracol environments to change the column layout for the second one even when they appear in a page as shown in Section 6.
- In the *i*-th column, \columnwidth has w_i and, for outermost paragraphs in the column, \hsize has w_i as well. As for \linewidth , it has $w_i (\textwidth l)$ where *l* is what \linewidth had at $\begin{paracol}, i.e., the \\linewidth for the list-like environment surrounding paracol if any, or <math>\textwidth$ otherwise.
- You can specify width of each column and that of each *gap* between two columns more detailedly by \setcolumnwidth shown below. If your document has both of \columnratio and \setcolumnwidth prior to a paracol environment, the command given later is effective for the environment.

$stcolumnwidth{s_0, s_1, \cdots, s_k}[s'_0, s'_1, \cdots, s'_{k'}]$

The command defines the width of each column and that of each gap between two columns by the column/gap specification s_i for the *i*-th column and the gap between it and the (i+1)-th column. More specifically, s_i has the form of \hat{w}_i or \hat{w}_i / \hat{g}_i where each of \hat{w}_i and \hat{g}_i is a proper glue including a proper dimension, or an empty string to mean $\hat{w}_i = \forall i l l$ and $\hat{g}_i = \forall columnsep$, to determine the width of *i*-th column w_i and that of *i*-th gap g_i as follows, where nat(x) is the natural width of the glue x, str(x) is the infinite stretch factor of x, W is $\forall textwidth$, and n is the number of columns given to $begin{paracol} p g_i = 1 \\ p g_i = 1$

$$W' = \sum_{i=0}^{n-2} \left(nat(\hat{w}_i) + nat(\hat{g}_i) \right) + nat(\hat{w}_{n-1})$$

$$F = \sum_{i=0}^{n-2} \left(str(\hat{g}_i) + str(\hat{g}_i) \right) + str(\hat{w}_{n-1})$$

$$x_i = \begin{cases} (W/W')nat(\hat{x}_i) & W' \ge W \lor F \le 0\\ nat(\hat{x}_i) + (str(\hat{x}_i)/F)(W - W') & W' < W \land F > 0 \end{cases} \quad (x \in \{w, g\})$$

That is, if the total of natural widths W' is larger than **\textwidth** W or there are no infinite stretch factors in the specification, given widths are scaled down or up so that the scaled total is equal to W. Otherwise, each width with an infinite stretch factor is extended according to its ratio in the total stretch so that the stretched total is equal to W.

For a **paracol** environment with parallel-paging, n is replaced with n_l for the columns in left parallel-pages, while n, w_i and g_i are replaced with n_r , w_{n_r+i} and g_{n_r+i} for those in right parallel-pages. Moreover, if the optional argument having $s'_0, s'_1, \dots, s'_{k'}$ is provided, w_{n_r+i} and g_{n_r+i} for a column in right parallel-pages are determined by s'_i instead of s_i .

 $^{^{17}}$ If the command is in a **paracol** environment, the command does not affect the column widths of the environment but does the next ones, though such usage is very unusual.

¹⁸Or second most to not using it at all, of course.

- In paracol environments having n columns, s_i s.t. $i \ge n$ and \hat{g}_{n-1} are ignored. On the other hand if k < n-1, it is assumed s_i is an empty string for all i > k.
- Finite stretch factors and finite or infinite shrink factors in \hat{w}_i and \hat{g}_i are ignored.
- Unlike T_EX's genuine glue addition, all infinite unit fil, fill and filll are not distinguished in the summation for F. Also unlike T_EX's genuine scaling of a glue primitive, $f \neq 1$ means 0 pt plus $f \neq 1$.
- The division W/W' and $str(\hat{x}_i)/F$ can have some arithmetic errors and thus the total of w_i and g_i may not be equal to W exactly but can be a little bit less than W. This small error is, however, equally distributed to g_i in typesetting of a page to make the total width of columns and gaps is exactly W^{20} .
- All the specifications shown in the table below give us same results for a paracol environment having three columns, providing \textwidth = 360 pt and \columnsep = S = 20 pt.

s_0, s_1, s_2	w_0	g_0	w_1	g_1	$w_2 \ (\text{in pt})$
50pt/20pt,100pt/40pt,150pt	50	20	100	40	150
50pt,100pt/2\columnsep,150pt	50	S	100	2S	150
50pt/\fill,100pt/2\fill,150pt	50	$(1/3) \cdot 60$) 100	$(2/3) \cdot 60$) 150
,2\fill/2\columnsep,3\fill	$(1/6) \cdot 300$	S	$(2/6) \cdot 300$	2S	$(3/6) \cdot 300$
50pt/20,50pt plus 1fil/40pt,50pt plus 2fil	50	20	$50 + (1/3) \cdot 150$	40	$50 + (2/3) \cdot 150$
5pt/2pt,10pt/4pt,15pt	$10 \cdot 5$	$10 \cdot 2$	$10 \cdot 10$	$10 \cdot 4$	$10 \cdot 15$
100pt/40pt,200pt/80pt,300pt	$0.5 \cdot 100$	$0.5 \cdot 40$	$0.5 \cdot 200$	$0.5 \cdot 80$	$0.5 \cdot 300$

• If your document has both of \columnratio and \setcolumnwidth prior to a paracol environment, the command given later is effective for the environment.

7.4 Commands for Two-Sided Typesetting and Marginal Note Placement

$\mathsf{twosided}[t_1t_2\cdots t_k]$

The command enables a set of two-sided typesetting features $\{t_i | t_i \in \{p, c, m, b\}, 1 \le i \le k\}$ explicitly by the optional argument, or all of the following four features as a whole without the argument, in even-numbered pages.

- p(age) for ordinary two-sided paging, letting the left side margin be \evensidemargin, page headers be different from those in odd-numbered pages with headings or myheadings page style, and \cleardoublepage leave an even-numbered page blank if it is used in an odd-numbered page.
- c(*olumn*) for *column-swapping* to *print* columns in even-numbered pages in reverse order. This feature is sometimes preferable in typesetting especially with unbalanced parallel columns to make, for example, a wider columns are always *inside* while narrower ones are *outside*.
- m(arginal text) to place marginal notes in the side margin opposite to that specified by the command \marginparthreshold discussed shortly.
- b(*ackground painting*) to make background painting, shown in Section 7.8, *mirrored* so that, for example, a color specified for the left margin is used to paint the right margin instead.
 - The feature p is also enabled by the twoside option of \documentclass with almost all classes including article, book, report, etc. Though it is strongly recommended to make both settings by \documentclass and this command consistent, they can be inconsistent resulting in lack of

¹⁹In T_EX's grammar, f (fill means a dimension rather than a glue and is 0 pt because the natural component of (fill is 0. ²⁰If we may ignore the arithmetic error inherent in T_EX.

some expected functions. For example, enabling p feature by \twosided without twoside option in \documentclass makes the format of headers and footers in all pages same even with \pagestyle{headings}.

- The column-swapping enabled by the feature c is ineffective in non-paired parallel-paging because it is meaningless²¹, and thus silently ignored.
- In ordinary single-column typesetting, marginal note swapping in even-numbered pages is enabled by the twoside option, while it never takes place in ordinary two-column typesetting. For marginal notes given in paracol environments, however, swapping of them in even-numbered pages is enabled by giving the feature m to \twosided.
- The command has to be outside of paracol environments to decide the action in the environments following them. If it appears in a paracol environment, you will have a warning message saying it is ignored.
- This narrower, outside and italicized column-1 is at first in right side but the page break has changed the position to the left.
- Here is an example of column swapping. Since this page 22 is odd, this wider column-0 with roman font is placed in left side and thus inside at the begining, but now we are in an even page in which this column is in right side.
- In old versions of paracol, namely 1.2 and its minor revisions 1.2x, column-swapping was controlled by lengthy commmands \swapcolumninevenpages and \noswapcolumninevenpages. Though they are still available and will be so forever for backward compatibility, it is recommended to use \twosided with or without the feature c. The old versions also have a problem that spanning stuff crossing a page boundary is placed incorrectly after the page break in it, but this problem is solved by a fix incorporated in version 1.3.
- It must be $t_i \in \{p, c, m, b\}$, or you will have an error message of illegal two-siding feature.
- Section 9 shows examples of two-sided typesetting together with related issues on parallel-paging.

$\mbox{marginparthreshold}{k}[k']$

The command specifies the minimum ordinal k of columns whose marginal notes are placed in right margin. That is, marginal notes given in a column-i go to left margin if i < k, while they go to right if $i \ge k$. The optional argument k', if given, is for columns in right parallel-pages to decide the margin where their marginal notes are placed. In default, k = 1 is assumed to let marginal notes from the leftmost column-0 go to left margin while those from other columns go to right.

- You may specify k = 0 to let all marginal notes go to right margin, or may give the command a large number, say 100, to place all of them in left margin.
- The setting k = 0 or k = 100 above makes a side margin *shared* by marginal notes from different columns, and sharing is inevitable when a (parallel-) page has three or more columns. When a margin is shared by marginal notes from two or more columns, it can happen that two marginal notes from different columns conflict over the space to be occupied by each of them. This conflict is solved by **paracol** to push down the note given later in your source .tex until an available space for it is found. Note that the marginal note to be pushed down is determined by the position in the source rather than that in the printed result. Also note that **paracol** exploits space between two marginal notes having been already placed in the placement of other note coming later to place it at the natural position if possible or to minimize the amount of pushing down otherwise.
- In the decision of the real margin in which a marginal note is placed, other two factors are involved; m feature of \twosided command and the parity of the page; and LATEX's genuine command \reversemarginpar. More specifically, after the first preliminary decision is made according to

²¹Unless somebody tells the author it is meaningful.

the threshold given to \marginparthreshold, we have the following two steps to modify the decision; if m feature has been specified in \twosided command and the marginal note belongs to an even-numbered page, the decision is reversed to have the second preliminary result; and then if \reversemarginpar has been specified, the second result is reversed (again) to have the final result.

- In old versions of paracol, namely older than 1.3, marginal note placement was not only uncontrollable but also gave ugly results when your document has three or more columns because the marginal notes from a column not being leftmost or rightmost were placed in the gap following the column rather than a margin. This miserable *gap note* placement does not happen any more, or in other words this is no more available because the author believes nobody loves it.
- Section 9 shows examples of marginal note placement together with related issues on parallel-paging and two-sided typesetting.

\marginnote[left]{right}[voffset]

You may use the package marginnote and its command \marginnote in paracol environments as a replacement of \marginpar. However, the command is *emulated* with \marginpar and paracol's own mechanism of marginal note placement. Therefore, some of marginnote's functionality are not effective in paracol environment except for the following features.

- Shifting up/down a marginal note by the optional *voffset*.
- Defining fonts (and others) for marginal notes by \marginfont.
- Controlling the holizontal paragraph alignment by \raggedleftmarginnote and \raggedright marginnote.

Note that you will see a warning message "\margninnote is emulated by \marginpar" at the first inparacol occurrence of the command to let you know the imperfection.

7.5 Commands for Counters

\globalcounter{*ctr*}

$\globalcounter*$

The command $\common delta counter{ctr}$ declares that the counter ctr is global to all columns, while $\common delta counter*$ does so for all counters. An update of a global counter in a column is seen by any other columns.

- All column-local values of a descendant local counter of a global counter are zero-cleared when the global counter is explicitly stepped by *`stepcounter* or *`refstepcounter*, or implicitly by a sectioning command and so on.
- The counter page is always global but an explicit update of it by e.g., \setcounter in a non-leftmost column is not seen by other columns and is canceled even for the column itself after a column-switching or a page break in the column. Therefore, if you want to make a *jump* of page, it must be done in the leftmost column 0. Note that a jump from a page p to q can be seen in other columns even if they have gone beyond p before the column 0 makes the jump, as far as page having q (or its successor) is referred to by \pageref or through contents files such as .toc²².
- All counters except for page are local by default. This feature may cause a problem with some packages including marginnote and (auto-)pst-pdf having their own counters which must be global. Since it is tough to find the name of such counters from package sources, if you have something wrong with these (or other) packages, try to put \globalcounter* in your preamble and use \localcounter shown below to localize specific counters which you need to be local.

²²Direct reference to page may give an inconsistent result, as you might have in ordinary LATEX documents.

• Globalizing a *ctr* being already global is just ignored without any complaints.

\clicalcounter{ctr}

The command declares that the counter ctr is local for each column.

• Though this command is intended for localizing a *ctr* which is once globalized, localizing a local counter does not causes any error but is just ignored. Localizing the permanently global **page** is also just ignored without any complaints.

\definethecounter{ctr}{col}{rep}

The command defines $\the ctr$ being $\{rep\}$ for the local use in the column *col*. That is, $\the ctr$ in the column *col* acts as if it is defined by $\renewcommand{\the ctr}{rep}$.

\synccounter{*ctr*}

The command broadcasts the value of the local counter ctr in the column in which the command appears to the values in all other columns.

\syncallcounters

The command broadcasts the values of all local counters in the column in which the command appears to the values in all other columns.

7.6 Page-Wise Footnotes

$footnoteplacement{layout}$

 $footnotelayout{layout}^{23}$

The command specifies the $layout \in \{c, p, m\}$ of footnotes in paracol environments as follows.

- c(olumn) makes footnotes *column-wise* (aka multi-columned) being default to place footnotes in each column at the bottom of the column and separating them from pre-environment and post-environment footnotes.
- p(age) makes footnotes *page-wise* (aka single-columned) so that footnotes in all columns are gathered, typeset spanning all columns, and placed at the bottom of the page in which they appear or at the end of the **paracol** environment they belong to, so that they are separated from pre-environment and post-environment footnotes.
- m(erge) makes page-wise footnotes *merged* with footnotes in outside of the environment but in the same page, i.e., those in pre-environment and post-environment stuff.
 - An example of merged footnote is found in p. 15 while you will see many of them in Section 8^{24} .
 - In any layouts, a footnote cannot have page breaks in it, i.e., a footnote is always put in a page as a whole. This makes it impossible to have a footnote taller than \textheight and thus you will see a warning message if you give a very long footnote which will be printed intruding into the area for page footer (or out of the paper bound).
 - Choosing the layout page-wise or merged makes footnote counter global and \fncounteradjustment shown below performed inside \footnoteplacement. Choosing column-wise let the command do the operations oppositely, i.e., localizes footnote and does \nofncounteradjustment. Though these settings are usually appropriate for each footnote layout but you can override them by explicitly using commands like \localcounter{footnote}.

 $^{^{24}}$ The left-column footnote 6 in p. 12 looks like a merged footnote because it is at the bottom of the page and the marked text is above the single-column text. However, it is an ordinary column-wise one produced by a trick with \footnotemark and \footnotetext in different paracol environments.

- The command has to be outside of paracol environments to decide the action in the environments following them. If it appears in a paracol environment, you will have a warning message saying it is ignored.
- In old versions of paracol, namely 1.2 and its minor revisions 1.2x, footnote layout was controlled by a set of commands \multicolumnfootnotes for c, \singlecolumnfootnotes for p, and \mergedfootnotes for m. Though they are still available and will be so forever for backward compatibility, it is recommended to use \footnoteplacement²⁵.
- It must be $layout \in \{c, p, m\}$, or you will have an error message of illegal layout specifier.

\footnote*[num]{text} \footnotemark*[num] \footnotetext*[num]{text}

The starred version of \footnote, \footnotemark and \footnotetext are for the adjustment of the footnote numbering, the order of footnote marks in main texts, and the stacking order of footnotes at page bottom. Their usages with various examples are given in Section 8.

\fncounteradjustment

\nofncounteradjustment

The maintenance of footnote with the starred footnote commands such as \footnote* shown above causes out-of-order progress of the counter to make it hard to have a consistent counter value at \end {paracol}. The command \fncounteradjustment is to let \end{paracol} adjust the value of the counter based on its value at \begin{paracol} and the number of footnote commands in the environment. The command \nofncounteradjustment is to tell \end{paracol} to do nothing as in default.

- Though \footnoteplacement with p(age-wise) or m(erged) argument does \fncounteradjustment while that with c(olumn) does \nofncounteradjustment inside of it, you can override these settings by explicitly putting a counter adjustment command after \footnoteplacement.
- The effect of \fncounteradjustment is shown in Section 8.

\belowfootnoteskip

The typesetting parameter specifies the amount of the space inserted below footnotes of single-column pre-environment stuff if it does not have bottom floats. The default amount is 0 pt, i.e., no space is added.

7.7 Commands for Coloring Texts and Column-Separating Rules

 $\columncolor[mode]{color}[col]$

 $\normalcolumncolor[col]$

The command \columncolor declares that the *default color* of a column is *color* or what it specifies by the combination with the optional *mode*. The command \normalcolumncolor declares the default color is what \normalcolor specifies, i.e., black usually. The target column of these commands is that in which the commands reside, or *col* if it specified.

- The command may be outside of paracol environment. If so and *col* is not provided, the target column is the leftmost 0.
- The default color declaration is *global*. Therefore, even if the command appears in a **paracol** environment (and even in some grouping structure in it), the declaration will be kept effective after **\end{paracol}** to determine the default color of the specified column in succeeding **paracol** environments.

 $^{^{25}}$ Not only for the sake of it, but also for being familiar with this command which could have some advanced feature, for example to put gathered footnotes into a specific column, someday.

- To give a color to texts (and maybe other stuff) in a column correctly, you need to load color package or its relative (e.g., xcolor) which the implementation of coloring in paracol relies on.
- Coloring with \color[mode]{color} and other coloring commands in paracol environments is of course allowed. One caution is that the \color decides the color for following texts until other specification is given or the group surrounding the command is closed. Therefore, \switchcolumn does not affect the coloring but a color given to the texts in a column is also applied to the texts in the column to be switched to. This irrelativeness of coloring and column-switching is shown in the example below.

This column is colored blue because This column is colored red because \columncolor{blue} \columncolor{red} is specified. Here we have a \switchcolumn. is specified. The color of this paragraph is green because Now the color of the right column is changed we are still in the environment of green colto green because oring, which we are now closing. \begin{color}{green} is given prior to this paragraph. Now we Since the coloring environment has been have another \switchcolumn to go back to closed, the color of this paragraph is the dethe left. fault blue. Now we have yet another and the

Since this paragraph is outside of the coloring environment, its color is the default red.

The default coloring of columns does not affect anything outside of paracol environment of course, and thus this sentence is not colored²⁶.

\coloredwordhyphenated

last \switchcolumn to the right.

\nocoloredwordhyphenated

The command \coloredwordhyphenated allows the first word following a coloring command such as \color to be hyphenated, but at the same time make it possible that a line is broken before the word. The command \nocoloredwordhyphenated acts oppositely and thus line breaking before the first word and hyphenating it are inhibited. By default, \coloredwordhyphenated is effective.

• The implementation of color package and its relatives makes it impossible that *word* is hyphenated when it appears like {\color{red}*word* ...} or \textcolor{*word* ...}. This inhibition of the hyphenation is sometimes annoying especially when the document is multi-columned and thus a line is narrow and a column is written in a language having long words such as German. Therefore in paracol package, a trick is used to allow the *word* is hyphenated. However this trick being insertion of a null horizontal space has a side effect that the word can have a line break before it. Though this line break is usually unharmful, in a special occasion the break is undesirable and inappropriate by making it possible that the *half-colored* word 'inappropriate' is broken between 'in' and 'appropriate' without hyphenation. Therefore, if you find such a inappropriate break, use \nocoloredwordhyphenated as follows, for example.

{\nocoloredwordhyphenated in\textcolor{red}{appropriate}}

\colseprulecolor[mode]{color}[col] \normalcolseprulecolor[col]

The command **\colseprulecolor** declares the color for *column-separating rules*, being the vertical rules drawn at the center of gaps between columns, is *color* or what it specifies by the combination with the optional *mode*. The command **\normalcolseprulecolor** declares the color of rules is what **\normalcolseprulecolor** specifies, i.e., black usually. If the optional argument *col* is given, these commands specifies the color of the rule in the gap following the column whose ordinal is *col*, rather than all rules.

 $^{^{26}\}mathrm{Or}$ colored black as **\normalcolor** specifies.

• The rules are drawn if LATEX's typesetting parameter \columnseprule for the rule width has nonzero value, e.g., 0.4pt to obey the standard rule thickness. The rules are *not* drawn on page-wise stuff, i.e., pre-environment and post-environment stuff, page-wise floats or (merged or non-merged) page-wise footnotes of course but also spanning texts. Therefore, if a page has spanning texts, the rules are *broken* by them as shown in the red rule example below.

This is a left column paragraph preceding a spanning text. Of cource the rule separating this and the next column starts from the top of this paragraph.

This is a right column paragraph preceding a spanning text given by the \switchcolumn* at its end.

An Example of Spanning Text Given by \subsubsection* Command

Since we have a spanning text above, the red rule separating this and the next column is broken by the text. It is also natural that the rule separating this and the previous column is terminated at the end of this paracol environment.

- To give a color to rules correctly, you need to load color package or its relative (e.g., xcolor) which the implementation of coloring in paracol relies on.
- Once you give a color to rules in a specific gap with the optional *col*, another \colseprulecolor or \normalcolseprulecolor without *col* does *not* change the color of the rule in the gap.

7.8 Commands for Background Painting

 $\backgroundcolor{region}[mode]{color} \\ backgroundcolor{region(x_0,y_0)}[mode]{color} \\ backgroundcolor{region(x_0,y_0)(x_1,y_1)}[mode]{color} \\ backgroundcolor{re$

The command declares that *background painting* of *region* is performed with *color* or what it specifies by the combination of the optional *mode*. The *region* whose background is painted is one of the following.

c(olumn) for all columns, or particular one if region is c[col] to specify its ordinal col.

g(ap) for all gaps between columns, or particular one if *region* is g[col] to specify the ordinal *col* of the column preceding the gap.

 $\mathbf{s}(panning)$ for spanning texts.

- f(loat) for page-wise floats.
- n(ote) for (merged or non-merged) page-wise footnotes.
- p(re/post) for pre-environment and post-environment stuff.
- t(op) for top margin.
- b(ottom) for bottom margin.
- l(eft) for left margin.
- $\mathbf{r}(ight)$ for right margin.

In addition, capitals of the keys above, i.e., C, G, \ldots, L , are also legitimate for *under painting*. For example, you may specify to paint the background of a region, say top margin, by two **backgroundcolor** with t and T and with different color arranging the size of the region of either t or T (or both of them) by the *extension* option shown below.

The optional (x_0, y_0) is to enlarge the region to be painted shifting its left-top and right-bottom corner outside by the dimension x_0 horizontally and y_0 vertically, or to shrink it with negative dimensions. This *extension* can be asymmetric giving another optional (x_1, y_1) so that it acts on the right-bottom corner while let (x_0, y_0) shift only the left-top corner. Moreover, you may make each extension *infinite* by giving 10000 pt (about 3.5 m) to x_0, y_0, x_1 and/or y_1 so that the corresponding region edge is shifted to the paper edge. Furthermore, this *infinite extension* can be terminated at the point α inside the corresponding paper edge by giving 10000 pt $-\alpha$ ($\alpha \leq 1000$ pt) to an extension parameter x_0 , etc.

- A region whose color is not specified is not painted and thus left blank (or kept as painted by **\pagecolor** if you specify it).
- Under-painting of columns and gaps by C and G is made for regions different from those over-painting c and g. That is, under-painting is done ignoring all page-wise stuff and thus the height of the regions is always \textheight + \maxdepth. On the other hand, over-painting is only for chunks shrunk or separated by page-wise stuff.
- You may exploit the following painting order, where x_i is the *i*-th spanning text ($x \in \{s, S\}$) or *i*-th chunk followed by the *i*-th spanning text, *m* and *n* is the number of spanning texts and columns in a page respectively, to overlay a preceding region with a succeeding region, if your *printer* allows overlaid color painting.

$$\begin{split} \mathbf{T} &\to \mathbf{B} \to \mathbf{L} \to \mathbf{R} \to \mathbf{G}[0] \to \dots \to \mathbf{G}[n-1] \to \mathbf{C}[0] \to \dots \to \mathbf{C}[n-1] \\ &\to \mathbf{t} \to \mathbf{b} \to \mathbf{l} \to \mathbf{r} \to \mathbf{N} \to \mathbf{n} \to \{\mathbf{F}, \mathbf{P}\} \to \{\mathbf{f}, \mathbf{p}\} \to \mathbf{S}_1 \to \dots \to \mathbf{S}_m \\ &\to \mathbf{g}_1[0] \to \dots \mathbf{g}_1[n-2] \to \mathbf{c}_1[0] \to \dots \mathbf{c}_1[n-1] \to \mathbf{s}_1 \\ &\to \dots \\ &\to \mathbf{g}_m[0] \to \dots \mathbf{g}_m[n-2] \to \mathbf{c}_m[0] \to \dots \mathbf{c}_m[n-1] \to \mathbf{s}_m \\ &\to \mathbf{g}_{m+1}[0] \to \dots \mathbf{g}_{m+1}[n-2] \to \mathbf{c}_{m+1}[0] \to \dots \mathbf{c}_m[n-1] \end{split}$$

- If you specify b feature by \twosided, background painting is *mirrored* in even-numbered pages so that 1 and L mean right margin, r and R mean left margin, and asymmetric extensions are applied to right-top and left-bottom corners.
- To give a color for background painting correctly, you need to load color package or its relative (e.g., xcolor) which the implementation of coloring in paracol relies on.
- To paint margins and regions having infinite extension correctly, the parameters \paperwidth and \paperheight should be set properly by, for example, a paper selection option of \documentclass.
- Section 10 shows examples of background painting to give you more intutive explanations of \backgroundcolor and its region specifications.

\nobackgroundcolor{region} \resetbackgroundcolor

The command **\nobackgroundcolor** declares that the background of *region* is not painted, where *region* is one of legitimate region specifiers of **\backgroundcolor**. The command **\resetbackgroundcolor** declares no regions are painted and thus gives you the default state.

• If you specified the background painting of c[col] or g[col] by \backgroundcolor, the painting is not canceled by \nobackgroundcolor with c or g but without [col]. Similarly, once you made declarations of background painting of both c and c[col] (resp. g and g[col]), \nobackgroundcolor with c[col] (resp. g[col]) cancels the painting of c[col] (resp. g[col]) but the region will still be painted by the color you gave to c (resp. g).

\pagerim

This is a (kind of) *length command*²⁷ to have the width of the *rim* area placed at each paper edge to inhibit background painting in the area. That is, the inner edges of the area are considered as virtual paper edges to block painting of all margins and regions having infinite extension to the edges, for example in order to avoid printing troubles caused by painting the rim area too close to the real paper edges. The default value of **\pagerim** is 0 to allow paint anywhere in a paper.

7.9 Control of Contents Output

$\ \file \ \col \$

The command inhibits the output of contents information to $file \in \{toc, lof, lot\}$ from columns other than *col*.

- For example, this manual has \addcontentsonly{toc}{0} to inhibit the contents information output from \subsection commands in the right column in Section 4 and 5, or the table should have duplicated entries of sub-sections.
- It must be $file \in \{toc, lof, lot\}$, or you will have an error message of illegal type of contents file.

7.10 Page Flushing Commands

\flushpage

The command flushes pages up to the *top page* in which the leading column resides. Deferred floats which can be put in the pages up to the top page are also flushed.

\clearpage

The command does what flushpage does and then flushes all floats still deferred if any. The deferred float flushing beyond the top page takes place at first for column-wise ones creating float columns for them, and then for page-wise ones creating *float pages* only with page-wise floats, as IAT_EX 's clearpage does outside paracol environment.

\cleardoublepage

The command does what IAT_EX 's \cleardoublepage does outside paracol. That is, it does \clearpage always and then leaves a blank page if it is even-numbered and two-sided p(age) feature is enabled by twoside option of \documentclass or paracol's own \twosided command shown in Section 7.4.

• This command is equivalent to **\clearpage** in **paracol** environments for non-paired parallel-paging because **\clearpage** flushes *both* left and right parallel-pages.

 $^{^{27}\}mathrm{In}$ reality, it is a <code>\dimen</code> register rather than a <code>\skip</code> register.

8 Numbering and Placement of Page-Wise Footnotes

Here we have a simple example of page-wise but not-merged footnotes²⁸.

²⁸Because of the non-merged typesetting, this footnote is put above the example.

First left-column paragraph
$\dots \dots \dots$ with a footnote ²⁹ $\dots \dots \dots$ in it.
Second left-column paragraph
$\dots \dots $

²⁹First left-column footnote.

 $^{30}\mathrm{Second}$ left-column footnote.

 $^{31}{\rm First}$ right-column footnote.

 32 Second right-column footnote. This and all other footnotes above are page-wise and, since footnote typesetting is non-merged, they are put above the post-environment stuff.

As shown above, it is easy to have a reasonable result of footnote numbering and placement as far as your **paracol** environment is completely included in a page and you accept the numbering in left-column-first manner constructing the environment as follows exploiting the fact **footnote** is made global, where b is the value of **footnote** counter at **\begin{paracol}**, i.e., the number given to the footnote just preceding the environment, and thus b = 28 in the example above.

 $\begin{paracol}{2} left-column stuff having n footnotes numbered b+1, b+2, ..., b+n \\ switchcolumn right-column stuff having m footnotes numbered b+n+1, b+n+2, ..., b+n+m \\ end{paracol} \begin{paracol}{c} b \end{paracol} \en$

The real life is, however, tougher than that, because the assumptions above are too optimistic as described in the following subsections.

8.1 Multiple \switchcolumn in a Page

Here we have an example with three switchcolumn commands in a page having six footnotes. Hereafter, footnotes are typeset with $footnoteplacement\{m\}^{33}$.

First left-column paragraph in it. Second left-column paragraph	First right-column paragraph in it. with a footnote ³⁶ in it. It is followed by a $switchcolumn*$.
\dots with a footnote ³⁵ \dots in it.	
It is followed by a \switchcolumn.	
Third and synchronized left-column paragraph .	Second and synchronized right-column paragraph
$\dots \dots \dots \dots$ with a footnote ³⁷ $\dots \dots \dots \dots \dots$ in it.	$\dots \dots $
It is followed by a \switchcolumn.	Third right-column paragraph in it.

 $^{33}\mathrm{And}$ thus this footnote is merged with those in the <code>paracol</code> environment.

 $^{34}{\rm First}$ left-column footnote.

³⁹Third right-column footnote.

³⁵Second left-column footnote.

³⁶First right-column footnote but following the second left-column one.

³⁷Third left-column footnote but following the first right-column one.

 $^{^{38}\}mathrm{Second}$ right-column footnote but following the third left-column one.

The example in the previous page should look weird because the order of the third footnote in the left column 37 and the first in the right 36 are reversed in their numbers and in the stack at the page bottom. However, the result is *natural* because they are numbered and stacked in the order of occurrence in the source .tex as always done in any documents without paracol and with it but column-wise footnote typesetting. Since the paracol cannot maintain the order automatically⁴⁰, you have to maintain it by yourself.

The problem is partly solved by using footnote with its optional argument [num] to number the first right-column and the third left-column footnotes explicitly, i.e., to give num = 37 to the former and num = 36 to the latter. One caution is that you have to remember that footnote with the optional num does not update footnote counter and thus you have to do $setcounter{footnote}{37}$ or $addtocounter{footnote}{2}$ after the third left-column footnote.

This remedy, however, cannot change the stacking order of these two footnotes of course. Therefore, you need another trick with \footnotemark and \footnotetext to stack the third left-column footnote above the first right-column one. More specifically, you can solve the problem inserting

\footnotetext[36] { text for the third left footnote }

somewhere between \footnote commands for the second left-column and the first right-column ones, e.g., at the end of the second left-column paragraph, and attaching its mark to the appropriate word for the footnote by \footnotemark[36], to have the following.

First left-column paragraph \dots in it.	First right-column paragraph in it.
Second left-column paragraph \dots in it.	It is followed by a \switchcolumn*.
It is followed by $footnotetext[43]{text}$ and a	
\switchcolumn.	
Third and synchronized left-column paragraph .	Second and synchronized right-column paragraph
\dots with a footnote whose mark here ⁴³	\dots with a footnote ⁴⁵ \dots in it.
is given by \footnotemark[43] in it.	Third right-column paragraph
It is followed by \addtocounter{footnote}{2} and	\dots with a footnote ⁴⁶ \dots in it.
a \switchcolumn.	

Though this solution gives a good result, however, it has the following two problems. First, you have to explicitly specify the footnote number through the optional arguments [num] of footnote, footnoteext and footnotemark. This problem is quite severe because, for example, if you add a footnote somewhere preceding the paracol environment in question, you have to modify all [num] arguments of footnote-related commands in the environment. This means that when the footnote addition is done in the first page of a 100-page document having paracol environments with explicitly numbered footnotes in every page, you have to make the corrections for environments in 99 pages. The other a little bit less severe problem is that you have to keep footnote counter having correct value by setcounter, addtocounter or <math>stepcounter for footnotes following those with explicit numbering so that their numbers are given by the default action of footnote.

To cope with these two problems, paracol provides you with the *starred* versions of footnote and its relatives as introduced in Section 7.6 and detailedly explained in the next Section 8.2.

 $^{^{40}}$ So far, because the maintenance is extremely tough. But since it is not impossible, some day you could have an improved version of paracol with the automatic ordering.

⁴¹First left-column footnote.

⁴²Second left-column footnote.

⁴³Third left-column footnote given by footnotetext[43] {text} placed at the end of the second left-column paragraph.

⁴⁴First right-column footnote whose number 44 is explicitly given by \footnote[44]{text}.

⁴⁵Second right-column footnote correctly following the first right-column one.

⁴⁶Third right-column footnote.

8.2 Commands \footnote* and Relatives

\footnote*[+disp]{text}
\footnote*[-disp]{text}
\footnote*[disp]{text}

The command is similar to its non-starred counterpart but the explicit numbering with the optional argument is done in *self-relative* or *base-displacement* style. That is, if the optional argument has a leading '+' or '-', the number given to the footnote is f + disp or f - disp respectively where f is the value of footnote counter, or in other words the number given to the last footnote⁴⁷. Otherwise, i.e., the optional argument is a number without +/- sign, the number given to the footnote is b + disp where b is the base value of footnote counter at \begin{paracol} paracol} for the environment in which the command appears, or in other words the number given to the last pre-environment footnote⁴⁸.

In addition, unlike the non-starred version, this command updates footnote counter with the number given to the footnote, i.e., $f \leftarrow f + disp$, $f \leftarrow f - disp$ or $f \leftarrow b + disp$ is performed, so that following **\footnote** without explicit numbering option have numbers f + 1, f + 2 and so on with new f.

• If the optional argument is not provided, it is assumed that [+1] is given and thus \footnote*{text} acts as \footnote{text}.

footnotemark*[[+-]disp]

This command is a mixture of its non-starred counterpart and \footnote*. That is the number for the footnote mark is calculated in the way of \footnote* and footnote counter is updated.

\footnotetext*[[+-]disp]{text}

Without the optional argument [[+-]disp], this command does what \footnotetext{text} does but in addition increments footnote counter before that. With the optional argument, on the other hand, the number given to the footnote text is calculated as done in \footnote, but the footnote counter is not updated.

With these starred commands, you can produce the following using the base-displacement mechanism without worrying about the absolute value of \footnote counter and its change.

First left-column paragraph 	First right-column paragraphin it. in it. It is followed by a \switchcolumn*.
\switchcolumn.	
Third and synchronized left-column paragraph	Second and synchronized right-column paragraph \dots with a footnote ⁵³ \dots in it.
is given by $footnotemark*[3]$ because $51 = 48 + 3$.	Third right-column paragraph
It is followed by a \switchcolumn.	\dots with a footnote ⁵⁴ \dots in it.

 $^{^{47}}$ If it is put by the ordinary \footnote.

⁴⁸Or the last footnote in the previous **paracol** environment, etc.

⁴⁹First left-column footnote.

 $^{^{50}\}mathrm{Second}$ left-column footnote.

⁵¹Third left-column footnote given by $footnotetext*[3]{text}$ placed at the end of the second left-column paragraph to have 51 = 48 + 3.

 $^{^{52}}$ First right-column footnote whose number 52 is given by $footnote*[4]{text}$ because 52 = 48 + 4.

⁵³Second right-column footnote produced by $footnote*[5]{text}$ because 53 = 48 + 5.

⁵⁴Third right-column footnote produced by $footnote{text}$ because 54 = 53 + 1.

The other way to produce the same result except for the absolute footnote numbers is to use the self-relative mechanism and to exploit the progress of footnote counter as follows.

First left-column paragraph in it. Second left-column paragraph in it. It is followed by \footnotetext*{text} and a	First right-column paragraph in it. with a footnote ⁵⁸ in it. It is followed by a \switchcolumn*.
\switchcolumn.	
Third and synchronized left-column paragraph . $\dots \dots$ with a footnote whose mark here ⁵⁷ $\dots \dots$	Second and synchronized right-column paragraph \dots with a footnote ⁵⁹ \dots in it.
is given by $footnotemark*[-1]$ because $57 = 58 -$	Third right-column paragraph
1. It is followed by a \switchcolumn.	\dots with a footnote ⁶⁰ \dots in it.

It depends on the structure of your document which of the base-displacement and self-relative is better. If your document has frequent switching between single- and multi-column text typesetting and thus the contents of a paracol environment is relatively small, the base-displacement is a good choice because you may concentrate on one base value of footnote counter. Otherwise, especially when your document consists of one single and large paracol environment, the base-displacement is almost equivalent to maintaining absolute values and thus the self-relative should be preferred.

Note that if the last footnote or footnotemark in a paracol environment is starred, the command lets footnote counter have some value smaller than that for the last stacked footnote. For example, if the second and third right-column footnotes 59 and 60 are omitted from the example above, the last footnote-related command will be <math>footnotemark*[-1] which makes the counter at $end\{paracol\}$ 57 rather than 58. You may not worry about this problem, however, because $end\{paracol\}$ automatically maintains the counter letting it have b+n where n is the number of footnote and footnotemark in the environment, if the maintenance is ordered by the command fncounteradjustment which is automatically executed by footnoteplacement with the argument p or m.

8.3 Page Break

When a paracol environment with footnotes lays across a page boundary, you could have some weird result even if the environment have just one \switchcolumn as shown below.

First left-column paragraph	First right-column paragraph
in it.	\dots in it.

 $^{55}\mathrm{First}$ left-column footnote.

 $^{56}\mathrm{Second}$ left-column footnote.

⁶⁰Third right-column footnote produced by $footnote{text}$ because 60 = 59 + 1.

⁶¹First left-column footnote.

⁵⁷ Third left-column footnote given by \footnotetext*{*text*} placed at the end of the second left-column paragraph because it follows the second footnote 56.

 $^{^{58}}$ First right-column footnote whose number 58 is given by \footnote{text} because 58 = 57 + 1 and \footnotetext* for 57 lets footnote have the value.

⁵⁹Second right-column footnote produced by $footnote*[+2]{text}$ because 59 = 57 + 2.

Second left-column paragraph	Second right-column paragraph
\dots with a footnote ⁶² \dots in it.	$\dots \dots $

Since the part of the source tex for this example above is fundamentally same as that in p. 30 at the beginning of this Section 8, footnotes are simply numbered in left-column-first manner without any tricks. However it results in giving an impression that two paragraphs in each of both columns at the bottom of the last page have footnote marks of inconsecutive numbers 61 and 63 due to the second left-column paragraph and the footnote 62 in it. More weirdly, the first right-column footnote 63 is not put in the last page where its mark is shown but is stacked below 62 in this page.

The reason why this happens is that a footnote is not immediately put to the bottom of the page where its mark resides but to the page constructing at the time when the footnote is processed at the end of the paragraph in which the corresponding footnote (or footnotetext) occurs⁶⁵. Therefore, it may happen even in an ordinary single-column document or a **paracol**ed multi-column one with column-wise footnotes that a footnote is thrown to the page p+1 next to the page p in which its mark is left, when the mark is placed around the bottom of the page p.

This footnote placement mechanism becomes clearly visible in the example above in which the footnote 63 is processed *after* the second left-column paragraph is processed to complete the last page giving no chance to the footnote placed in the page⁶⁶. Therefore, the solution of this placement problem is to let the first right-column footnote processed *before* the page is broken by the progress of the left-column. That is, in the solution shown below the author inserted **\switchcolumn** after the first left-column paragraph to let the first right-column paragraph and its footnote are processed, and then did **\switchcolumn** again after the right-column paragraph to go back to the left-column.

First left-column paragraph	First right-column paragraph
	in it.
It is followed by a \switchcolumn.	It is followed by a \switchcolumn to go back to the left column.

 $^{^{62}\}mathrm{Second}$ left-column footnote.

 $^{^{63}}$ First right-column footnote weirdly placed here while the footnoted main text is in the previous page.

 $^{^{64}}$ Second right-column footnote whose mark in the main text gives impression that footnote numbering jumps from 62 to 64. 65 More accurately, the footnote is kept in a place in TEX together with other preceding but still unprocessed footnotes and then

 T_{EX} examines them at the end of a paragraph in which a page break is found to decide whether each of them is included in the page just being completed.

 $^{^{66}\}mathrm{In}$ fact, even **\footnote** for the footnote is processed after the page break in this case.

⁶⁷First left-column footnote.

⁶⁸First right-column footnote which is now placed in this page where its mark <u>68</u> resides.

Second left-column paragraph		
\dots with a footnote ⁶⁹ \dots	in i	it.
It is also followed by a \switchcolumn.		

Second right-column paragraph			•	 •					
\dots with a footnote ⁷⁰ \dots						•	in	ı i	it.

Unfortunately, this tactics does not always solve the problem. If a left-column paragraph has a page break in it and a footnote before the break, doing \switchcolumn after the paragraph is too late to let right-column footnotes reside in the page just having been broken, while inserting \switchcolumn before the paragraph should cause incorrect stacking order.

The remedy for this problem is similar to that shown in Section 8.1 to cope with multiple \switchcolumn in a paracol environment. Here it is shown a little bit more formally. Suppose we have a page in a paracol environment in which a page break occurs in p_l -th and p_r -th paragraphs in the left and right columns respectively. Thus we have $p_l - 1$ and $p_r - 1$ completed paragraphs in each of both columns. Let n_l (resp. n_r) be the number of footnotes in the pre-break left-column (resp. right-column) paragraphs, and m_l (resp. m_r) be the number of pre-break footnotes in the p_l -th (resp. p_r -th) paragraph. Thus we have $n_l + m_l$ (resp. $n_r + m_r$) footnotes in the left (resp. right) column of the page before the break. The following construct assures that those footnotes are properly numbered and stacked at the bottom of the page.

First to $(p_l - 1)$ -th paragraphs with n_l footnotes in total given by $footnote{text}$. footnotetext*{1st footnote in p_l -th paragraph}

 $\times footnotetext*{m_l-th footnote in p_l-th paragraph} \times to (p_r - 1)-th paragraphs with n_r footnotes in total given by \footnote{text}. \footnotetext*{1st footnote in p_r-th paragraph}$

 $\times footnotetext*{m_r-th footnote in p_r-th paragraph} \switchcolumn$

 p_l -th paragraph whose first footnote mark is given by $footnotemark*[-(m_l+n_r+m_r-1)]$, while second to m_l -th ones are given by footnotemark without * nor optional [num]. The first subsequent footnotes beyond the page break, if any, is given by $footnote*[+(n_r+m_r+1)]{text}$ while further subsequent ones are given by $footnote{text}$.

 p_r -th paragraph whose first footnote mark is given by \footnotemark*[- (m_r+k_l-1)] where k_l is the number of left-column footnotes beyond the break, while second to m_r -th ones are given by \footnotemark. The first subsequent footnotes beyond the page break, if any, is given by \footnote*[+ (k_l+1)] {text}, while further subsequent ones are given by \footnote{text}.

The example shown in the next two pages is for the case of $p_l = p_r = n_l = n_r = m_l = m_r = k_l = 2$.

[\]switchcolumn

 $^{^{69}}$ Second left-column footnote whose number 69 follows the right-column footnote 68 in the last page.

 $^{^{70}}$ Second right-column footnote whose number 70 follows the left-column footnote 69.

First left-column paragraph with two footnotes
and here 72 also by \footnote{text}
followed by a series of \footnotetext*{ <i>text</i> } and
then a \switchcolumn.
Second left-column paragraph across two pages
with two pre-break footnotes
79
\dots here ⁷³ by \footnotemark*[-5] because $m_l + n_r +$
here ⁷³ by \footnotemark*[-5] because $m_l + n_r + m_r - 1 = 2 + 2 + 2 - 1 = 5$ and thus $73 = 78 - 5$
here ⁷³ by \footnotemark*[-5] because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by \footnotemark
here ⁷³ by $footnotemark*[-5]$ because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by $footnotemark$
$\label{eq:main_state} \begin{array}{l} \dots \mbox{ here}^{73} \mbox{ by \footnotemark*[-5] because } m_l + n_r + \\ m_r - 1 = 2 + 2 + 2 - 1 = 5 \mbox{ and thus } 73 = 78 - 5 \dots \\ \dots \mbox{ and here}^{74} \mbox{ by \footnotemark} \dots \dots \\ \end{array}$
here ⁷³ by \footnotemark*[-5] because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by \footnotemark
here ⁷³ by \footnotemark*[-5] because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by \footnotemark
here ⁷³ by \footnotemark*[-5] because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by \footnotemark
here ⁷³ by \footnotemark*[-5] because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by \footnotemark
here ⁷³ by \footnotemark*[-5] because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by \footnotemark
here ⁷³ by $footnotemark*[-5]$ because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by $footnotemark$
here ⁷³ by $footnotemark*[-5]$ because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by $footnotemark$
here ⁷³ by \footnotemark*[-5] because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by \footnotemark
here ⁷³ by $footnotemark*[-5]$ because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by $footnotemark$
here ⁷³ by $footnotemark*[-5]$ because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by $footnotemark$
here ⁷³ by $footnotemark*[-5]$ because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by $footnotemark$
here ⁷³ by $footnotemark*[-5]$ because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by $footnotemark$
here ⁷³ by $footnotemark*[-5]$ because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by $footnotemark$
here ⁷³ by $footnotemark*[-5]$ because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by $footnotemark$
here ⁷³ by $footnotemark*[-5]$ because $m_l+n_r+m_r-1=2+2+2-1=5$ and thus $73=78-5$ and here ⁷⁴ by $footnotemark$.

⁷¹First left-column footnote given by \footnote{text}.
⁷²Second left-column footnote also given by \footnote{text}.
⁷³Third left-column footnote given by \footnotetext*{text}.
⁷⁴Fourth left-column footnote given by \footnotetext*{text}.
⁷⁵First right-column footnote given by \footnote{text}.
⁷⁶Second right-column footnote also given by \footnote{text}.
⁷⁷Third right-column footnote given by \footnotetext*{text}.
⁷⁸Fourth right-column footnote given by \footnotetext*{text}.

\dots here ⁷⁵ by \footnote{ <i>text</i> }
×
followed by a series of \foothotetext*{ <i>text</i> } and
then a \switchcolumn.
Second right-column paragraph across two pages
Second fight column paragraph across two pages
with two pre-break footnotes
with two pre-break footnotes here ⁷⁷ by \footnotemark*[-3] because $m_r+k_l-1 = 2+2-1 = 3$ and thus $77 = 80-3$ and here ⁷⁸ by \footnotemark
with two pre-break footnotes here ⁷⁷ by \footnotemark*[-3] because $m_r+k_l-1 = 2+2-1 = 3$ and thus $77 = 80-3$ and here ⁷⁸ by \footnotemark
with two pre-break footnotes here ⁷⁷ by \footnotemark*[-3] because $m_r+k_l-1 = 2+2-1 = 3$ and thus $77 = 80-3$ and here ⁷⁸ by \footnotemark
with two pre-break footnotes here ⁷⁷ by \footnotemark*[-3] because $m_r+k_l-1 = 2+2-1 = 3$ and thus $77 = 80-3$ and here ⁷⁸ by \footnotemark
with two pre-break footnotes here ⁷⁷ by \footnotemark*[-3] because $m_r+k_l-1 = 2 + 2 - 1 = 3$ and thus $77 = 80 - 3$ and here ⁷⁸ by \footnotemark
with two pre-break footnotes here ⁷⁷ by \footnotemark*[-3] because $m_r+k_l-1=2+2-1=3$ and thus $77=80-3$ and here ⁷⁸ by \footnotemark
with two pre-break footnotes here ⁷⁷ by \footnotemark*[-3] because $m_r+k_l-1=2+2-1=3$ and thus $77=80-3$ and here ⁷⁸ by \footnotemark
with two pre-break footnotes here ⁷⁷ by \footnotemark*[-3] because $m_r+k_l-1=2+2-1=3$ and thus $77=80-3$ and here ⁷⁸ by \footnotemark
with two pre-break footnotes here ⁷⁷ by \footnotemark*[-3] because $m_r+k_l-1=2+2-1=3$ and thus $77=80-3$ and here ⁷⁸ by \footnotemark

First right-column paragraph with two footnotes
and two post-break footnotes	and two post-break footnotes
$\dots here^{79}$ by \footnote*[+5]{ $text$ }	here ⁸¹ by \footnote*[+3]{ <i>text</i> }
\dots and here ⁸⁰ by \footnote{ <i>text</i> }	\dots and here ⁸² by \footnote{ <i>text</i> }
followed by a \switchcolumn.	

Note that though the remedy works well as shown above, it is not a good idea to do that when you are writing draft versions of your document because page break points go up and down by your modifications to the document. Therefore, it is recommended to put all footnotes by non-starred \footnote until your document becomes perfect except for footnote numbering and placement and then to adjust them by the technique described in this section.

⁷⁹Fifth left-column footnote given by \footnote*[+5] because $n_r + m_r + 1 = 2 + 2 + 1 = 5$ and thus 79 = 74 + 5. ⁸⁰Sixth left-column footnote given by \footnote{*text*}.

⁸¹Fifth right-column footnote given by footnote*[+3] because $k_l + 1 = 3$ and thus 81 = 78 + 3.

⁸²Sixth right-column footnote given by \footnote{text}.

9 Two-Sided Typesetting and Parallel-Paging

This and the next section are typeset with $\pm 0.5 \text{ m}^{83}$. This setting makes the left side or outside margin of this evennumbered page is narrower than that of the previous pages because the author reduced the effective right side margin being calculated from $\pm 0.5 \text{ m}^{83}$. This setting makes the left side or outside margin of this page enlarged by 125%, as well as the right side and outside margin of the next odd-numbered page specified by $\pm 0.5 \text{ m}^{12}$.

Next, we see the effects of c and m features by the paracol environment below for which \columnratio{0.6} and \marginparthreshold{0} are declared to make the *inside* columns (right ones in even-numbered pages) are wider than the *outside* ones and all marginal notes go to outside (left in even-numbered pages) margins.

First This is the first paragraph in the nar-This line of the first paragraph of the inside column-0 has marginal rower, italicized and outside column-1. In a marginal note. Now the author puts a few dummy lines to note from this paragraph, we shortly have a marginal keep a space below the marginal note. column-0. note, italicized too, which goes to the out-side margin shared by all marginal notes Firstfrom both columns. The marginal note marginal given here is placed its natural position note from and its first line is aligned to the first line column-1. of the second sentence of this paragraph by exploitation of the space between two marginal notes from the column-0, though we already have had three notes from the column. Now the author puts another marginal note whose first line would be aligned to Second that of this paragraph, but it is pushed This line of the second paragraph of the inside column-0 marginal down below the second marginal note from also has a marginal note. Now the author puts a few dummy the column-0 because two notes conflict note from lines again but this time to go down to the bottom of the page. column-0. with each other over the $space^{84}$. Note that Second since the note from this column is given marginal after that from the column-0 was given, note from the conflict is solved pushing the note from column-1. this column down rather than that from the column-0. Now the author puts a few dummy lines to go to the second last line of this page. This is the third paragraph of the out-This is the third paragraph of the inside column-0 having a side column-1, which becomes right shortly page break in it. Since shortly we will be in an odd-numbered

⁸³This document itself does not have twoside option in its \documentclass but the inconsistency between the option and \twosided is not visible because \pagestyle is plain.

 $^{^{84}}$ Since the author is temporarily disabling the warning from marginal note placement mechanism of IAT_EX, pushing down the second marginal note from column-1 is silently performed when you process this document.

page 39 (now), this wider column is now left one keeping it inside, while the marginal note given in the first line of this page goes to right and outside. Now we will have a \switchcolumn below this paragraph to go to the column-1 and back to the previous page 38.

by the page break. The third marginal note Third is given in the first line of this page, but marginal it is pushed down again due to the conflict note from with the note from the column-0. Third

ment is

closed.

marginal

Note that the position of the last marginal note in the **paracol** environment which we just have closed *note from* affects the marginal note placement in post-environment stuff. For example, the marginal note given in the first *column-1*. line of this paragraph is pushed down. Marginal

We will see a few examples of parallel-paging shortly, but before that we will have an intentional black note given page to make the first page of the example odd-numbered to avoid you have an impression that its layout is after incorrect⁸⁵ because if it were in an even page you would see the *outside* third and fourth supplementary *columns* paracol at first.

 $^{^{85}\}mathrm{At}$ least the author himself had such impression without the blank page.

(intentionally blanked page)

9.1 Example of Paired Parallel-Paging

Shortly we will start a paracol environment by \begin{paracol}[2]{4} having four columns but two for each of left and right paired parallel-pages. Since the author declares \columnratio{0.6}[0.5], the columns in left pages are made unbalanced while those in right pages are balanced.

This is the first paragraph of the leftmost column-0, whose first line has a marginal note placed in the right margin because the setting of \marginparthreshold being 0 is still effective and we are in the odd-numbered page 41. Now we have a \switchcolumn to the next column-1.

This is the first paragraph of the sec-Marginal ond and right column-1 in the left parallel- note from page. We shortly give an italicized mar-column-0. ginal note carefully, so that it does not conflict with the marginal note from the column-0. That is, now the author puts Marginal the note. Now we have a \switchcolumn note from to the next column-2. column-1.

A Spanning Text: though this is wider than the page width, this text does not span the boundary between the left and right parallel-pages.

We have restarted this column-1. We have come back to this column-0. The space above the This paragraph has a footnote⁸⁶ as shown bespanning text is due to the synchronization because two paragraphs in the column-2 are significantly taller in total than the low. paragraphs in other columns. As the spanning text itself says, it cannot extend to the right parallel-page. The author puts dummy lines to go to the page bottom. Now we will have a page break shortly. You could be sur-After the page break below, this column prised by seeing this column is not in the left parallel-page after also goes to the right page together with the

 $^{^{86}}$ This footnote is put in the left parallel-page together with another footnote below given in the column-2 in the right parallel-page.

page. 87 This footnote is *not* put in the right parallel-page though it is given in the column-2 in the right parallel-page and thus its reference is in the column, of course.

This is the first paragraph of the column-2 being the left column of the right parallel-page. Though we are in a page different from that column-0 and 1 reside in, this page is still numbered 41 because the left and right page is paired. Therefore, the left margin of this page is narrower than the right margin because the page number is odd.

You have to notice the first paragraph does not start from the page top but above it we have some space of exactly same size as the pre-environment stuff shown in the left parallel-page. Therefore, the top of the first paragraphs in all columns are aligned. The marginal note given in the first line of this paragraph goes to the right margin of this page because of the \marginparthreshold setting and the parity of this page. Now we have a \switchcolumn to the next column-3.

We have a few other materials not shown in right parallel-pages. The space above this paragraph is for the spanning text placed in the left parallel-page. The page-wise footnote given here⁸⁷ is also not in this page but in the left. Finally, the author has put a page-wise figure spanning columns just before \switchcolumn by which we left this column, but it will be in the right page 42 together with column-0 and 1.



page, its space and that of 86 make this and the next

This is the first paragraph in the last rightmost Marginal column-3 whose width is equal to that of the column- note from 2. The marginal note given in the first line goes column-3. to right and does not conflict with that from the column-2. We are now going back to the column-0 by a \switchcolumn* with a spanning text.

Marginal note from column-2.

As expected, this line is aligned to the first line of the paragraph in the column-2 as well as those in column-0 and 1. It is also consistent the first lines including that of this paragraph are not indented because the spanning text is given by \subsection* which makes first paragraphs unindented.



After the page break we will have shortly, this column becomes the leftmost in the left parallel-page, Another marginal note from column-3. as you are seeing now, but still outermost as well as the marginal note in the outside left margin. columns shorter in the previous page. Similarly, we have a space above for the page-wise figure shown in the right page.

page-wise figure given in column-2

Figure 11: A Page-Wise Figure

Another marginal note from column-1. column-0 and is placed outside (left) in the page, as well as the marginal note in this right page but in the outside margin. the break but in the right one. This is because the feature c is enabled to swap not only columns in a page but also the left and right paired parallel-pages when they are even-numbered. The other feature p makes the left outside margins of this right and the previous left pages wider than the right inside margins.

Now you are seeing yet another material placed only in the page in which the column-0 resides and thus being the right page now, i.e., this paragraph and the next one in the post-environment stuff. You might be disappointed by the fact the *outside* pages, i.e., left in this page 42 and right in the previous page 41, cannot have page-wise stuff but it is what the author can do now for the version 1.3 and thus you have to wait some future versions in which the author could devise a mechanism to exploit the corresponding space in the pages⁸⁸. In addition, you might think it is weird that the c feature of \twosided swaps columns and paired pages. However this swapping is a natural consequence of the combination of column-swapping and paired parallel-paging. Therefore, you can simply disable the c feature (maybe together with other features) to have more intuitive results.

In the next Section 9.2, you will see another kind of parallel-paging namely non-paired one. Before that, we need a blank page to let the non-paired parallel-paging start from an even-numbered page so that a left and right page pair comprises a double spread. A short remark on the blank next page is that it does not have a right counterpart parallel-page because the page is outside **paracol** environments and does not have any portion from the environments⁸⁹.

⁸⁸You might complain the immaturity of parallel-paging and might claim that it should be included in **paraco**l after the author implements the mechanism. In fact the author himself is frustrated current features of parallel-paging but he dared to release the version 1.3 knowing that there are people who happily typeset their parallel-paged documents with the current limited features. ⁸⁹To illustrate this fact, the author dares to put a real blank page rather than stepping the **page** counter.

(intentionally blanked page)

9.2 Example of Non-Paired Parallel-Paging

This and following three pages are to show an example of non-paired parallel-paging, in which the author keeps the setting of \twosided , \columnratio and \mrginparthreshold unchanged. The arguments of $\begin {paracol} for column population are also unchanged to have <math>2 + 2$ configuration, but the first argument is followed by * for non-paired typesetting. That is, the environment below starts by $\begin{paracol}[2]*{4}. The contents of the environment is also almost same as the previous Section 9.1, while bold-faced words show the difference from the paired typesetting.$

Marginal note from column-0.

Marginal note from column-1.

This is the first paragraph of the leftmost column-0, whose first line has a marginal note placed in the **left** margin because the setting of \marginparthreshold being 0 is still effective and we are in the **even**-numbered page 44. Now we have a \switchcolumn to the next column-1. This is the first paragraph of the second and right column-1 in the left parallelpage. We shortly give an italicized marginal note carefully, so that it does not conflict with the marginal note from the column-0. That is, now the author puts the note. Now we have a \switchcolumn to the next column-2.

A Spanning Text: though this is wider than the page width, this text does not span the boundary between the left and right parallel-pages.

We have come back to this column-0. The space above the We have restarted this column-1. This paragraph has a footnote⁹⁰ as shown bespanning text is due to the synchronization because two paragraphs in the column-2 are significantly taller in total than the low. paragraphs in other columns. As the spanning text itself says, it cannot extend to the right parallel-page. The author puts dummy lines to go to the page bottom. Now we will have a page break shortly. You will not be After the page break below, this column surprised by seeing this column is still in the left parallelalso stays in the left page together with

 $^{^{90}}$ This footnote is put in the left parallel-page together with another footnote below given in the column-2 in the right parallel-page.

page. 91 This footnote is *not* put in the right parallel-page though it is given in the column-2 in the right parallel-page and thus its reference is in the column, of course.

This is the first paragraph of the column-2 being the left column of the right parallel-page. **Since we are in the page next to** that column-0 and 1 reside in, this page is numbered **45** because the left and right page is **non-paired**. Therefore, the left margin of this page is narrower than the right margin because the page number is odd.

You have to notice the first paragraph does not start from the page top but above it we have some space of exactly same size as the pre-environment stuff shown in the left parallel-page. Therefore, the top of the first paragraphs in all columns are aligned. The marginal note given in the first line of this paragraph goes to the right margin of this page because of the \marginparthreshold setting and the parity of this page. Now we have a \switchcolumn to the next column-3.

We have a few other materials not shown in right parallel-pages. The space above this paragraph is for the spanning text placed in the left parallel-page. The page-wise footnote given here⁹¹ is also not in this page but in the left. Finally, the author has put a page-wise figure spanning columns just before \switchcolumn by which we left this column, but it will be in the **left** page **46** together with column-0 and 1.



page, its space and that of 90 make this and the next

This is the first paragraph in the last rightmost Marginal column-3 whose width is equal to that of the column- note from 2. The marginal note given in the first line goes column-3. to right and does not conflict with that from the column-2. We are now going back to the column-0 by a \switchcolumn* with a spanning text.

Marginal note from column-2.

As expected, this line is aligned to the first line of the paragraph in the column-2 as well as those in column-0 and 1. It is also consistent the first lines including that of this paragraph are not indented because the spanning text is given by \subsection* which makes first paragraphs unindented.



umn is kept being the rightmost in the right

page-wise figure given in column-2

Figure 12: A Page-Wise Figure

Another marginal note from column-1.

page after the break. This is because the feature c is not effective in non-paired parallel-paging. The other feature p consistently makes the left outside margins of this and the previous page in which this column resides wider than the right inside margins. the column-0 and is placed **inside (right)** in the page, as well as the marginal note in this **left** page **still** in the outside margin.

As the post-environment stuff in Section 9.1 is, this paragraph being the post-environment stuff of the non-paired parallel-pages appears only in the parallel-page in which the column-0 belongs to, and thus in the left parallel-page in this case.

columns shorter in the previous page. Similarly, we have a space above for the page-wise figure shown in the **left** page.

parallel-page, as you are seeing now, and still out- Anotherermost as well as the marginal note in the outside marginalright margin.note fromcolumn-3.

10 Examples of Background Painting

10.1 Fundamental Painting

As you undoubtedly notice, this page and a few pages following it are colorfully painted. For this and the next three pages, the author declared the background color of each region as follows.

\backgroundcolor{t}[rgb]{0.7,0,0}	% dark red for top margin
\backgroundcolor{b}[rgb]{0.8,0.6,0}	% dark orange for bottom margin
\backgroundcolor{1}[rgb]{0,0,0.7}	% dark blue for left margin
\backgroundcolor{r}[rgb]{0,0.7,0}	% dark green for right margin
$\backgroundcolor{c[0]}[rgb]{1,0.8,1}$	% pink for colunmn-0
<pre>\backgroundcolor{c[1]}[rgb]{1,1,0.8}</pre>	% cream yellow for column-1
\backgroundcolor{g}[rgb]{0.8,1,1}	% light blue for the gap
\backgroundcolor{f}[rgb]{0.8,0,1}	% purple for page-wise floats
$backgroundcolor{n}[rgb]{0.8,0.6,1}$	% light purple for page-wise footnotes
\backgroundcolor{p}[rgb]{0.8,1,0.6}	% pale green for pre/post-environment
$\backgroundcolor{s}[rgb]{0.8,0.8,0.8}$	% light gray for spanning texts

Therefore, the background of this pre-environment paragraph and other stuff above is painted by pale green. Since the author set pagerim to be 5 pt, you will see unpainted strips of 5 pt wide at all paper edges surrounding painted regions. For this and the next three pages, twosided[pcm] is declared to enable p, c and m features but to disable the b feature. Therefore, though this page 48 is even and thus the left outside margin is wider than the right inside one, the backgrounds of l(eft) and r(ight) margins are painted by dark blue and dark green respectively.

As explained in the right column-0, the background of this left and outside column-1 is painted by cream yellow as \backgroundcolor{c[1]} specifies. Now we have a \switchcolumn* with a spanning text to show the background painting for it⁹². This column-0 is now right and inside because of the c feature of \twosided is enabled. On the other hand, the background is this column is painted by pink because \backgroundcolor for c[0] specifies so. That is, the column ordinals optionally given to c(olumn) (and g(ap)) regions are *logical* ones not always corresponding to their *physical* positions in a page.

The background of this s(panning text) region is painted by light gray

See the right column for the reason why this paragraph is to show how the first line of a paragraph just below a spanning text is placed in the painted region.

See the right column for what we are now doing.

Now we have a **\flushpage** to see the background painting for a material not shown in the page, i.e., a page-wise float.

⁹²Since the footnotes in this **paracol** environment are page-wise and merged, and **\backgroundcolor{n}** specifies light purple, the background of this (foot)**n**(ote) region is painted by the color.

	f(loat) region for this page-wise figure is painted by purple		
Figure 13: A Page-Wise Figure			
0 is	Since we are now in an odd-numbered page 49, this column- now a left one and is still painted by pink of course.	this llow.	3
r	This paragraph is to show how the last line of a page without		

This paragraph is to show how the last line of a page witho page-wise footnotes is placed in the painted region.

See the comment in the left column.

See the right column for the reason why we have this almost blank page.	This page is to show how the page without any page-wise stuff looks like.
See the right column for what will happen shortly.	Shortly we will close this paracol environment in the next page.

Now we are closing this **paracol** environment to show how its post-environment stuff is painted. See the left column for the reason why we are now closing the environment.

The background of this paragraph in p(ost-environment) region is also painted by pale green, because postenvironment stuff can be pre-environment stuff at the same time as we see shortly.

This short **paracol** environment illustrates how the preenvironment stuff of this environment, or the post-environment stuff of the last environment in other words, is painted. Therefore, the author does not have much to say in this column, except for giving a footnote here⁹³.

Before moving to the next example, one caution is given for background painting of merged footnotes. As the footnote 93 itself says, merged footnotes given in the last page of a paracol environment are considered as belonging to post-environment stuff. Therefore, the footnote 93 is painted by pale green as well as another footnote given now⁹⁴.

⁹³Since this footnote is merged with that in the post-environment stuff, it is considered as a part of post-environment stuff and thus painted by pale green rather than light purple.

⁹⁴Since this footnote really belongs to post-environment stuff, its background is painted by pale green naturally.

10.2 Mirrored Painting and Enlarging/Shrinking/Shifting Regions

At a glance, this and the next three pages look painted similarly to previous four pages, but by a careful examination you should notice two important differences. The first one is found in the colors of left and right margins. As the author enabled all features of \twosided including b for mirroring and we are now in an even-numbered page 52, the left and outside margin is painted by dark green for the region r(ight margin), while the right and inside one is painted by dark blue for 1(eft margin).

The other is that regions are enlarged, shrunk or shifted by 4 pt by the following \backgroundcolor commands with extensions.

$backgroundcolor{t(0pt,0pt)(0pt,-4pt)}[rgb]{0.7,0,0}$	% B up
\backgroundcolor{b(0pt,-4pt)(0pt,0pt)}[rgb]{0.8,0.6,0}	% T down
\backgroundcolor{1(0pt,4pt)(-4pt,4pt)}[rgb]{0,0,0.7}	% R left T/B outside
\backgroundcolor{r(-4pt,4pt)(0pt,4pt)}[rgb]{0,0.7,0}	% L right T/B outside
$\backgroundcolor{c[0](4pt,4pt)}[rgb]{1,0.8,1}$	% all edges outside
$\backgroundcolor{c[1](4pt,4pt)}[rgb]{1,1,0.8}$	% all edges outside
<pre>\backgroundcolor{g(-4pt,4pt)}[rgb]{0.8,1,1}</pre>	% L/R inside & T/B outside
\backgroundcolor{f(4pt,4pt)(4pt,-4pt)}[rgb]{0.8,0,1}	% L/R outside & T/B up
\backgroundcolor{n(4pt,-4pt)(4pt,4pt)}[rgb]{0.8,0.6,1}	% L/R outside & T/B down
<pre>\backgroundcolor{p(4pt,4pt)}[rgb]{0.8,1,0.6}</pre>	% all edges outside
<pre>\backgroundcolor{s(4pt,-4pt)}[rgb]{0.8,0.8,0.8}</pre>	% L/R outside & T/B inside

In the comments above, L(eft), R(ight), T(op) and B(ottom) mean edges moved by a given extension. Therefore, for example, "L/R outside & T/B up" for f(loat) region means it is enlarged horizontally and shifted up vertically by the asymmetric extension (4pt, 4pt)(4pt, -4pt). These a little bit complicated setting of extensions are to solve the problems in the fundamental example shown in previous four pages, namely too strict definition of the regions to be painted. That is, both vertical edges of regions having texts, e.g., c(olumn) regions, should look too close to the first and last letters. Similarly both horizontal edges of those regions seem too close especially when the first line is tall (e.g., the section title in p. 48 and the page-wise figure in p. 49) and the last line of a column is followed by spanning text or post-environment stuff. Therefore, the author made fine tuning moving inside edges of margins outside, and so on. We will come back this issue after exemplifying the effect of the tuning.

This paragraph is surrounded by spaces of a small but comfortable amount as well. ⁹⁵. By the tuning to enlarge this c(olumn) region, this paragraph has comfortable spaces above and below it, as well as at the both side edges.

The background of this s(panning text) region is painted by light gray and enlarged horizontally but shrunk vertically

See the right column for the reason why this paragraph is here.	This paragraph is to show how well the first line of a paragraph just below a spanning text is separated from the boundary of two painted regions.
See the right column for what we are now doing.	By enlarging this $c(\text{olumn})$ region and shift the $(\text{foot})n(\text{ote})$ region down, this paragraph has a comfortable amount of space below it.

 95 Shifting this (foot)n(ote) region down a little bit, the space below this footnote and above the top edge of the b(ottom margin) region is enlarged.

shifting up this f(loat) region gives us a small space above the top edge of the rectangle

Figure 14: A	A Page-Wise	Figure
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Similarly to other paragraphs below page-wise stuff, this paragraph is well separated from the bottom edge of the f(loat) region above.

See the comment in the left column for the intention of placing this paragraph here.

As in the case of the line above page-wise footnotes, the last line of this paragraph has a sufficient space separating it from the top edge of the b(ottom margin) region.

See the comment in the left column, too.



This page is to show how the page without any page-wise stuff looks like. As you are seeing, the space above this paragraph is sufficient and comfortable.

See the right column for what will happen shortly.

Shortly we will close this **paracol** environment in the next page.

Now we are closing this paracol environment to show how this paragraph is separated from the boundary of c(olumn) and p(ost-environment) regions.

See the left column for the reason why we are now closing the environment.

The background of this paragraph in p(ost-environment) region is painted by pale green as done in p. 51, but its top and bottom edges *look* shifted down and up to give spaces below and above the last and first paragraphs in paracol environments, respectively.

This short **paracol** environment illustrates how the preenvironment stuff of this environment, or the post-environment stuff of the last environment in other words, is painted. Therefore, the author does not have much to say in this column, except for giving a footnote here⁹⁶.

In the setting with \backgroundcolor commands in p. 52, the author carefully moved contacting edges of regions. For example, to enlarge c(olumn) regions, the inside edges of l(eft margin) and r(ight margin) regions are moved outside, and both vertical edges of the g(ap) region shifted toward its inside. As for the horizontal edges, the bottom edges of t(op margin) and f(loat) regions are moved up, the top edges of b(ottom margin) and (foot)n(ote) regions are moved down, and both top and bottom edges of the s(panning text) region are shifted toward its inside.

These edge shifting could make a region too narrow or too much shifted resulting in a material in it overreaching its boundary, especially in vertical shifting of horizontal edges. However we can exploit some large space automatically or manually inserted above and/or below the material to avoid overreaching. That is the author exploited the following spaces; **\headsep** below the page head (though it is empty in this document); **\dbltextfloatsep** below the bottom-most page-wise float; spaces that **\subsection*** inserts above and below it together with manually inserted **\medskip** below it; **\skip\footins**⁹⁷ above the first footnote which the author enlarged by 4pt temporarily for this and the next subsections; and **\footskip** from the bottom edge of text area to that of the page number.

Now you might notice that the explanation above does not mention the p region for pre-environment and post-environment stuff. As you should find in the settings, this region is enlarged horizontally *and vertically* so that its top and bottom edges are moved up and down when the region is at the top or bottom of a page, as you are seeing now and find in p. 52. However, this enlargement of course has a side effect that the region collides against c(olumn) and g(ap) regions also enlarged vertically making them overlapped. This overlap will be invisible with most of *printers* because, as shown in Section 7.8, p region is painted *before* c and g regions are painted. In addition, since relatively large spaces of **bigskip** are manually inserted before each **begin{paracol}** and after each **end{paracol}**, texts in pre-environment and post-environment stuff are well separated from region boundaries.

This overlay painting c and g over p, however, might produce an unexpected result with some printer with which, for example, two colors are *blended* in the thin overlapped strip⁹⁸. Unfortunately, this overlay painting is inevitable in the current version 1.3, but in a future version, hopefully 1.4, more sophisticated *position-dependent* region definition, for example, to shift the top edge of p region only when the region is at the top of page, could be introduced.

Another remark is that the mirroring specified by the **b** feature of \twosided works not only on the colors of side margins but also on their asymmetric shrinkage. That is, the asymmetric shifts of vertical edges of 1 and **r** regions correctly performed irrespective of their physical positions, i.e., even when the 1 (resp. **r**) region is at the right (resp. left) margin and the edge to be shift is the left (resp. right) one rather than right (resp. left).

 $^{^{96}}$ As the footnote 93 in p. 51, this merged footnote is a part of post-environment stuff and thus painted by pale green rather than light purple.

⁹⁷This is a kind of "length command" maybe not widely known.

⁹⁸For example, a dvi previewer dviout produces such a blended result with the default setting of coloring.

10.3 Regions with Infinite Extensions

You are now seeing another background painting much different from previous two examples. That is, after disabling painting of t, b, l, r and g regions by \nobackgroundcolor, the author gave the followings for painting this and the next pages.

\backgroundcolor{c[0](4pt,4pt)(0.5\columnsep,4pt)}[rgb]{1,0.8,1} \backgroundcolor{c[1](0.5\columnsep,4pt)(4pt,4pt)}[rgb]{1,1,0.8} \backgroundcolor{C[0](10000pt,10000pt)(0.5\columnsep,10000pt)}[rgb]{1,0.8,1} \backgroundcolor{C[1](0.5\columnsep,10000pt)(10000pt,10000pt)}[rgb]{1,1,0.8}

The first two lines above is different from the previous declaration because inside edges of c[0] and c[1] regions are shifted toward outside of them and thus inside of unpainted g region so that the edges are contacted. On the other hand, the last two lines are for *under-painting* of columns and has *infinite extension* to make top, bottom and outside edges of C regions reaching to the corresponding paper edges. Since this under-painting is done with colors same as those of over-painting of c regions, you will have an impression that the paper is two-toned and page-wise stuff are pasted on the paper⁹⁹.

As explained in the right column, this c[1] region also has an invisible left edge shifted left by $4 pt^{100}$.

Though you cannot see, the right edge of this over-painted c[0] region is shifted right by 4 pt to hide the small patch at the right bottom corner of the p region above by overlaying.

This s(panning text) region could be extended to both side edges of the paper if its extension were (10000pt,-4pt).

Little to say as well.

The author does not have much to say now for this column chunk.

Nothing to say as well.

Still nothing to say particular to the page break we will have shortly.

 99 This footnote is given outside **paracol** environment but its background is painted by light purple because it is merged with the footnote 100. 100 This (foot)n(ote) region could be extended to both side edges and the bottom edge of the paper if its extension were

(10000pt,-4pt)(10000pt,10000pt).

This figure is given in the paracol environment closed in the previous page but its background is not painted.

Figure 16: A Page-Wise Figure Exported to Post-Environment

This f(loat) region could be extended to both side edges and the top edge of the paper if its extension were (10000pt,10000pt)(10000pt,-4pt).

Figure 15: A Page-Wise Figure Imported from Pre-Environment

This paragraph is just for keeping the paracol environment	This paragraph is not necessary for
alive in this page.	keeping alive the environment but is given
	for consistent view.

Note that overlay painting is inevitable for two-toned page painting, as far as you want to paint background of page-wise stuff.

The last issue of background painting is about painting materials given outside **paracol**. As you have seen, pre-environment and post-environment stuff are painted but it is done only when they reside in a page having a portion of a **paracol** environment (maybe) of course. Therefore, the next page is *not* painted because the page does not have any parallel-columned stuff. Therefore, even if you wish to paint the whole of your document including pages without **paracol** stuff, you cannot do it just with **paracol** package, at least so far.

On the other hand, some materials given outside paracol environments are painted as if they are given in the environment when they are *imported* into the environment. One category has footnotes given in preenvironment stuff when $footnoteplacement{m}$ is specified for merging, as exemplified by the footnote 99 in the previous page. Note that such a footnote is painted by the color for n region rather than p region even when there are no footnotes in the paracol environment. The other category has ordinary floats given by figure and/or table (i.e., neither figure* nor table*) environments outside paracol and then *deferred* to a page having (a portion of) stuff produced by paracol. Since such a float, e.g., Figure 15 in this page, is considered as a page-wise float given in the paracol environment in this section, its background is painted by the color for the f region, rather than that for the p region which would be used if the float were is placed in the previous page. Note that such a deferred float import could occur not only from the page having $begin{paracol} but also from pages preceding it. For example, if you have three figure environments in a page <math>p-1$ just preceding the page p in which you start a paracol environment, it could happen that first one is placed in p-1 without painting, the second is placed in p and painted by the color for p, and the third is placed in p+1 and painted by the color for f.

Finally some materials *exported* from a paracol environment are painted as if they are in post-environment stuff. In previous two subsections, we saw merged footnotes (e.g., 93 in p. 51 and 96 in p. 55) are painted by the color of p rather than n. The other kind of exportation is of page-wise floats given in a paracol environment but deferred to the page next to the page having $end{paracol}$, or further. For example, Figure 16 is given in the paracol environment above in this page, but its background is not painted because the next page in which the figure is placed does not have any parallel-columned stuff¹⁰¹.

 $^{^{101}}$ If it has, the background is painted by the color for p.

(intentionally blanked page to show this page is not painted)

11 Known and Unknown Problems

Here a few problems you could face in the use of paracol are summarized.

- If your (e.g.,) left column goes ahead too much farther than the right column, LATEX could stop with the following error message.
 - ! Package paracol Error: Too many unprocessed columns/floats.

This usually means that the internal space to keep materials in the left column is exhausted. More specifically, suppose at some point in your .tex the left column is in the page p while the right is in q < p. We need (p-q) boxes to keep the left column contents in the pages $q, q+1, \ldots, p-1$ because these pages cannot be *printed* yet until the right column fills them. In addition, we also need two boxes for the left column in p and the right column in q so that you make column-switching between them keeping unprinted contents in them. Therefore, at least we need to have (p-q) + 2 boxes, while the number of them provided by LAT_{EX} is only 18^{102} . Therefore, paracol cannot continue its work if (p-q) reaches 17. Furthermore, other stuff also consumes the boxes as follows.

- If there are n pages in q, q + 1, ..., p having pre-environment stuff or page-wise floats, n boxes are consumed by them. Similarly, if m pages in them have page-wise footnotes, m boxes are given to them.
- If the left (resp. right) column has column-wise footnotes in p (resp. q), a box is used for them.
- If the left (resp. right) column has k floats to be placed in p (resp. q) or to be deferred to p+1 (resp. q+1) or a succeeding page, k boxes are reserved for them.

Therefore, it should be safe to keep (p-q) from exceeding 10 or so placing \switchcolumn in both columns fairly frequently.

- As discussed in Section 7.2, setting a synchronization point in a page brings the following side effects.
 - Stretch and shrink factors of all vertical skips in the page are nullified. The nullification of stretch factors could make a sparse column in the page have a vertical space at its bottom as if \raggedbottom setting is in effect even with \flushbottom one, rather than distributing the amount of the space to the skips so that the bottom line is aligned at the page bottom. As for the nullification of shrink factors, it makes the page have lines a little bit less than that it would have without synchronization because lines above the (last) synchronization point cannot be compressed. The other effect is a little bit subtle because the shrink factors below the last synchronization point are taken care of by TEX's page builder when it examine the appropriateness of each breakable point, but they are nullified when the page is printed. That is, if TEX finds a good break point which needs that the stuff between the synchronization and break points is compressed a little bit, the stuff is printed without compression making its bottom edge a little bit below the page bottom.
 - After a synchronization point is set, columns in the page cannot have top floats any more even if a column has space above the synchronization point and large enough to place the float. Therefore, if you like to exploit the space, you have to place the figure or table environment in question prior to the column-switching command or environment for the synchronization.
- As the author did for Section 1 to 5, sometimes you will make a section header spanning all columns by giving a sectioning command such as \section, \subsection and \subsubsection to the optional

¹⁰²Readers who are acquainted with LATEX implementation will understand that 18 is the cardinality of the set {bx@A, ..., bx@R} for floats acquired by **newinsert**. Those who are more familiar with that might know that most LATEX, based on e-TEX or others having similar extensions, now have 52 **\inserts** {bx@A, ..., bx@Z, bx@AA, ..., bx@ZZ} for floats and materials of paracol, since 2015

argument of \switchcolumn* or \begin of a synchronizing column-switching environment. These three commands work well and you will have what you intend to have, but you have to be careful with lower-level commands \paragraph and \subparagraph. Unlike higher-level relatives, these lower-level commands does *not* put the header *immediately* but keep it somewhere¹⁰³ so that when the paragraph following the command starts it is put as the leading part of the paragraph. Therefore if the spanning text has (e.g.) \paragraph only, the header is not put as a spanning text but at the head of the first paragraph of the column to which you switch, leaving an empty spanning text with some large space as follows.

 This left-column paragraph precedes a synchronized column-switching.
 This right-column paragraph precedes a synchronized column-switching.

 A Spanning Text Given by \paragraph This left-column paragraph follows the synchronization but is led by \paragraph given to the optional argument of \switchcolumn* for spanning text.
 This right-column paragraph follows the synchronization nized column-switching.

 Therefore, unless this is what you intend to do, you have to give some paragraph together with \paragraph following \paragraph because it produces (almost) nothing. By using this technique the example above becomes the followings.

This left-column paragraph precedes a synchronized column-switching.

This right-column paragraph precedes a synchronized column-switching.

A Spanning Text Given by \paragraph Followed by \mbox{}

This left-column paragraph follows the spanning This text above. text a

This right-column paragraph follows the spanning text above.

- As shown in Section 8, it is not easy to have good numbering and stacking order of page-wise footnotes even with the supports from \footnote* and its relatives. In addition, a footnote in a paracol environment cannot be broken into two (or more) pages.
- As the author confessed in Section 9.1, right parallel-pages cannot have page-wise stuff but have blank spaces in the corresponding region for them. The author will try to remove this limitation from a future version of paracol, in the version 1.4 hopefully.
- As discussed in Section 10.2, it is desirable that background painting region definition in **\backgroundcolor** has position dependent extensions. The author is fairly optimistic about the incorporation of this advanced feature in the version 1.4.
- In the release dated 2015/01/10, IATEX changed its mechanism of the placement of double-column floats (or in our terminology, page-wise floats) to avoid *out-of-order* appearance of them. That is, until the release on 2014/05/01 a double-column float (e.g., figure*) can be overtaken by a single-column float of the same category (e.g., figure) when they cannot be put into the page in which texts around them are put. In order to cope with the problem, the new version merged two lists to keep *deferred* double- and single-column floats into one so that the appearance order of them is determined by their order in the single list. Though this change should have made people happy when they typeset *ordinary* two-column (or multiple-column) documents, the new feature might not be welcomed by paracol users because your

 $^{^{103}}$ For people familiar to T_EX's *dangerous bends*, the header is kept in \everypar.

parallel-columns have their own *streams* of floats to be put in the corresponding columns. Therefore, and for the sake of simplicity of paracol's implementation, the author decided to nullify this new feature in paracol environments. That is, even with new releases of LATEX, your page-wise floats given in a paracol environment can be overtaken by column-wise floats.

In addition to the problems above known to the author, there may be (or should be, honestly speaking) other unknown problems in **paracol** because it cannot be perfect though the author has made his best effort for testing and debugging it. Particularly, sometimes it is very tough, if not impossible, to make **paracol** compatible with other packages, especially with those having dark magic as **paracol** has in it¹⁰⁴. Therefore, though reporting incompatibleness with a package you use is very welcome¹⁰⁵, you should kindly understand the toughness of the compatibility issue.

Furthermore, even without such problematic packages, paracol might produce weird results due to its bug. If your document has something to make unknown bugs visible, you might have one (or more) of the followings which the author encountered in his debugging work.

- A page, a column, a footnote and/or a float disappears¹⁰⁶.
- A page, a column, a footnote and/or a float is duplicated.
- A message like "Overfull \vbox (1.23456pt too high) has occurred while \ouptut is active" is shown.
- A message "Underfull \vbox (badness 10000) has occurred while \ouptut is active" is shown. This message, however, does not always mean a bug but may just be a complaint that a column or a page is too sparse to meet your request to align the bottom of all columns and pages by \flushbottom setting. Therefore, if you have this message and you cannot be sure whether it means a bug or not, try \raggedbottom setting to see if you still have the message, before sending a bug report to the author.

If you encounter anything like them (or whatever you cannot solve by yourself), don't hesitate to report it to the author with minimum source file to produce the problem¹⁰⁷.

 $^{^{104}}$ For example, the author knows it is almost impossible to make paracol compatible with one of the author's own package available in CTAN.

 $^{^{105}}$ For example, paracol is now compatible with color package thanks to a report from a user.

¹⁰⁶In fact, a bug fixed in version 1.2 caused page losing though it happens very very rarely but an unlucky user encountered it.

¹⁰⁷And with patience because your problem might not be solved quickly.

PART II Implementation

1 Overview

1.1 Column-Pages

In our parallel multi-column typesetting, a column may grow independently of other columns and may cross its page boundary asynchronously with others. Therefore, we cannot throw away the contents of a column in a page, or a *column-page* in short, when a page break occurs in the column. Instead, we have to keep column-pages until all columns are *synchronized* implicitly or explicitly.

An *implicit synchronization* takes place when all columns in a page see page-breaks to let the page is shipped out. In general, all columns but the last one which arrives the page-break have completed column-pages in the page in question and some of them may have succeeding column-pages. Therefore, we maintain the list of completed column-pages $S_c = \text{pcol@shipped} \cdot c$ for each column $c \in [0, C)$, where C = pcol@ncol is the number of columns given through the argument of paracol environment, and the set of them $S = \{S_c | c \in [0, C)\}$.

Each element $s_c(p)$ of a list S_c is an **\insert** whose **\vbox** contains the *p*-th completed column-page¹⁰⁸, where p = 0 for the first column-page produced in **paracol** environment or that following a page flushing macro **\flushpage**, **\clearpage** or **\cleardoublepage**. That is, S_c is defined as follows, where $p_b = \text{\pcol@basepage}$ is the zero-origin ordinal of the *base page* being the oldest page not shipped out yet.

$$S_c = (s_c(p_b), s_c(p_b+1), \dots, s_c(p_b+k-1))$$

= \@elt s_c(p_b) \@elt s_c(p_b+1) \... \@elt s_c(p_b+k-1)

Note that a list S_c can be empty and all members in S may be empty.

The other type of synchronization, explicit synchronization, takes place by \switchcolumn* or the beginning of starred column-switching environments, by \end{paracol}, or by one of page flushing macros \flushpage, \clearpage and \cleardoublepage. A flushing explicit synchronization ships out the pages from p_b to $p_t = \pool@toppage$ being the ordinal of the top page to which the most advanced leading column has reached. On the other hand, other non-flushing explicit synchronization keeps the page p_t from being shipped out because the column-pages in it or the page itself will grow further.

1.2 Current Column-Pages and Their Contexts

We also have to maintain another type of column-pages which are currently built, or *current* column-pages in short, to switch from a column to another. Since each column may have its own context for the typesetting of it, or column-context in short, it were perfect to save the context when we leave from a column and to restore that when we revisit the column if we could. However, T_EX and L^AT_EX has a tremendously large number of context variables and the number becomes virtually boundless when we take variables defined in various styles and by users themselves into account. Therefore, we had to abandon to keep the whole context of the column but carefully chose a small subset comprising variables automatically modified outside

 $^{^{108}\}mathrm{Other}$ registers such as **\count** are not used.

- β represents $\ insert \cdot \beta$ containing the followings.
 - $-\beta^b = \log \beta = \log \beta$ is the vbox containing the main vertical list which has already contributed to the current column-page.
 - $\beta^p = \text{count} \cdot \beta = \text{pcol@page}$ means the current column-page belongs to the page β^p .
 - $-\beta^r = \dim \beta = \Im$ is the room of the column.
- $\tau = \text{pcol@currfoot}$ is the \insert containing the footnotes added in the current column-page, if column-wise footnote typesetting is in effect. Its constituent \box, \count, \dimen and \skip are denoted as τ^b , τ^c , τ^d and τ^s respectively. On the other hand, if page-wise footnote typesetting is in effect, τ is always empty¹⁰⁹.
- $\delta =$ bcol@prevdepth is the depth of the last vertical item in β^b obtained by prevdepth.
- $\lambda_t =$ \@toplist is the list of top floats inserted in the current column-page.
- $\lambda_m =$ (**Cmidlist** is the list of mid floats inserted in the current column-page.
- $\lambda_b =$ \@botlist is the list of bottom floats inserted in the current column-page.
- $\lambda_d =$ \@deferlist is the list of column-wise floats deferred to the next column-page.
- $\xi =$ bcol@textfloatsep is the vertical skip used instead of \textfloatsep for top floats in the current column-page if it has synchronization points, or ∞ otherwise.
- $\eta =$ **Otextfloatsheight** is the total height of mid floats and their separators in the current column-page.
- $\nu_t =$ \@topnum is the maximum number of top floats which the current column-page can accommodate further.
- $\rho_t = \langle \texttt{Ctoproom} \text{ is the room for top floats in the current column-page.}$
- $\nu_b = \$ botnum is the maximum number of bottom floats which the current column-page can accommodate further.
- $\rho_b = \$ botroom is the room for bottom floats in the current column-page.
- $\nu_c = \colnum$ is the maximum total number of floats which the current column-page can accommodate further.
- σ is the following encoding of \if@nobreak and \if@afterindent at the time we left from the column c.

$$\sigma = \begin{cases} 0 & \texttt{ifQnobreak} = false \\ 1 & \texttt{ifQnobreak} = true \land \texttt{ifQafterindent} = true \\ 2 & \texttt{ifQnobreak} = true \land \texttt{ifQafterindent} = false \end{cases}$$

Note that we have only three states because if@afterindent is meaningful only when $if@nobreak = true^{110}$.

¹⁰⁹But the macro \pcol@currfoot is used to keep page-wise footnotes temporarily.

 $^{^{110}\}mathrm{If}$ only with the standard IATEX and so far.

• $\varepsilon = \langle everypar$ is the tokens stored in $\langle everypar$ at the time we left from the column c.

In addition, we have special context variables $w_c = \col@columnwidth c$ in which we keep \columnwidth for the column c.

Note that we could add other variables to the saved context and/or provide some API macro to define them by users, but abandon them because it should be too complicated for users¹¹¹. Also note that we provide a save/restore mechanism for local counters as discussed in §1.4.

1.3 Pages and Their Contexts

Besides the column-pages, we have to keep track each whole page not yet shipped out but has some complete or incomplete (i.e., current) column-pages. We maintain the list;

$$\begin{split} \Pi &= \texttt{lpcol@pages} = (\pi(p_b), \pi(p_b+1), \dots \pi(p_t-1)) \\ &= \texttt{l@elt} \pi(p_b) \texttt{l@elt} \pi(p_b+1) \cdots \texttt{l@elt} \pi(p_t-1) \\ \pi(p) &= \{\pi^p(p)\}\pi^i(p)\pi^f(p)\{\pi^s(p)\}\{\pi^m(p)\} \end{split}$$

where $\pi(p)$ is the page context of p and its elements $\pi^p(p)$, $\pi^i(p)$, $\pi^f(p)$, $\pi^s(p)$ and $\pi^m(p)$ have the followings.

- $\pi^p(p) = page(p)$ is the value of the counter page (i.e. \c@page) for the page p.
- Iff $\pi^i(p) \neq \bot$, the page p has page-wise floats or the single-column pre-environment stuff preceding \begin{paracol} in the starting page where it resides and spanning all columns. In this case $\pi^i(p) = i$ represents \insert $\cdot i$, often cached in the macro \pcol@ spanning, for such spanning stuff whose registers have the followings.
 - $-\pi^{b}(p) =$ \box $\cdot i$ contains the spanning stuff.
 - $-\pi^{h}(p) = \dim i = \operatorname{Qcolht} if positive for the height of columns shrunk by the spanning stuff. If negative, the page is only for the spanning stuff, i.e. a$ *float page* $. We use the notation <math>\pi^{h}(p)$ for the pages $\pi^{i}(p) = \bot$ to mean \textheight.
 - $-\pi^t(p) = \stip \cdot i = \pcol@topskip being the value of \topskip at \begin{paracol} paracol be inserted at the top of each column in each non-first page. Otherwise, i.e., for the columns in the starting page following the pre-environment stuff, it has 0 to prevent the \topskip insertion. We use the notation <math>\pi^t(p)$ for the pages $\pi^i(p) = \bot$ to mean \pcol@topskip.
- Iff $\pi^f(p) \neq \bot$, page-wise footnote typesetting, discussed in §1.5, is in effect and the page p has some footnotes in $box \cdot \pi^f(p)$. This element is often *cached* in the macro pcol@footins.
- $\pi^s(p) = (span(H_1, h_1), \ldots, span(H_n, h_n)) = \ensuremath{\basel{eq:hamiltonian}} \ensuremath{\basel{eq:hamiltonian}} \ensuremath{\basel{hamiltonian}} \ensurema$

¹¹¹And for the author if we include save/restore of macros, though it could be done with a \toks containing the definitions of macros.

• $\pi^m(p) = \{M_L^l\}\{M_L^r\}\{M_R^l\}\{M_R^r\}$ is the set of lists of marginal notes in the left (l) and right (r) margins and in the left (L) and right (R) parallel-pages. The words left and right of margins mean physical left and right, while left and right of parallel-pages mean the logical ones, i.e., the page where the column-0 resides is left. Each element $M_{\{L,R\}}^{\{l,r\}}$ has a list $(mpar(t_1, b_1), \dots, mpar(t_n, b_n)) = \ensuremath{\columnwidth{\mathbb{C}}} \$ of marginal notes whose top and bottom are at t_i and b_i from the top of the column area, where t_i and b_i are represented in the form of integers. Each element can be empty of course, and $\pi^m(p)$ itself can be so as well to mean all elements are empty¹¹². Therefore, $\pi^m(p)$ is emptied by \pcol@startpage, and then examined and modified by \pcol@addmarginpar when it adds a marginal note through macros \pcol@getmparbottom and \pcol@setmpbelt. Another modifier \pcol@output@start initializes one of the element $M_L^{\{l,r\}}$ with the value representing the last marginal note in pre-environment stuff, while another examiner $\collocate{pcollocat$ element, according to LATEX's setting of marginal note placement. The whole element $\pi^m(p)$ is often *cached* in the macro \pcol@mparbottom. The usage of this element is discussed in $\S1.7$ a little bit more detailedly.

Note that even in parallel-paging and in non-paired one in particular, a page p consists of all columns $c \in [0, C)$. Therefore, the term *left/right parallel-page* p always mean the left and right component of a parallel-page (pair) p.

The reason why we keep track of page(p) is that page numbering is not necessary to be consecutive. If such a *jump* occurs randomly in any columns explicitly updating **page**, it is very tough to give a consistent view of the page number of a specific page to all columns. Therefore we suppose jumps occur only in the leftmost column 0^{113} which controls the page numbering, while non-leftmost columns are expected to refer the **page** passively.

This page numbering is implemented as follows. Each time a column-page at p of the leftmost column is completed to start a new column-page, page(p) is fixed to be the value of page and $page(q) = \pi^p(q)$ for all $q \in [p, p_t]$ are let be page(p) + (q - p) in usual cases but page(p) + 2(q - p) in non-paired parallel-paging. This update also takes place on column-switching from the leftmost column-page at p to another column so that a jump happening before the switching is notified to other columns. On the other hand, starting or column-switching to a non-leftmost column-page at p lets page have page(p) referring to $\pi(p)$, unless the column starts the most advanced top page. In this new top page case, $\pi(p_t+1)$ is added to Π with the temporary setting $\pi^p(p_t+1) = page(p_t+1) = page(p_t) + 1$ usually but $\pi^p(p_t+1) = page(p_t + 1) = page(p_t) + 2$ in non-paired parallel-paging, and p_t is incremented.

Note that this management is imperfect because direct references of page in non-leftmost columns can give inconsistent results if page is modified in a non-leftmost column or the reference occurs in a page p after that the leftmost column modifies page in a page q such that $q \leq p$. In addition to them, this mechanism in non-paired parallel-paging always gives incorrect page number to the columns in a right parallel-page because $\pi^p(p)$ always has page(p) for the left parallel-page. However, it is expected that the progress of the leftmost column usually precedes other columns to give consistent page reference even with jumps, unless the reference is made by a column in a right non-paired parallel-page. More importantly, it is assured that indirect references through .aux records and page numbers recorded in .toc, .idx, and so on are always consistent because of the lazy evaluation of page = page(p) at ship-out of an ordinary page p or a left parallel-page p, while the counter is let have page(p) + 1 when a right

 $^{^{-112}}$ To minimize the possibility of miscoding for emptying and save a small amount of memory for pages having no marginal notes.

 $^{^{113}}$ But we neither inhibit nor nullify a jump in non-leftmost column and thus the update can be seen referring to page counter explicitly.

non-paired parallel-page p is shipped out.

Also note that we also keep $\pi(p_t)$ in \pcol@currpage which is initialized by \pcol@output@ start to let $\pi^i(p_t)$ have the pre-environment stuff. Then the macro is redefined to have the value representing the new page possibly with $\pi^i(p_t)$ for page-wise floats in \pcol@startpage by the macro \pcol@defcurrpage. Another \definition is done in \pcol@output@switch also with \pcol@defcurrpage to let $\pi^f(p_t)$ have page-wise floats built in \footins if page-wise typesetting is in effect and the column-switching leaves the column in p_t^{114} . We denote the concatenation of Π and $\pi(p_t)$ as Π^+ to represent all pages on-the-fly.

1.4 Counters

Besides the context variables discussed in §1.2, we need to make counters local to each column except for those declared to be global by \globalcounter. Let Θ be the set (list) of all counters declared before \begin{paracol}, i.e., $\Theta = \cl@ckpt$, and

$$\Theta^g = \texttt{Pcol@gcounters} = \{\theta^g_1, \ldots\} = \texttt{Qelt}\{\theta^g_1\} \cdots$$

be the set of global counters which have declared so by $\globalcounter{\theta_i^g}$. Then the set of local counters Θ^l is defined as follows.

$$\Theta^l = \Theta - \Theta^g = \texttt{pcol@counters} = \{\theta_1^l, \ldots\} = \texttt{Qelt}\{\theta_1^l\} \cdots$$

Since each column has its own values in local counters, we have to keep the set of counter/value pairs

$$\Theta_c = \texttt{lpcol@counters} \cdot c = \{ \langle \theta_1^l, val_c(\theta_1^l) \rangle, \ldots \} = \texttt{lgelt}\{\theta_1^l\}\{val_c(\theta_1^l)\} \cdots$$

for each column c, where $val_c(\theta_i^l)$ is the value of a counter θ_i^l local to c. That is, whenever we switch from a column c to d, we save $\langle \theta_i^l, val_c(\theta_i^l) \rangle$ in Θ_c and restore θ_i^l for d by letting it have $val_d(\theta_i^l)$ in Θ_d , for all $\theta_i^l \in \Theta^l$.

A global counter is free from these save/restore operations but needs another special operation when it is incremented by \stepcounter. That is, the invocation of \stepcounter for a global counter θ_i^g may clear local counters in its set of descendant counters $\zeta(\theta_i^g) =$ \pcol@cl@ θ_i^g and this clearing must be performed on the all instances of $\theta_j^l \in \zeta(\theta_i^g)$ saved in Θ_c for all $c \in [0, C)$. Therefore, on the \stepcounter, we do the followings for all $c \in [0, C)$; temporarily restore all $\theta_k^l \in \Theta^l$ from Θ_c ; clear all $\theta_j^l \in \zeta(\theta_i^g)$; and then save $\langle \theta_k^l, val_c(\theta_k^l) \rangle$ back to Θ_c .

The other item we maintain for a local counter θ^l is its *local representation* $\langle rep \rangle$ in a column c defined by \definethecounter $\langle \theta^l \rangle \langle c \rangle \langle rep \rangle$. The local representation $\langle rep \rangle$ is kept in \pcol@thectr@ $\theta^l \cdot c$ and is made \let-equal to \the θ^l when the column c is visited.

1.5 Page-Wise and Merged Footnotes

Page-wise footnote typesetting is completely different from ordinary *column-wise footnote* typesetting.

When a column-page in the top page is built, \footins keeps all footnotes \inserted by \footnote or \footnotetext in any columns in the page. Therefore, \footnote and \footnotetext in the top page act as usual to add the footnote to \footins. Then if a column-switching takes place to leave the column, \footins is saved into $\pi^f(p_t)$ by \pcol@

¹¹⁴The \definition of \pcol@currpage in \pcol@setpnoelt, and emptying it in \pcol@output@start and \pcol@freshpage are for coding trick and thus not for giving a really new \definitions.

output@switch, so that $\pi^f(p_t)$ is \inserted to \footins again by \pcol@restartcolumn when it visits a column in p_t , or by \pcol@startcolumn when it finds a column proceeds to p_t .

Then, when a column-page in the top page completes advancing p_t , \footins is kept in $\pi^f(p_t-1)$ by \pcol@startpage, rather than being combined with the column-page. This saving into $\pi^f(p_t-1)$ fixes the footnotes in p_t-1 so that $\pi^f(p_t-1)$ is combined with other materials in the page by \pcol@outputelt or \pcol@makeflushedpage through \pcol@putfootins when the page is shipped out.

Fixing $\pi^f(p)$ for $p < p_t$ makes it impossible to add footnotes in a column in the page p not only to $\pi^f(p)$ but also to **\footins** for the page p because we have at least one fixed column-page $s_c(p)$ unable to shrink to have such additional footnotes in p^{115} . Therefore, such a footnote addition is *deferred* and is thrown into $\pi^f(p_t)$ through a list;

 $\Phi = \texttt{Vpcol@topfnotes} = (f_1, f_2, \dots, f_n) = \texttt{Vbox} \{f_1 \ f_2 \ \cdots \ f_n\}$

where f_i is a **\vbox** containing the deferred footnote preceded by **\penalty\interlinepenalty** to allow TEX to break footnotes to place them in two (or more) pages. That is, **\footnote** or **\footnotetext** in $p < p_t$ adds an element for the footnote to Φ , then all the elements¹¹⁶ are **\inserted** to **\footins** by **\pcol@deferredfootins** invoked in **\pcol@restartcolumn** when it visits a column in p_t , or in **\pcol@startcolumn** when it starts a column-page in p_t . The macro **\pcol@output@end** also do the **\insertion** by itself with merged footnote typesetting to let deferred footnotes be a part of post-environment stuff.

The reference to $\pi^f(p)$ for $p < p_t$ is also made in \pcol@restartcolumn and \pcol@ flushcolumn. The former \inserts $\pi^f(p)$ to \footins so that the column-page which the macro restarts is built as if it has the footnotes in $\pi^f(p)$ to make the column-page broken leaving the space for the footnotes. However, \footins is never grown because it has been fixed and thus additional footnotes will go to Φ as discussed above. Then \footins is discarded by \pcol@makecol when the column-page completes, or by \pcol@output@switch when it leaves the column.

The reference to $\pi^f(p)$ by the latter macro \polloflushcolumn is to build the ship-out image of the column-page to be flushed. When this macro and other macros, namely $\pollomakecol and \pollomakeflushedpage$, build the ship-out image in a page p having $\pi^f(p)$ using $\mbox{Qmakecol}$, we have to be careful of the fact that the column-page has been build as if it has footnotes in $\pi^f(p)$ but the footnotes are not included in its ship-out image but that of the page. Therefore, \colht referred in $\mbox{Qmakecol}$ should be shrunk by the sum of height and depth of $\pi^f(p)$ and $\skip \cdot \pi^f(p)$ by \polloshrinkcolbyfn . Other and more subtle adjustment is to add the stretch and shrink factors of $\skip \cdot \pi^f(p)$ at the tail of the column-page by \polloue unvboxQcclv. This is necessary because TEX has broken the column-page taking account of the stretch and, more essentially, shrink factors, and thus without the factors the main vertical list in the column-page could be a little bit taller than \colht causing overfull.

The feature gathering footnotes in all columns in a page brings a problem to explicit synchronization, because a column whose contents fit the top page at the last visit may be too tall on the synchronization because other columns have put some footnotes after the last visit. That is, we cannot simply build the top page combining $s_c(p_t)$ for all $c \in [0, C)$ and $\pi^f(p_t)$ because there could be $s_c(p_t)$ too tall to reside in p_t with $\pi^f(p_t)$.

To solve this problem, we perform the following operations prior to fix the contents of p_t having an explicit synchronization point in it. First one is *column-scan* to visit all columns by column-switching prior to the synchronization so that T_FX's page builder has opportunities

¹¹⁵The column-page $s_c(p)$ could have some space at its bottom produced by, for example, \newpage, but exploitation of such space is extremely hard.

 $^{^{116}}$ More accurately, some trailing elements may be left in Φ if its total height is too large, as discussed in §11.5.

to break too tall column-pages. Since this scan could merely break footnotes rather than the main vertical lists in the column-pages and the broken footnotes will be reconnected when the **\output**-routine is invoked for the synchronization, we then examine if all $s_c(p_t)$ are accommodated in p_t with $\pi^f(p)$.

This examination for a synchronization by switchcolumn* or its relatives is done as a part of the inherent synchronizing procedure to see if the combination of the tallest *top* items, i.e., top floats and the main vertical list, and the tallest *bottom* items, i.e., bottom floats and columnwise footnotes, is too large causing page flushing. As for page flushing and environment closing, this *pre-flushing column height check* requires a special kind of synchronized column-switching by which we flush pages up to $p_t - 1$ and examine if there is a too tall column.

Then if too tall columns are found, in either cases, we move to the *tallest* column to force a page break in the column so that we have a new page with shorter columns and shorter pagewise footnotes as well. In the synchronization by \switchcolumn* or its relatives, this forced page break is then applied to all other columns so that new column-pages have top floats, if any, below which we should place the synchronization point. This examination and forced page break is repeated until we have a page without any too tall columns, because a page break may bring deferred floats and footnotes which may result in a too tall column.

1.6 Text Coloring

1.6.1 Fundamental Mechanism

Text coloring done by color package and its relatives using special stands on the fact that the main vertical list is *printed* in the order of occurrence in the source .tex. That is, a command such as $color{red}$ puts $special{color push [1 0 0]}^{117}$ into .dvi to make all stuff in the main vertical list colored red until other coloring special inserted by other coloring macro appears in .dvi. This simple mechanism works well even when the pair of coloring specials are in different pages and/or columns because, with respect to the main vertical list, everything between them in .tex is also surrounded by the special pair in .dvi. As for other stuff such as header, footer, floats and footnotes, IAT_EX surrounds them by color@begingroup and color@endgroup or other similar constructs so that they are colored without interference with the coloring of the main vertical list.

In paracol environment, however, the orders of the main vertical list in .tex and .dvi are not always same. When a column encounters a page break, in .dvi the other column should intervene between the stuff in the broken pair of column-pages possibly changing the color of the second column-page. A column-switching from c_1 to c_2 also makes the main vertical list out-of-order to cause another unexpected coloring because a coloring command in c_2 will have no effect when c_1 is revisited after that following its pre-switching stuff in .dvi which was put before the coloring. Therefore, we have to make *color contexts* in both .tex and .dvi coherent inserting appropriate \specials into .dvi whenever an out-of-order *jump* occurs in .dvi by a page break or in .tex by a column-switching.

The color package and its relatives¹¹⁸ assume that *printers* have a stack for coloring and thus a coloring \special pushes the new color into the stack while it is popped by another \special which will be inserted by \aftergroup mechanism when a group surrounding the coloring \special is closed. Therefore we have to keep track of the color context with *color* stack

$$\Gamma = (\gamma_1, \gamma_1, \dots, \gamma_n) = \bigvee \max\{\gamma_1 \ \gamma_2 \ \dots \ \gamma_n\}$$

 $^{^{117}}$ If .dvi is processed by dvips, or other printer-dependent command corresponding to it.

¹¹⁸And all other coloring mechanism compliant with $IAT_{E}X 2_{\varepsilon}$, hopefully and believingly.

where γ_i is a **\vbox** of 1 sp tall, 0 deep and 0 wide containing a coloring **\special** which **\set@color** puts into the main vertical list. That is, when **\set@color** is invoked we push γ to the tail of Γ , while when the corresponding **\reset@color** appears we pop it from Γ . Then when we encounter an out-of-order jump, at first we rewind the color stack in .dvi by putting **\specials** which **\reset@color** for it is invoked for all $\gamma_i \in \Gamma$. Therefore from the viewpoint of a *printer*, it will see stack-rewinding at the end of each column-page and the leaving points of column-switching, while the beginning of each column-page and the entry points of column-switching should have the sequence of coloring **\specials** to regain the color stack which the *printer* must have at each of the points.

In addition, for each column c we keep $\gamma_0^c = \col@columncolor@box c$ as the *default* color of the column c, optionally given by the API macro \columncolor or \normalcolumncolor. If given for c, it is assumed to be at the bottom of the color stack denoted by $\Gamma^c = (\gamma_0^c, \gamma_1, \ldots, \gamma_n)$ which we rewind/reestablish at each out-of-order jump in the column c.

1.6.2 Coloring in Horizontal Mode

We have to pay attention to the fact a coloring command can appear in horizontal mode of course, and thus push/pop operations in a column-page would be done *before* the column-page starts when set@color or reset@color is in the second half of a page-crossing paragraph and if we immediately performed push/pop of the color stack in these macros. In addition, even in vertical mode these macros can appear before T_EX finds a page break after which they must be in effect, if they are preceded by a sequence of non-breakable vertical items by which T_EX 's examination of the page break is *delayed* as well as the invocation of output at the break.

In order to solve the problem of push/pop timing, we perform push/pop operations through \insert to our own register set \pcol@colorins. That is, we \insert γ to \pcol@ colorins when we encounter a \set@color for γ , while its corresponding \reset@color also \inserts another \vbox γ^- of null-height/depth/width having a \special which the \reset@color puts into the main vertical list. Since we let \count\pcol@colorins = 0 and \skip\pcol@colorins = 0 to keep the \insertion from affecting the growth of \pagetotal, it is guaranteed that an inserted γ or γ^- is given to \output through \pcol@colorins together with \box255 containing the corresponding \special.

When **\output** is invoked, **\pcol@colorins** has Γ_r containing γ_i and possibly its corresponding γ_i^- . Therefore, if **\output** is for a page break or a column-switching, we remove all pairs of γ_i and γ_i^- from **\pcol@colorins** to let it have Γ only with γ_j whose corresponding γ_j^- is not in Γ_r . For this removal, we scan Γ_r from its tail incrementing/decrementing a counter n_{pop} which we initialize to 0 before scanning. In the scan, we remove all γ^- unconditionally incrementing n_{pop} , and γ such that $n_{\text{pop}} > 0$ on the encounter with it decrementing n_{pop} . This scan is done by **\pcol@clearcolorstack**, invoked from **\pcol@col@clearcst@unvbox**, and is for rewinding the color stack (γ_0^c, Γ_r) = Γ_r^c . Therefore, for each γ to be kept because of $n_{\text{pop}} = 0$ on the encounter with it we put **\special** for **\reset@color**. Note that on another scan for stack reestablishment, **\pcol@colorins** has Γ and is kept unchanged. Also note that other **\output** invocations such as that for floats do not touch Γ_r to allow it grows with γ and γ^- corresponding to **\set@color** and **\reset@color** in the column-page in which the invocation happens¹¹⁹.

The mechanism above especially for horizontal mode has subtle issues as follows.

 $^{^{119}}$ Unlike \footins which becomes void by putting its contents back to the main vertical list to reexamine the footnote placement possibly with splitting.

- If \set@color appears in a \vbox, the \insertion for pushing is not effective but corresponding \reset@color can be outside of the \vbox to make pushes and pops unbalanced because \aftergroup for it inserts it just after the closing of the \vbox if \set@color is not surrounded by an inner group.
- If we are in vertical mode, we can know if we are in a \vbox by \ifinner. However, in horizontal or math mode, \ifinner cannot help us because it is true iff we are in a \hbox or in an in-text math. In short, T_EX does not provide us with any convenient means to know if we are in a \vbox.

To solve the problem above, we introduced a trick with \everyvbox to turn a switch \ifpcol@inner = true at the beginning of every \vbox in a paracol environment, by which we suppress the \insertion for \set@color because a \vbox cannot cross a page boundary. As for that of \reset@color, we suppress it by not reserving our own macro \pcol@reset@ color@pop for the \insertion by \aftergroup. That is, we reserve both \reset@color and \pcol@reset@color@pop with \aftergroup if we are outside of any \vboxes, while does the former only otherwise. By the same reason, we suppress the \insertion if we are in restricted horizontal mode, i.e., if both \iffmode and \iffinner are true. On the other hand, we cannot suppress the \insertion when we are in an in-text math because it can cross a page boundary¹²⁰. Note that the detailed implementation shown in §12 does not interfere the use of \everyvbox inside/outside of paracol environments or is not affected by the use.

Another attention we should pay is that \color will leave \aftergroup tokens of \reset@ color and thus they are invoked just after \end{paracol}. However, since we have completed all column-pages in the last page, the color stack in .dvi should be empty. Therefore to avoid stack underflow, we should reestablish Γ (not Γ^c) so that elements in the stack are popped by \reset@color invoked with the \aftergroup mechanism. We also take care of our own color stack popper \pcol@reset@color@pop which must do nothing, i.e., must not make an \insertion, after we completed the last page, i.e., if \ifpcol@output is false.

1.6.3 Changing Default Column Color

The implementation of \columncolor and \normalcolumncolor is relatively easy for the cases that they appear outside paracol environment or they define the default color of a column different from the current column. That is, for the default color of a column c we simply \define $\hat{\gamma}_0^c = \text{pcol@columncolor} \cdot c$ to let it have what \current@color has for the color. Then, in \begin{paracol} in the former case or immediately in the latter, we let $\gamma_0^c = \text{pcol@columncolor@box} \cdot c$ have the coloring \special for the color acquiring an \insert from \@freelist if the box is \bot .

On the other hand, when the API commands are to define the default color of the current column c, we need to place the coloring at the bottom of color stacks in terms of .tex and .dvi. That is, for the former we have to rewind and reestablish the stack which can be different from Γ^c because the API command can follow a page break which T_EX does not yet find. Therefore, we maintain a *shadow* of Γ namely;

$$\hat{\varGamma} = \texttt{Pcol@colorstack@shadow} = (\hat{\gamma}_1, \hat{\gamma}_2, \dots, \hat{\gamma}_n) = \texttt{Qelt}\{\hat{\gamma}_1\} \texttt{Qelt}\{\hat{\gamma}_2\} \cdots \texttt{Qelt}\{\hat{\gamma}_n\}$$

to which our version of $set@color</code> pushes <math>\hat{\gamma}_i$ being current@color</code> which the original one defines, while popping is done automatically by TFX's grouping mechanism because pushes are

 $^{^{120}}$ If an in-text math is in a **\hbox**, **\insert**ion is not necessary because the math cannot cross a page boundary. Though we can detect it by a trick with **\everyhbox**, we abandon this idea because the request is not harmful. Another and more serious issue of coloring in math mode will be discussed shortly.
done by \edef rather than \xdef. Then before we \define $\hat{\gamma}_0^c$ we rewind $\hat{\Gamma}^c = (\hat{\gamma}_0^c, \hat{\gamma}_1, \dots, \hat{\gamma}_n)$ putting \special for pop to the main vertical list for each elements, and then after the \definition of $\hat{\gamma}_0^c$ we reestablish $\hat{\Gamma}^c$ putting coloring \special for each element.

1.6.4 Coloring in Math Mode

Unfortunately the solution above is imperfect because T_EX builds an implicit hbox for a {math stuff} construct in math mode and an insert in the construct does not contribute to the main vertical list at all¹²¹. Since the implicit hbox does not care about everyhbox, we cannot use the trick similar to that with everyvbox. Another bad news is that built-in ifs for mode checking cannot help us because we always have ifwmode = false and ifmmode = true while ifinner is true or false when we are in in-text or displayed math mode respectively. Therefore, we have to take care of the potential loss of insertion for pushes and thus unmatched pops in Γ_r .

For example, we have to remember that, in the cases like $\{ color{c} text \}$ or $\{c\} text \}$ expanded to the former, the \insertion for push is lost while its counterpart for pop survives making it necessary to check the existence of pushing counterpart for each pop in Γ_r^{122} . Note that the fact that the pop in the examples is in the in-text math does not help us, because the pop in $\{c\}$ text \endgroup \color{c} text \endgroup \sigma is also in the in-text math while its pushing counterpart performs an effective \insertion, and two \insertions must be presented in Γ_r because we can have a page-break in text. Therefore, we have to find a means to examine whether a pop γ_i^- has its counterpart γ_i in Γ_r to remove γ_i from Γ_r if exists or to ignore γ_i^- otherwise. That is, we have to attach an identifier m to γ_i and γ_i^- , i.e., to make them $\gamma_{i,m}$ and $\gamma_{i,m}^-$.

Since the only means we have for the communication with **\output** routine is what we **\insert** to Γ_r , the **\insert** d **\vbox** must carry an identifier m for a push/pop in math mode. To do that, we make **\vbox** m sp wide (m > 0) if our version of **\set@color** is in math mode to represent $\gamma_{i,m}$ and $\gamma_{i,m}^-$, while the width is 0 otherwise as described in §1.6.2. Then in the scan of Γ_r for rewinding in **\output**, we suppress incrementing/decrementing n_{pop} for $\gamma_{i,m}$ and $\gamma_{i,m}^-$, but remove $\gamma_{i,m}$ if $\gamma_{i,m}^-$ is in Γ_r as a successor while we keep it in Γ_r otherwise putting a **\special** of pop for it to the main vertical list.

To ensure that $\gamma_{i,m}$ has its counterpart $\gamma_{i,m}^-$ in Γ_r iff the push and pop are in a column-page, we maintain the counter \pcol@mcid incremented before (the attempt of) the \insertion of $\gamma_{i,m}$ with $m = \pcol@mcid$ and the \aftergroup reservation for that of $\gamma_{i,m}^-$. Then the counter is zero-cleared by \output routine in order to keep it less than \pcol@mcpushlimit = 1000 unless, roughly speaking, a column-page has a unexpectedly large number of math constructs having coloring commands in them. Note that this zero-clearing does not ensure that an identifier m is unique in Γ_r . That is, it can happen that Γ_r has $\gamma_{i,m}$, $\gamma_{i,m}^-$, $\gamma_{j,m}$ and/or $\gamma_{j,m}^$ in this order for i < j, when two math constructs with coloring for i and j are in different

 $^{^{121}}$ The contents is not thrown away but **\insert**ion itself is added to the list rather than given to **\output**.

 $^{^{122}}$ Since a pop is always in a group one level outer from its push counterpart, the pop request should be presented if the push does.

paragraphs and \bigcirc is invoked at or after the end of the paragraph with the math for *i*. This potential duplication is, however, unharmful because of the following.

- Since a math construct cannot have immediate **\output** invocations in it, the order of the elements in Γ_r must be $\gamma_{i,m}$, $\gamma_{i,m}^-$, $\gamma_{j,m}$ and $\gamma_{j,m}^-$ from its bottom to top, though some of them could be missing. Therefore, if $\gamma_{i,m}^-$ is in Γ_r , then $\gamma_{j,m}$ must follow it if it exists not causing accidental matching with $\gamma_{i,m}^-$.
- If $\gamma_{i,m}$ is in Γ_r but $\gamma_{i,m}^-$ is not, it means we have a page break between vertical items corresponding to $\gamma_{i,m}$ and $\gamma_{i,m}^-$ to keep the **\insert**ion of $\gamma_{i,m}^-$ and anything following it from appended into Γ_r . Therefore, Γ_r cannot have $\gamma_{j,m}^-$ not causing accidental matching with $\gamma_{i,m}$.

1.6.5 Emptiness of a Column-Page

The mechanism above works well with respect to coloring, but it has a problem that a columnpage created by, for example, a forced page break may not be perfectly empty but can have some coloring \specials for color stack reestablishing and rewinding. They are of course invisible but affect the examination of column-page emptiness for explicit synchronization. That is, we examine if a column-page does not have anything by a tricky way by \pcol@ifempty but the existence of coloring \specials makes the examination failed even if no other ordinary stuff such as boxes and skips are in the column-page.

Therefore we need to put coloring specials for color stack establishing and rewinding a little bit more carefully to avoid empty column-pages just having such specials as follows. When we start a new column-page, we don't put specials for establishing immediately but save the color stack Γ^c into $\Gamma_s = pcol@colorstack@saved$. Then when we leave the column-page by switching or page breaking, we examine the emptiness of the column-page and if so we do nothing, while otherwise we put the specials for reestablishing Γ_s at the top of the column-page and those for rewinding Γ_r at the bottom. Similarly, when we revisit a column-page, we examine its emptiness and if so we save Γ^c into Γ_s , while otherwise we put specials for reestablishing Γ^c and nullify Γ_s so that nothing will be put at the top of the column-page when we leave it. By these mechanisms, an empty column-page should not have coloring specials, while non-empty ones should have a sequence of triples; reestablishing specials; ordinary main vertical list items including coloring specials inserted by color etc.; and then rewinding specials.

1.7 Parallel-Paging, Column-Swapping, Column-Separating Rule Drawing and Background Painting

We have the following four extensions, which are correlated to each other, from the basic parallel-columning.

Parallel-paging to extend the concept of parallel-columning in a page to a pair of adjacent pages. A *left* parallel-page starts from column-0, has C_L columns where C_L is given by the first optional argument of \begin{paracol}, while a *right* parallel-page starts from column- C_L and has $C - C_L$ columns. Since we let $C_L = C$ when parallel-paging is not in effect, we may ship out columns $c \in [0, C_L)$ always and then, if $C_L < C$, ship out columns $c \in [C_L, C)$ as a right parallel-page.

The pair of parallel-pages can be *paired* to comprise a virtual page p and thus has common page number page(p), while *non-paired* parallel-paging produces two individual pages from a

internal page p (i.e., set of all columns $\{c \mid c \in [0, C)\}$) whose left and right components have page numbers page(p) and page(p) + 1 respectively. Since a page p is internally considered as the set of all columns $c \in [0, C)$ always, regardless of paired or non-paired parallel-paging, the difference between them arises only in two-sided ship-out process in which the header, footer and left-margin are common for left/right paired parallel-pags while they have to depend on the parity of the number of each non-paired parallel-page. Note that **paracol** does not specify the parity of a left non-paired parallel-page number, but the number is decided by the page from which a parallel-paged **paracol** environment starts.

In ship-out process, we build the ship-out image of a right parallel-page in our own \box register \pcol@rightpage instead of the usual \@outputbox. The register, however, must survive after \end{paracol} to keep the columns in the last right parallel-page, so that it is shipped out when the whole of last page including post-environment stuff is shipped out, or, more complicatedly, to be passed to the next paracol environment as a part of its pre-environment stuff.

Page-wise stuff spanning all columns, i.e., spanning stuff being pre-environment stuff or page-wise floats, spanning texts, page-wise footnotes and post-environment stuff are always placed in a left parallel-page, while the corresponding regions for them in a right parallel-page are always blank¹²³ unless pre-environment stuff has the last page of the previous paracol environment.

Column-swapping to reverse the order of columns in even numbered pages from left-to-right to right-to-left. It is enabled by the specifier 'c' of \twosided^{124} . Though it is fundamentally simple because we just need to reverse the scanning order of columns from left-to-right (i.e., 0 to C - 1) to right-to-left (i.e., C - 1 to 0) in the ship-out process of an even numbered page, there are a few complications in the implementation of related functionalities.

First, a paired parallel-page should also be swapped so that a *physical* left (resp. right) parallel-page has columns C - 1 to C_L (resp. $C_L - 1$ to 0) in this order. Note that this parallel-page swapping also swaps the page in which page-wise stuff are placed. That is, if both paired parallel-paging and column-swapping are in effect, page-wise stuff are placed in the physical right parallel-page, or in other words they always placed in the page in which column-0 resides. Note that since column-swapping with non-paired parallel-paging is meaningless and thus column-swapping is disabled.

Second, the side margin to which a marginal note goes can be swapped but enabling this swap is independent of column-swapping and done by the specifier 'm' of \twosided, though almost all users will specify both swapping consistently. Since the side margin for a marginal note is decided in \output routine by \pcol@addmarginpar being our own version of IAT_EX's macro for marginal notes \@addmarginpar, the page in which the marginal note resides has been fixed. However, the number of the page and thus its parity may not have been fixed yet due to the possible jump in column-0 taking place afterward, unlike column-swapping for which the page number has been fixed because it is performed in ship-out process. Since it is too costly to avoid this possibly wrong placement, we have to accept the possibility as IAT_EX itself does. Also unlike column-swapping, the swapping of marginal notes is not disabled in non-paired parallel-paging because it is meaningful.

Another remark for marginal notes is that two ore more columns may *share* a margin, inevitably if a (parallel) page has three or more columns or intentionally with a setting of \marginparthreshold. Therefore, the context of marginal notes cannot be in column-context

¹²³So far. In some future, we could implement a special setting to let pre-environment stuff, post-environment stuff and page-wise footnotes are split into both parallel-pages, and to make it possible that a page-wise float or a spanning text has its counterpart placed in the corresponding right parallel-page.

 $^{^{124}\}mathrm{Or}$ the backward compatible macro <code>\swapcolumninevenpages</code>.

but should be in page context, or cannot simply give the bottom of the last marginal note (i.e., IATEX's \@mparbottom) but should show all marginal notes in margins in a page¹²⁵. Therefore, each page context has all marginal notes in the form of lists of their top and bottom positions in all margins as $\pi^m(p)$, so that we find a space for a marginal note in a column to add it to not only to the bottom but also into a space between two marginal notes having already been put by other columns.

Third and finally, we have to take care the placement of spanning texts. In version 1.2 to which column-swapping is introduced, we let a spanning text belong to column-(C-1) instead usual column-0 so that its left edge is aligned to the left edge of the leftmost column, i.e., that of the text area. However this simple solution has a severe problem that, if a spanning text is broken into two pages, its second half should be put in the rightmost column. In addition, even when a spanning text does not have page break in it, such wrong placement may happen if the text is followed by **\nobreak** and thus a page break is made above the text but *after* the text is processed.

In version 1.3, this problem is solved by capturing the first half of a spanning text in $\quad truther routine for the page break in the text, and the second half or the whole of it in that for synchronized column-switching to close the text. Since an invocation of <math>\quad truther routine means that it has been fixed which page the spanning text or its part resides in, we can place the text much more reliably expecting the parity of the page number has also been fixed. In addition, this decision making in <math>\quad truther routine allows$ (or forces) us to let spanning texts always belong to column-0 preserving the consistency of, for example, local counter values referred to in them, while we need to shift a text to the left edge of the text area if it resides in an even numbered page. Furthermore, this spanning text capturing enables to measure the vertical size of the captured text together with the vertical position of its top edge to record them in the list $\pi^s(p)$, so that we draw column-separating rules skipping the text and painting its background with a specific color different from colors of columns and column-separating gaps, as discussed shortly.

Column-separating rule drawing to draw a vertical rule in *column-separating gap* is correlated with a part of *background painting* to paint each region in a page with a color specific to the region. Thanks to the list of spanning texts $\pi^s(p) = (span(H_i, h_i))_i^n$, we can draw column-separating rules skipping spanning texts in the page p as the sequence of;

$$rule(H'_1), gap(h_1), \dots, rule(H'_n), gap(H'_n), rule(H'_{n+1})$$
$$H'_i = H_i - (H_{i-1} + h_{i-1}) \qquad H_0 = h_0 = 0 \qquad H_{n+1} = \pi^h(p)$$

where rule(H') is a vertical rule of H' high and gap(h) is a vertical space of h. A rule may be colored with the color specified by **\colseprulecolor** for each column-separating gap or all of them. Note that if column-swapping is in effect, a column c is *preceded* by c-th columnseparating gap which may have its own width and color for its rule, rather than being followed by it.

Background painting also uses the list $\pi^s(p)$ to paint the background of each column-*c* with the color B_c^c , each column-separating gap following the column-*c* with B_g^c , and spanning texts with B_s and B_s , where $B_a^{[c]}$ is specified by the second argument of $\bckgroundcolor{a[c]} \{color\} (a \in {c, g, s, S})$ and kept in the macro $\close{a[c]} (a \in {c, g, s, S})$ and kept in the macro $\close{a[c]} (a \in {(x, y) | x \in S)}$

 $^{^{125}}$ Before version 1.3, we have \@mparbottom in column-context because a column has its own area for marginal notes, which can be the gap between columns rather than a margin of a page.

 $[x_0, x_1), y \in [y_0, y_1)$ of the top-down xy-coordinate whose origin is at the left-top corner of the leftmost column.

$$\begin{split} R_c^c(i) &= [(W_c, \ H_{i-1} + h_{i-1}) \ (W_c + w_c, \ H_i + d_{c/g})] \\ R_g^c(i) &= [(W_c + w_c, \ H_{i-1} + h_{i-1}) \ (W_{c+1}, \ H_i + d_{c/g})] \\ R_{\{s,S\}}(i) &= [(0, \ H_i) \ (W_T, \ H_i + h_i + d_s)] \\ W_c &= \sum_{d=c_0}^{c-1} (w_c + g_c) \qquad c_0 = \begin{cases} 0 & c < C_L \\ C_L & c \ge C_L \end{cases} \\ W_T &= \textwidth \\ d_{c/g} &= \begin{cases} \maxdepth & i = n+1 \ \land \ H'_{n+1} > 0 \ \land \ non-last \ page \\ 0 & otherwise \end{cases} \\ d_s &= \begin{cases} H_{n+1} - (H_n + h_n) + \maxdepth & i = n \ \land \ H'_{n+1} = 0 \ \land \ non-last \ page \\ otherwise \end{cases} \end{split}$$

In the specifications above, w_c and g_c is the width of the column c and that of the columnseparating gap following it, defined by \columnratio or \setcolumnwidth and stored in \pcol@columnwidth·c and \pcol@columnsep·c respectively. The additions of $d_{c/g}$ and d_s are to extend the bottom edge of each region down to the bottom of text area. In addition, for each $R_a^{[c]} = [(x_0, y_0)(x_1, y_1)]$, extensions $e_a^{[c]}(\{x, y\}^{\pm})$ can be specified to shift the base points x_0, y_0, x_1 and y_1 left (x^-) , right (x^+) , upward (y^-) and downward (y^+) respectively. That is, a region is defined as;

$$R_a^{[c]} = [(x_0 - e_a^{[c]}(x^-), y_0 - e_a^{[c]}(y^-)) (x_1 + e_a^{[c]}(x^+), y_1 + e_a^{[c]}(y^+))]$$

with the optional shifts specified by the first argument of \backgroundcolor as $\{a[c] (x^{\pm}, y^{\pm})\}$ (for both x^{-}/y^{-} and x^{+}/y^{+}) or $\{a[c] (x^{-}, y^{-}) (x^{+}, y^{+})\}$ and kept in macros \pcol@bg@ext@ $d \cdot @ \cdot a[\cdot @ \cdot c]$ where $d \in \{1, \mathbf{r}, \mathbf{t}, \mathbf{b}\}$ for x^{-} (1), x^{+} (r), y^{-} (t) and y^{+} (b). Note that $e_{a}^{[c]}(\{x, y\}^{\pm})$ can be extremely large, namely greater than or equal to 9000pt, to mean the region is extended to a border near by the corresponding paper edge. More specifically, by this *infinite extension*, each xy coordinate in $[(x_0, y_0)(x_1, y_1)]$ is defined as follows to represent a coordinate being 10000 pt $-e_{a}^{[c]}(\{x, y\}^{\pm}) +$ \pagerim inside from the page edge;

$$\begin{split} x_0 &= -W_M + (10000 \, \mathrm{pt} - e_a^{[c]}(x^-) + W_R) \\ y_0 &= -(H_S + H_M) + (10000 \, \mathrm{pt} - e_a^{[c]}(y^-) + H_R) \\ x_1 &= (W_P - W_M) - (10000 \, \mathrm{pt} - e_a^{[c]}(x^+) + W_R) \\ y_1 &= (H_P - H_S - H_M) - (10000 \, \mathrm{pt} - e_a^{[c]}(y^+) + H_R) \\ W_P &= \mathbb{paperwidth} \\ W_M &= 1 \mathrm{in} + \begin{cases} \mathbb{p} \\ \mathbb{$$

where f_{even} is *true* iff we are in an even numbered page and two-sided typesetting is specified by the optional argument of \documentclass or by the specifier 'p' of \twosided explicitly or implicitly. Another remark is that column-swapping affects $R_c^c(i)$ and $R_s^c(i)$ to *mirror* the region making a reflection-symmetric transformation on it using a vertical edge of a page as the axis. That is, $[(x_0, y_0)(x_1, y_1)]$ for a region is transformed to $[(W_T - x_1, y_0)(W_T - x_0, y_1)]$ if $x_{\{0,1\}}$ is not extended infinitely. With infinite extension on the other hand, before this transformation x_0 and/or x_1 are calculated by the rule above replacing W_M with $W_P - (W_M + W_T)$ to represent the width of the right margin rather than the left.

On the other hand, the mirroring of $R_{\{s,S\}}$ is enabled by the specifier 'b' of \twosided, together with other regions being top margin (t,T), bottom margin (b,B), left margin (l,L), right margin (r,R), page-wise floats (f,F) and page-wise footnotes (n,N). The geometrical specifications R_a for those regions are given as follows, but the coordinate origin is at the top-left corner of text area (rather than the leftmost column).

$$\begin{split} R_{\{t,T\}} &= [(-W_M + W_R, \ -H_M + H_R), \ (W_P - W_M - W_R, \ 0)] \\ R_{\{b,B\}} &= [(-W_M + W_R, \ H_T - H_M), \ (W_P - W_M - W_R, \ H_P - H_M - H_R)] \\ R_{\{l,L\}} &= [(-W_M + W_R, \ 0), \ (0, H_T)] \\ R_{\{r,R\}} &= [(W_T, \ 0), \ (W_P - W_M - W_R, \ H_T)] \\ R_{\{f,F\}} &= [(0, \ 0), \ (W_T, \ H_S)] \\ R_{\{n,N\}} &= [(0, \ H_T - H_N) \ (W_T, \ H_T)] \\ H_T &= \textheight + \mbox{maxdepth} \\ H_N &= \skip\footins + \ht\footins + \dp\footins \end{split}$$

Note that, since we use text area coordinates, in the calculation of infinite extension H_S is let be 0.

We have other regions for columns and column-separating gaps, namely R_C^c and R_G^c , which vertically span all over text area regardless existence of any page-wise stuff. Therefore, their geometrical specifications are as follows with text area coordinates.

$$R_C^c = [(W_{c-1}, 0), (W_{c-1} + w_c, H_T)]$$

$$R_G^c = [(W_{c-1} + w_c, 0), (W_c, H_T)]$$

In addition, we have to paint pre-environment stuff and post-environment stuff with color $B_{\{p,P\}}$. The region $R_{\{p,P\}}$ for them is defined as follows with text area coordinates where H_B is the *y*-coordinate of the bottom of previous **paracol** environment if any, or 0 otherwise.

$$R_{\{p,P\}} = \begin{cases} [(0, H_B) (W_T, H_S)] & \text{pre-environment stuff} \\ [(0, H_B) (W_T, H_T)] & \text{post-environment stuff} \end{cases}$$

Note that painting of post-environment stuff is done *outside* paracol environment when the post-environment stuff encounters a page break, unless another paracol environment starts in the page and thus the post-environment stuff becomes pre-environment stuff of the second (or subsequent) environment.

Finally, we define the order of background painting as follows, where a, a(i), a^c and $a^c(i)$ mean R_a , $R_a(i)$, R_a^c and $R_a^c(i)$ respectively, so that a succeeding region is *overlaid* on preceding regions.

$$T \to B \to L \to R$$

$$\to G^0 \to \dots \to G^{C-2} \to C^0 \to \dots \to C^{C-1}$$

$$\to t \to b \to l \to r \to N \to n \to \{F, P\} \to \{f, p\}^{126}$$

$$\to S(1) \to \dots \to S(n)$$

$$\begin{array}{l} \rightarrow g^{0}(1) \rightarrow \cdots \rightarrow g^{C-2}(1) \rightarrow c^{0}(1) \rightarrow \cdots \rightarrow c^{C-1}(1) \rightarrow s(1) \\ \rightarrow \cdots \\ \rightarrow g^{0}(n) \rightarrow \cdots \rightarrow g^{C-2}(n) \rightarrow c^{0}(n) \rightarrow \cdots \rightarrow c^{C-1}(n) \rightarrow s(n) \\ \rightarrow g^{0}(n+1) \rightarrow \cdots \rightarrow g^{C-2}(n+1) \rightarrow c^{0}(n+1) \rightarrow \cdots \rightarrow c^{C-1}(n+1) \end{array}$$

1.8 Page-wise Float Placement

In the release on 2015/01/10, IATEX's float placement mechanism was drastically changed to avoid *out-of-order* appearance of page-wise floats as follows. Since the cause of overtaking of a page-wise float by a column-wise float is that they are in two separated lists \@dbldeferlist for the former and \@deferlist for the latter, in the new implementation the two lists are merged to let all floats go to \@deferlist. To distinguish page-wise and column-wise floats in the list, \end@dblfloat lets the page-wise float processed by the macro have a special depth of 1sp, while depth of column-wise floats are 0 since \@endfloatbox add a \vskip of 0 at the end of the box of floats.

Then all float placement macros invoked in **\output**-routine examine the depth of floats in the list they are working on against a newly introduced macro **\f@depth** by also newly introduced **\@testwrongwidth**, so that they process only floats of a page/column category specified by **\f@depth**, while those not matching to **\f@depth** are let go to **\@deferlist** to inhibit succeeding floats of the same type from overtaking them. The **\definition** of **\f@depth** is done only by modified **\@dblfloatplacement**, always invoked in a group, to let it have **1sp** so that float placement macros usually work on column-wise ones with the default setting of **\f@depth** = **\z@** except for special occasions in which the placement of page-wise floats is tried.

Though the mechanism should work well with *ordinary* multi-columned documents, it is incompatible with **paracol** almost inherently. That is, in the first place we have to separate float-related lists into the sets of them corresponding to columns as we do¹²⁷. Therefore, it is obviously nonsense to merge the list for page-wise floats, i.e., \@dbldeferlist, to \@deferlist of a particular column, and thus we have to stick with the conventional implementation to process page-wise and column-wise floats separately as follows.

- (1) We \define our own \end@dblfloat namely \pcol@end@dblfloat whose definition is exactly same as the old version of \end@dblfloat, and replace the new version with it by \letting them equivalent in \pcol@zparacol by which start paracol environments. Therefore, page-wise floats composed in a paracol environment is processed in the traditional way, i.e., being included in \@dbldeferlist rather than \@deferlist and having ordinary depth 0.
- (2) Each invocation of \@dblfloatplacement in our own \output-routine is followed by a \let to nullify the setting of \f@depth = 1sp done by \@dblfloatplacement by doing \f@depth=\z@. By this setting, \@tryfcolumn in \pcol@startpage and \@makefcolumn in \pcol@output@clear work on their argument \@dbldeferlist in the way exactly same as in 2014 or before.

¹²⁶In column flushing, the order is $\{F, P\} \rightarrow \{f, p\} \rightarrow N \rightarrow n$ but this reversion should have no effect (almost always).

¹²⁷If counters figure and table are global and we have to avoid inter-column overtaking with respect to, for example, the partial ordering rooted by the top-left corner, merging column-wise lists together with the merge of \@deferlist and \@dbldeferlist might be a solution to let the depth of a column-wise float be $c \, sp$ while that of page-wise is $C \, sp$. However such implementation is not only tough but also doubtful to be worthwhile.

- (3) Among IATEX's macros in its \output-routine which we use in our own one as well, only \@addtodblcol changed its target from \@dbldeferlist to \@deferlist. That is, if the macro fails to put a page-wise float to the page we just have started by \pcol@startpage, the float is added to \@deferlist rather than \@dbldeferlist. Therefore, when we apply \@sdblcolelt to the copy of \@dbldeferlist to invoke \@addtodblcol for each of its element float, we have to save \@deferlist somewhere, to \reserved@c in reality, and clear it prior to the application. Then after all elements are processed, we have to let \@dbldeferlist have what \@deferlist have, while \@deferlist should regain its original contents from the saved place. A subtle issue is that we might work with IATEX of 2014 or older in which the floats are returned to \@dbldeferlist. Therefore to make paracol compatible with both of new and old versions, we have to add \@deferlist to \@dbldeferlist rather than replacing \@dbldeferlist with \@deferlist. This addition should work well, because we clear both lists before the application of \@sdblcolelt and then one of them will have the still-deferred floats after the application while the other remains empty.
- (4) We convert \@deferlist to \@dbldeferlist in \pcol@output@start to start a paracol environment, and perform the reverse operation in \pcol@output@end to close the environment. Though it is very unlikely (or maybe impossible) that the \@deferlist imported in the former operation has LATEX's (i.e., not paracol's) double-column floats of 1sp deep, we make such floats old-fashioned making their depth 0 so that they can be put in a page built in the paracol environment. On the other hand, the latter cannot export a list having floats of 1sp deep because they have been produced in the closing paracol environment or have passed our custom \pcol@output@start when they were imported¹²⁸.

Note that the operations (1), (2) and (4) are fully compatible with 2014 or older version of IATEX, because with the old version; (1) \pcol@end@dblfloat is equivalent to \end@dblfloat; (2) modification of \f@depth cannot be seen because it does not exist; and (4) we virtually do nothing in the importation. As for (3), we explicitly take care of the compatibility as shown above.

2 Interaction with T_EX and PT_EX

The macros of paracol interacts with T_EX and LAT_EX through various registers and macros as discussed in this section.

2.1 Registers

2.1.1 Insertion Registers

- \footins is used to \insert footnotes through it by \footnote and \footnotetext, and then in \output routine the footnotes \inserted in a page is presented in the register. The register is referred to by the following macros.
 - \pcol@makecol examines if the register has page-wise footnotes and, if so, saves it into $\pi^f(p)$ if $p = p_t$ or discards it otherwise.

 $^{^{128}}$ Therefore, if one try to *smuggle* a double-column float of the new scheme into a **paracol** and to pass it through the environment to another double-column world, the float will become a single-column one. Even if such guy a really exists and complains about this transformation, however, we have good right to say "don't do that".

- \pcol@startcolumn \inserts $\pi^f(p)$ into the column-page to be created through the register.
- \pcol@specialoutput logs the contents of the register for debugging.
- \pcol@output@start examines if the register has footnotes to be merged with those in paracol environment, refers to its height plus depth to calculate effective \@colht, and/or \inserts its contents through itself to the main vertical list as the first part of merged footnotes.
- \pcol@makenormalcol combines footnotes in the register to other pre-environment stuff to make a spanning stuff, or makes save/restore of the register to/from \@tempboxa to exclude footnotes from spanning stuff when merged-footnote typesetting is specified.
- \pcol@output@switch saves the register into $\pi^f(p)$ or $\kappa_c(\tau)$, or discards its contents, when we leave from the column c with footnotes.
- \pcol@restartcolumn restores $\kappa_d(\tau)$ or $\pi^f(p)$ to the register and then \inserts the contents of \box\footins into itself so that it contributes to the main vertical list to be rebuilt for the column d.
- \pcol@getcurrfoot for column d lets the register have $\kappa_d(\tau)$.
- \pcol@savefootins saves the register into an \insert for $\pi^f(p)$ or $\kappa_c(\tau)$.
- \pcol@deferredfootins refers the \skip component of the register to have the vertical skip above page-wise footnotes and \inserts deferred footnotes through the register.
- \pcolCoutputCend \inserts $\pi^f(p)$ into the last page through the register.
- \pcol@fntexttop{*text*} \inserts the footnote $\langle text \rangle$ and a penalty through the register.
- \pcol@fntextbody{*text*} refers to the \skip component of the register to cap the height of the footnote (*text*).
- $\label{eq:linear_states} $$ \sum_{\sigma \in \mathcal{T}_{c}} \sum_{\sigma \in \mathcal{T}_{c}} \left(\sum_{\sigma \in \mathcal{T}_{c}} \sum_{\sigma \in$

2.1.2 Integer Registers

- \deadcycles is T_EX's primitive register to count the number of \output requests made between two \shipout operations. It is zero-cleared by \pcol@invokeoutput because it can have a large number in a paracol environment.
- **\outputpenalty** is TEX's primitive register to have the page-break penalty with which **\output** routine is invoked. It is referred to by **\pcol@output** to know whether it has special code

less than -10000, and by \pcol@specialoutput in detail for the dispatch according to the code. The register is also used for the communication from the latter, which lets it be -10000 for our own special \output routines, to the former to determine \vsize according to if the register has a value greater than -10004 or not.

- \interlinepenalty is T_EX's primitive register to have the page-break penalty inserted between two lines. The register is referred to in the following macros.
 - \pcol@output@start to make pre-environment merged footnotes followed by this \penalty on the \insertion, and to insert it to start the first column-page allowing page-break before the start unless it is inhibited by \if@nobreak = true.
 - \pcol@restartcolumn to insert this \penalty to resume a column-page allowing page-break if \if@nobreak = false.
 - \pcol@deferredfootins to let the second half of split Φ have this \penalty as the very first element.
 - \pcol@fntexttop{*text*} to make the footnote (*text*) followed by this \penalty on the \insertion.
 - \pcol@fntextother{*text*} to make the footnote $\langle text \rangle$ preceded by this \penalty in Φ .
 - \pcol@fntextbody to let the register have \interfootnotelinepenalty.
- floatingpenalty is T_EX 's primitive register to have the page-break penalty added to \insertpenalties if an \insert is moved to the page next to the page in which the line having the \insert resides. It is let have 20000 in \pcol@fntextbody for footnote typesetting.
- \vbadness is TEX's primitive register to have the threshold of the badness of \vbox construction with underfull messages. That is, if the badness exceeds the threshold on a \vbox construction, TEX will complain showing an underfull message. In \pcol@makenormalcol and \pcol@deferredfootins, the register is temporarily let have 10000 to avoid that \@makecol invoked in the former and \vsplit done in the latter causes the message with inevitable underfull.
- \showboxdepth is T_EX's primitive register to determine the maximum depth of box structure to be shown in logging etc. The register is let have 10000 in \pcol@ShowBox for full logging.
- \showboxbreadth is TEX's primitive register to determine the maximum breadth of box structure to be shown in logging etc. The register is let have 10000 in \pcol@ShowBox for full logging.
- \interfootnotelinepenalty is an API \count register to have \interlinepenalty for footnotes. It is used in \pcol@fntextbody to let \interlinepenalty have it.
- **@ne** is a **chardef** register to have 1. The register is referred to by the following macros mainly for incrementing another register.

\pcol@F@count, \pcol@output, \pcol@opcol, \pcol@setpnoelt, \pcol@nextpage, \pcol@nextpelt, \pcol@startpage, \pcol@checkshipped, \pcol@outputelt, \pcol@ioutputelt, \@outputpage, \pcol@bg@paint@ii, \pcol@output@start, \pcol@makenormalcol, \pcol@output@switch, \pcol@setcurrcol, \pcol@iscancst, \pcol@addmarginpar, \pcol@do@mpbout@i, \pcol@sync, \pcol@flushcolumn, \pcol@measurecolumn, \pcol@synccolumn, \pcol@makeflushedpage, \pcol@imakeflushedpage, \pcol@iflushfloats, \pcol@freshpage, \pcol@output@end, \pcol@invokeoutput, \pcol@zparacol, \pcol@setcolwidth@r, \pcol@setcolwidth@s, \pcol@setcw@scan, \pcol@setcw@calcf, \pcol@synccounter, \pcol@com@syncallcounters, \pcol@stepcounter, \pcol@com@switchcolumn, \pcol@sptext, \pcol@visitallcols, \pcol@ifootnote, \pcol@ifootnotemark. \pcol@swapcolumn, \pcol@set@color@push,

\tw0 is a \chardef register to have 2. It is used in \pcolOsetcurrcol to let $\kappa_c(\sigma) = 2$ when \ifOnobreak = true but \ifOafterindent = false, in \pcolOsetcwOcalcf $\langle x \rangle \langle y \rangle \langle z \rangle$ to calculate $x \cdot 2^k$, $y/2^k$ and $(x/y) \cdot 2^k$ with various k, and in \pcolOswapcolumn to calculate $C^1 - (c' - C^0) - 2 = c - 1 = c^g$ for the column-separating gap ordinal c^g physically following the column c at the position c'.

\mCne is a \count register to have -1. It is used in the following macros.

- \pcol@setpnoelt, \pcol@nextpelt, \pcol@getpelt and \pcol@setmpbelt to decrement \@tempcnta which initially has $p p_b$ for a page p.
- \pcol@bg@paint@i to decrement C_b^1 by one locally to have the column scanning range $[C_b^0, C_b^1-1)$.
- \pcol@iscancst to decrement n_{pop} by one.
- \pcol@do@mpbout@i to let \@tempcnta have it to indicate left margin.
- \pcol@setcolwidth@r to calculate $C^1 C^0 1$.
- \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$ in \@whilenum loops to calculate $z'/2^k$ and z'/2k 16 where $z'/2^k \approx x/y$.
- \pcol@iadjustfnctr to decrement \c@footnote.
- \sixt@On is a \chardef register to have 16. It is used in \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$ to calculate $Z = z \times 1 \text{ pt} = z' \cdot 2^{16-k}$ where $z'/2^k \approx x/y$.
- \@m is a \mathchardef register to have 1000. It is used in \pcol@synccolumn and \pcol@ output@end to let \prevdepth = 1000 pt on a synchronization or the closing paracol environment with an empty main vertical list, and in \pcol@setcw@getspec@i to add 1000 pt to stretch and shrink components of \@tempskipa having a column/gap specification to make it sure the skip register has those components.
- \CM is a \mathchardef register to have 10000. It is used in the following macros
 - \pcol@ShowBox to let \showboxdepth and \showboxbreadth have 10000 for full logging of a box.
 - \pcol@output to examine if <code>\outputpenalty</code> < -10000 to mean a special <code>\output</code> request.
 - $\col@specialoutput to let \outputpenalty = -10000 to tell \pcol@output that the special \output request is our own.$
 - \pcol@makenormalcol and \pcol@deferredfootins to let \vbadness have 10000 temporarily to avoid underfull messages.

- \pcol@synccolumn to bias \pcol@textfloatsep by 10000 pt to indicate a columnpage has an MVL-float and in \pcol@cflt and \pcol@addflhd to remove the bias.
- \pcol@switchcol and \pcol@flushclear to put \penalty-10000 for forced page break.
- \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$ to let $Z = z \times 1 \text{ pt} = 10000 \text{ pt}$ if x/y is too large.
- \@Mii is a \mathchardef register to have 10002. It is used in \pcol@end@dblfloat to examine if \@floatpenalty = -10002 to mean the float environment to be closed is given in horizontal mode.
- \@Miv is a \mathchardef register to have 10004. It is used in \pcol@output to examine if \outputpenalty = -10004 for a dummy \output request made by IATEX's float-related macros and our \pcol@invokeoutput to ensure the real request is not eliminated when it is made at the very beginning of a page or a column-page. It is also used in \pcol@ specialoutput for footnote logging when \outputpenalty = -10004.
- \@MM is a \mathchardef register to have 20000. It is used in \pcol@fntextbody to let \floatingpenalty have it for footnote typesetting.
- \@beginparpenalty is a \count register to have the page-break penalty inserted before the first \item of each list-like environment. The penalty is determined in class files and is, for example, -\@lowpenalty = -51 with article.cls. It is referred to and inserted by \pcol@zparacol when it finds the paracol environment to start is at the very beginning of a list-like environment.
- \@floatpenalty is a \count register to have the penalty code -10002 or -10003 given by \@xfloat at the beginning of a float environment according to the environment is in horizontal or vertical mode respectively, or by \marginpar for a marginal note in the same meaning. It is referred to by \pcol@end@dblfloat to insert the penalty, and by \pcol@xympar to confirm \marginpar is error free.
- \@topnum is a \count register to have the maximum number of top floats which the current column-page can accept further. It is used in \pcol@setcurrcol and \pcol@iigetcurrcol to save/restore it into/from $\kappa_c(\nu_t)$. The macro \pcol@synccolumn also lets \@topnum = 0 to inhibit top-float insertions in the current column-page any more after a synchronization.
- \@botnum is a \count register to have the maximum number of bottom floats which the current column-page can accept further. It is used in \pcol@setcurrcol and \pcol@ iigetcurrcol to save/restore it into/from $\kappa_c(\nu_b)$.
- \@colnum is a \count register to have the maximum total number of floats which the current column-page can accept further. It is used in \pcol@setcurrcol and \pcol@ iigetcurrcol to save/restore it into/from $\kappa_c(\nu_c)$.
- \c@page is LATEX's counter page being a \count register to have the page number. It is referred to by \pcol@setpnoelt, and \pcol@output@start to let $\pi^p(p) = page(p)$. The macro \pcol@startpage reload the register from $\pi^p(p_t-1)$ and then increment it by one

usually but two in non-paired parallel-paging, and repeat $\pi^p(p_t) = page(p_t)$ and incrementing page(p) for each float pages of page-wise floats. Reloading page(p) to the register from $\pi^p(p)$ is also done by \pcol@getpelt for macros using \pcol@getcurrpage, and by \pcol@outputelt, \pcol@sync and \pcol@makeflushedpage by \pcol@getcurrpinfo. Then the register is referred to by the following macros to examine its parity.

- Our own \Coutputpage to give page(p) or page(p) + 1 to \pcolCoutputpageCl and \pcolCoutputpageCr which finally let the register have the value to be referred to by \pcolCoutputpage being LATEX's \Coutputpage.
- \pcol@bg@swappage to determine the values of \pcol@bg@leftmargin and \ifpcol@bg@cswap with other factors.
- \pcol@shiftspanning to decide the necessity of shifting spanning text left with column-swapping, examining $raw \c@page$ at the \output request to close the spanning text rather than $\pi^p(p_t)$ which will have the correct value with respect to possible jump *after* the macro completes its work.
- \pcol@addmarginpar to determine the margin to which a marginal note goes.
- \pcol@do@mpbout@i to determine which of M_L^l or M_L^r is the target of the operation specified by \pcol@do@mpbout@elem.
- \pcol@swapcolumn $\langle c_1 \rangle \langle c_2 \rangle \langle C^0 \rangle \langle C^1 \rangle$ to determine c_2 for c_1 if column-swapping is in effect.

In addition, to do the parity examination in \pcol@bg@swappage above correctly, the macros \pcol@ioutputelt, \pcol@makeflushedpage, \pcol@imakeflushedpage, \pcol@iflushfloats and \pcol@output@end temporarily increment the register by one when they are working on a right non-paired parallel-page.

The other users are $localcounter{ctr}$ to check $\langle ctr \rangle \neq page$, pcol@remctrelt to let $cl@.\theta = pcol@stepcounter{\theta}$ unless $\theta = page$, and pcol@FF to write it to a log file as a part the logging information of memory leak debugging.

- $\operatorname{count} @$ is a count register for temporary use. It is used in $\operatorname{pcol}@iscancst$ to have m of $\gamma_{i,m}$, $\operatorname{pcol}@addmarginpar$ to have the physical column position of the current column c in which $\operatorname{marginpar}$ is given, and in $\operatorname{pcol}@extract@fil@i(s) @nil</code> to extract the unit of the stretch component <math>s$ of a glue.

\@tempcnta is a \count register for temporary use. The usages of this register are as follows.

• In \pcol@F@count, it is used to measure the cardinality of \@freelist.

- In $\col@makecol,$ it is used to keep $page(p_t)$ gotten by $\col@getcurrpinfo$ until we store it back by $\col@defcurrpage.$
- In \pcol@setpageno, \pcol@setpnoelt, \pcol@nextpage, \pcol@nextpelt, \pcol@getcurrpage, \pcol@getpelt, \pcol@addmarginpar and \pcol@setmpbelt, it has p q when we scan $\pi(q)$ for all $q \in [p_b, p_t]$ and the current column-page is at p.
- In \pcol@checkshipped, it has c when we scan S_c for all $c \in [0, C)$ to examine if all of them are not empty and thus we have pages to be shipped out.
- In \pcol@ioutputelt, it has c' when we scan $s_c(q)$ for all $c \in [0, C_L)$ or $c \in [C_L, C)$ to build the shipping out image of a page q, where c = c' or $c = C^1 1 (c' C^0)$ where $(C^0, C^1) \in \{(0, C_L), (C_L, C)\}$.
- In \Coutputpage, it has page(p) or page(p) + 1 to be given to \pcolCoutputpageC
 1 or \pcolCoutputpageCr as their argument when they are used to ship out the second (not always right) component of a parallel-page pair.
- In $\colorsection C_b^0, c$ to sum up the width of columns and column-separating gaps in the range.
- In \pcol@output@switch, it is used to have page(p) obtained by \pcol@getcurrp info and simply to store the value in $\pi^p(p)$ by \pcol@defcurrpage when we use these macros to add an element to $\pi^s(p)$ and/or let $\pi^f(p) =$ \footins.
- In \pcol@setcurrcol, it has the code calculated from \if@nobreak and \if@after indent to be saved in κ_c(σ).
- In \pcol@scancst(box), it is let have (box) ∈ {\pcol@colorins, \pcol@color stack@saved} and then is referred to in \pcol@iscancst.
- In \pcol@addmarginpar besides the page scan shown above, it is used to scan all columns whose physical position is left from the current column c to measure the distance between the left edges of the leftmost column and c.
- In $\pcol@do@mpbout@i</code>, it has <math>\pm 1$ according to the margin (left = -1) which marginal notes outside paracol environments goes to.
- In \pcol@flushcolumn, it is used to throw $page(p_t)$ away when we get it by \pcol@ getcurrpinfo because we don't need it.
- In \pcol@setcolwidth@r, it has c to scan fractions r_d where $d = c C^0$ in its argument $\langle ratio \rangle$ specified by \columnatio, and then to distribute the unspecified portion of \textwidth evenly to w_c for all $c \in [C^0+k+1, C^1)$, where k is the number of fractions and $(C^0, C^1) \in \{(0, C_L), (C_L, C)\}$.
- In \pcol@setcw@scan $\langle C^0 \rangle \langle C^1 \rangle \{spec\}$, it has c for two loops for $c \in [C^0, C^1)$ to add ',' to the tail of $\langle spec \rangle$ as many as $k = C^1 C^0$ and then to process first k elements in $\langle spec \rangle$, and is referred to by \pcol@setcw@set invoked in the second loop.
- In \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$, it used to calculate and to have k such that $z'/2^k \approx x/y$.
- In \pcol@cmpctrelt, it has $val(\theta)$ of a counter θ to be compared with $val_0(\theta)$.
- In \column it has $(c + 1) \mod C$ being the target of column-switching.
- In \pcol@sptext, it temporarily has d being the target of column-switching during we let \pcol@nextcol have 0 to visit the leftmost column to put a spanning text.

- In \pcol@visitallcols, it has $d \in [0, C) \{c\}$ being the columns to be visited for column-scanning.
- In \definecolumnpreamble{c}{pream}, c is assigned to the register to ensure c is a number.
- In \pcol@calcfnctr, it has the footnote ordinal calculated by the macro to be referred to by the invokers \pcol@iadjustfnctr and \pcol@iifootnotetext.
- In $\max lt_l [t_r]$ it is let have t_l , while in the related macro $\sum t_r$.

\@tempcntb is a \count register for temporary use. It is used in the following macros.

- In \pcol@ioutputelt it has c, while in \pcol@imakeflushedpage and \pcol@iflushfloats it has c', to have c = c' or $c = C^1 1 (c' C^0)$ according to column-swapping for c'-th iteration of column scanning loop for $c' \in [C^0, C^1)$, where $(C^0, C^1) \in \{(0, C_L), (C_L, C)\}.$
- In \collectronscol
- In \pcol@addmarginpar, it is let have the column number d whose physical position is left from the current column c to measure the distance between the left edges of the leftmost column and c.
- In \pcol@sync and \pcol@measurecolumn, it has the (so-far) tallest column which gives V_P.
- In \pcol@setcolwidth@r, it has $C^1 C^0 1$ then $C^1 1$ and finally $C^1 \min(C^0 + k, C^1 1)$, where k is the number of fractions given in the argument of \columnratio and $(C^0, C^1) \in \{(0, C_L), (C_L, C)\}$.
- In \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$, at first it is used to calculate $z'/2^k \approx x/y$ and then to calculate $Z = z \times 1 \text{ pt} = z' \cdot 2^{16-k}$.
- In $\coloriginal cols$, it has $c = \color color color cold if from the column-scan targets.$

2.1.3 Dimension Registers

- vsize is T_EX 's primitive register to have the height of a page or a column-page being built. It is let be Qcolroom or maxdimen by pcolQoutput.
- **\hsize** is T_EX's primitive register to have the width of a page or a column-page being built. It is let be w_c by **\pcol@invokeoutput** to restart (or stay in) the column c, be **\textwidth** by **\pcol@sptext** for spanning text, and be either of **\textwidth** or w_c by **\pcol@ fntextbody** according to the footnote typesetting being page-wise or column-wise respectively.
- \maxdepth is TEX's primitive register to have the maximum depth of the page being built. In IATEX, it is assumed that its value is fixed at \begin{document}, in which the value is saved into \@maxdepth, for the typesetting throughout the document, unless a bottom float is added to a page in which the register is let have 0 until it is shipped out. This temporary setting for a page with bottom floats has some reasonability but its implementation for paracol environments having column-switching from/to a column-page with bottom floats to/from another one without them is too costly¹²⁹. Therefore, we

 $^{^{129}}$ That is, we would need to incorporate \maxdepth as a member of column-context, but we don't because the idea of temporary setting itself is too vague to pay the effort and a precious membership in column-context.

let the register have <code>\Qmaxdepth</code> in <code>\pcolQoutput</code> and <code>\pcolQcombinefloats</code> to cancel the temporary setting done in <code>\Qaddtobot</code> for the references by T_EX 's page builder and <code>\Qcflt</code> respectively.

- \boxmaxdepth is T_EX's primitive register to have the maximum depth of \vboxes. The macros \pcol@cflt, \pcol@opcol, \pcol@ioutputelt, \pcol@combinefloats, \pcol@output@ flush and \pcol@output@clear let it be \@maxdepth for the boxes having a completed column-page or page to cap the depth of the box. The macro \pcol@@makecol $\langle d \rangle$ also do that when $d = \mbox{maxdepth}$ but it can be d = 0 when it is invoked to build last page.
- splitmaxdepth is T_EX's primitive register to have the maximum depth of the vbox being the first half of a box being split. It is used in pcol@deferredfootins to cap the depth of the first half of deferred footnotes split from Φ , and in pcol@fntextbody to let it have the depth of strutbox.
- \prevdepth is TEX's primitive register to have the depth of the box which just has been added to a vertical list, or to be given to TEX's vertical list builder for the calculation of the vertical skip inserted below the last box. The macro \pcol@invokeoutput refers to it to save its value in \pcol@prevdepth before putting a dummy \vbox and making a \output request, and then let it have \pcol@prevdepth which is given by \output routine for the column that we resume. The macro \pcol@zparacol also refers to it to save it in \pcol@ firstprevdepth for the pre-environment stuff.
- vfuzz is T_EX's primitive register to have the threshold height of overfull messaging. It is set to 0 in pcol@ShowBox(b) to ensure overfull for any box b of non-null height.
- \maxdimen is a \dimen register to have 16383.99999pt being the largest legal dimensional value. The usages of this register are as follows.
 - For the \insert register set \pcol@colorins = Γ_r , \dimen\pcol@colorins is let be \maxdimen for the consistency with our intention that a column-page can have virtually infinite number of \insertions for text coloring.
 - In \pcol@output, it is set into \vsize when \outputpenalty = -10004 for the dummy \output request so that no page break should occur between the dummy and real requests.
 - Our own \dimen register \pcol@textfloatsep has \maxdimen if a column-page does not have synchronization points to let top floats are inserted in usual way. Therefore, \pcol@floatplacement and \pcol@zparacol let the register have \maxdimen as the initial value. Then the macros \pcol@makecol and \pcol@combinefloats examine if \pcol@textfloatsep = \maxdimen to determine the operation type of top float insertion, while \pcol@synccolumn does that to know if it is flushing a columnpage with a synchronization point or is setting the first synchronization point in the column-page. The macro \pcol@addflhd also examines it for the measurement of the combined height of top and bottom floats, while \pcol@measurecolumn gives it \maxdimen as its third argument for bottom floats.
 - The page context $\pi^h(p)$ has $-\mbox{maxdimen}$ if the page is a float page. The macro $\pcol@startpage$ makes that when it creates such a page.
 - Our own \colorevdepth and that saved in $\kappa_c(\delta)$ have \maxdimen if the main vertical list is empty at a synchronization. The macro \colorevdepth makes that when it finds an empty list.

- The column-context $\kappa_c(\rho_t)$ may have \maxdimen if the column c has a float column in the last page of a paracol environment and the floats in it can be put as top floats. The macro \pcol@makefcolumn makes this special assignment, and \pcol@ flushcolumn and \pcol@imakeflushedpage examine it.
- The macro \pcol@makefcolelt let the room for floats in a float page be -\maxdimen if it finds no further floats can be added to the page.
- At a synchronization, we measure the maximum combined size of top floats and the main vertical list V_T , that of footnotes and bottom floats V_B , that of four items V_P , and V'_P being V_P or $V_P + \texttt{textfloatsep}$ according to the existence of bottom floats. We also let D_T and D_P be the minimum depth of the column-pages which gives V_T and V'_P respectively. For the measurement, the macro pcol0sync lets $V_T = V_B = V_P = V'_P = -\texttt{maxdimen}$ and $D_T = D_P = \texttt{maxdimen}$ as their initial values. Then the macro pcol0synccolumn examines if $D_T = \texttt{maxdimen}$ to mean the synchronization point is set just below the top floats of a column whose main vertical list is empty. On the other hand, pcol0makeflushedpage and pcol0 output0end examine if $V'_P = -\texttt{maxdimen}$ to mean the last column-pages are empty.
- \linewidth is a \dimen register for an API parameter of LATEX to have the width of a line possibly shorter than \columnwidth in list-like environments. It is let have $w_c \mu$ by \pcol@invokeoutput for the outermost paragraphs in paracol environment, where $\mu =$ \pcol@lrmargin = \textwidth l which \pcol@zparacol lets have to represent the left-plus-right margin of the list-like environment, whose \linewidth is l, enclosing paracol if any. The macro \pcol@sptext also sets the register temporarily for spanning texts but letting it have \textwidth μ .
- \footnotesep is a \dimen register for an API parameter of LATEX to have the vertical space inserted in a footnote when it is split into two or more pages. It is used in \pcol@ fntextbody to \splittopskip have it, and to make the first line of the footnote is at least as tall as the amount in the register.
- **\topmargin** is a \dimen register for an API parameter of IATEX to have the width (height) of the top margin minus 1 inch. The register is used as an element of \pcol@bg@pagetop to calculate the distance from the origin at the left-top corner of text area to the top edge of a page. The other users are \pcol@ioutputelt and \pcol@makeflushedpage temporarily add the height-plus-depth of $\pi^b(p)$ to the register to make the calculation biased shifting the origin to the left-top corner of column area, i.e., below $\pi^b(p)$. The macro \Coutputpage also refers to the register together with \headheight and \headsep to calculate the distance from the page top (ignoring 1 inch shift) to the text area top.
- \oddsidemargin is a \dimen register for an API parameter of LATEX to have the width of the left margin minus 1 inch for two-sided odd-numbered pages and all single-sided pages. The register is used together with \evensidemargin in \pcol@outputpage@l, \pcol@ outputpage@r and \pcol@bg@swappage to decide the left margin of the page they are working on.
- \evensidemargin is a \dimen register for an API parameter of IATEX to have the width of the left margin minus 1 inch for two-sided even-numbered pages. The register is used together with \oddsidemargin in \pcol@outputpage@l, \pcol@outputpage@r and \pcol@bg@ swappage to decide the left margin of the page they are working on.
- \headheight is a \dimen register for an API parameter of LATEX to have the height of page headers. The register is used together with \topmargin and \headsep as an element

of \pcol@bg@pagetop and in \@outputpage to calculate the distance from the real and imaginary page top to the text area top respectively.

- \headsep is a \dimen register for an API parameter of LATEX to have the vertical distance from the bottom of a page header to the text area top. The register is used together with \topmargin and \headheight as an element of \pcol@bg@pagetop and in \@outputpage to calculate the distance from the real and imaginary page top to the text area top respectively.
- \textheight is a \dimen register for an API parameter of LATEX to have the height of text area in a page. The register is referred to by \pcol@output to examine if a page is very short, by \pcol@getpinfo, \pcol@startpage, \pcol@flushfloats and \pcol@output@ end to let \@colht be it for a page without spanning stuff (so far), by \pcol@outputelt, \@outputpage, \pcol@output@flush and \pcol@output@clear to build a page to be shipped out, by \pcol@bg@textheight to calculate H_T , and by \pcol@fntextbody to cap the height of a footnote.
- \textwidth is a \dimen register for an API parameter of IATEX to have the width of a page, which we occasionally refer to as W_T . The register is referred to by \pcol@ioutputelt, \pcol@imakeflushedpage and \pcol@iflushfloats to build a \hbox of \textwidth wide to have all columns (in a left or right parallel-page). It also referred to by following macros; \pcol@bg@swappage to calculate the right margin for mirrored background painting; \pcol@bg@@r, \pcol@bg@@f, \pcol@bg@@n, \pcol@bg@@p and \pcol@bg@@s to specify the width of background of page-wise stuff to be painted; \pcol@shiftspanning to calculate the left-shift amount of a spanning text in column-swapping; \pcol@addmarginpar to measure the distance between the right edges of the rightmost and current columns; \pcol@zparacol for the calculation of $\mu =$ \pcol@Irmargin; \pcol@setcolwidth@r for the calculation of w_c for all $c \in [0, C_L)$ or $c \in [C_L, C)$; \pcol@setcw@calcfactors for the calculation of W_T/W and $(W_T - W)/F$; \pcol@sptext, \footnoterule of paracol's local and \endparacol to set it in \columnwidth; and \pcol@fntextbody to set it in \hsize if page-wise footnote typesetting is in effect.
- \columnwidth is a \dimen register for an API parameter of LATEX to have the width of a column. The register is let have w_c by \pcol@getcurrcol for the column c, then is referred to by the following macros; \pcol@shiftspanning to calculate the left-shift amount of a spanning text in column-swapping; \pcol@addmarginpar to measure the distance between the right edges of the rightmost and current columns; \pcol@imakeflushedpage and \pcol@iflushfloats to put each column-page into a \hbox of w_c wide for shipping a page out; \pcol@invokeoutput to let \linewidth and \hsize have the value of or based on it; and \pcol@fntextbody to let \hsize have it for column-wise footnote typesetting. The register is also let have \textwidth by \footnoterule of paracol's local defined in \pcol@zparacol if page-wise footnote typesetting is in effect, by \pcol@sptext for spanning texts, and by \endparacol for post-environment stuff.
- **\columnsep** is a **\dimen** register for an API parameter of IAT_EX to have the width of columnseparating gaps. It is referred to by **\pcol@setcolwidth@r** to calculate w_c for all $c \in [0, C_L)$ or $c \in [C_L, C)$, and by **\pcol@setcw@getspec** as the default width of columnseparating gaps.
- \columnseprule is a \dimen register for an API parameter of IATEX to have the width of the rules to be drawn in column-separating gaps. It is referred to by \pcol@buildcolseprule and \pcol@buildcselt to draw the rule, and by \pcol@hfil to examine if it is positive

to mean the rule is really drawn and if so to add skips of $-\columnseprule/2$ to surround the rule to nullify the width of the rule.

- $\mbox{marginparwidth}$ is a \mbox{dimen} register for an API parameter of \mbox{IAT}_EX to have the width of a marginal note. It is temporarily modified by $\pcol@addmarginpar$ so that a left marginal note is placed appropriately.
- \marginparsep is a \dimen register for an API parameter of LATEX to have the distance between a marginal note and text area. It is temporarily modified by \pcol@addmarginpar so that a right marginal note is placed appropriately.
- \marginparpush is a \dimen register for an API parameter of $\[MTEX]$ to have the minimum vertical distance between two marginal notes. It is referred to by \pcol@addmarginpar to find a place for a marginal note and remember the place in $\pi^m(p)$.
- \paperheight is a \dimen register for an API parameter of $\square T_EX$ to have the height of physical pages H_P . It is referred to by \pcol@bg@paperheight to calculate $H_P 2W_R$.
- \paperwidth is a \dimen register for an API parameter of IAT_EX to have the width of physical pages W_P . It is referred to by \pcol@bg@swappage to calculate the right margin for mirrored background painting, and by \pcol@bg@paperwidth to calculate $W_P 2W_R$.
- \z@ is a \dimen register to have 0pt to initialize \pagerim, \belowfootnoteskip and \skip\pcol@colorins at their declarations, and is used in the following macros.

\pcol@ShowBox, \pcol@makecol, \pcol@combinefloats, \pcol@nextpelt, \pcol@floatplacement, \pcol@startpage, \pcol@restartcolumn, \pcol@outputelt, \pcol@buildcselt, \@outputpage, \pcol@startcolumn, \pcol@bg@paint@i, \pcol@bg@paintregion, \pcol@output@start, \pcol@putbackmvl, \pcol@iscancst, \pcol@deferredfootins, \pcol@combinefootins, \pcol@addmarginpar, \pcol@getmparbottom, \pcol@sync, \pcol@measurecolumn, \pcol@synccolumn, \pcol@makeflushedpage, \pcol@imakeflushedpage, \pcol@output@end, \pcol@invokeoutput, \pcol@setcolwidth@s, \pcol@setcw@calcfactors, \pcol@setcw@calcf, \pcol@extract@fil@ii, \pcol@sptext, \pcol@fntextbody. \pcol@marginpar, \pcol@icolumncolor, \pcol@set@color@push, \pcol@reset@color@pop, \pcol@reset@color@pop, \pcol@backgroundcolor@iii.

It is also used to give the number 0 for the initializations of \pcol@currcol, \pcol@ncol, \pcol@ncolleft and \count\pcol@colorins at their declarations, and in the following macros.

\pcol@ShowBox, \pcol@F@count, \pcol@makecol, \pcol@opcol, \pcol@setpnoelt, \pcol@nextpelt, \pcol@checkshipped, \pcol@getpelt, \pcol@outputelt, \pcol@ioutputelt, \@outputpage, \pcol@startcolumn, \pcol@output@start, \pcol@output@switch, \pcol@setcurrcol, \pcol@iscancst, \pcol@addmarginpar, \pcol@setmpbelt, \pcol@do@mpbout@i, \pcol@sync, \pcol@synccolumn, \pcol@makeflushedpage, \pcol@imakeflushedpage, \pcol@flushfloats, \pcol@iflushfloats, \pcol@freshpage, \pcol@output@end, \pcol@zparacol, \pcol@setcolwidth@r, \pcol@setcw@calcf, \pcol@synccounter, \pcol@com@syncallcounters, \pcol@stepcounter, \pcol@stpclelt, \pcol@com@switchcolumn, \pcol@switchcolumn, \pcol@sptext, \pcol@switchcol, \pcol@visitallcols, \pcol@xympar, \endparacol.

- \p@ is a \dimen register to have 1pt. It is used in \pcol@ShowBox, \pcol@cflt, \pcol@
 addflhd, \pcol@synccolumn, \pcol@output@end, \pcol@setcolwidth@s, \pcol@
 setcw@getspec@i, \pcol@setcw@fill and \pcol@setcw@calcf, and the top level as signment to \@tempskipa for the invocation of \pcol@defkw, as the shorthand of pt.
- \@totalleftmargin is a \dimen register to have the total size of the left margins of a list-like
 environment and those surrounding it. It is given to \parshape by \pcol@invokeoutput
 and \pcol@sptext if paracol is enclosed in a list-like environment.
- \@themargin is a control sequence \let-equal to \evensidemargin for two-sided even numbered pages or \oddsidemargin for others. In \pcol@outputpage@l and \pcol@ outputpage@r it is bound to one of \dimen registers for the references in \pcol@ outputpage@ev¹³⁰.
- \@maxdepth is a \dimen register to have \maxdepth at \begin{document} to recover the temporary update of \maxdepth with 0 by \@addtobot for bottom float incorporation in a page. As discussed in the explanation of \maxdepth, in paracol environments \maxdepth is let have \@maxdepth always by the assignments in \pcol@ output and \pcol@combinefloats. Other users, \pcol@cflt, \pcol@opcol, \pcol@ ioutputelt, \pcol@combinefootins, \pcol@output@flush and \pcol@output@clear, let \boxmaxdepth have \@maxdepth so as to limit the depth of boxes for a completed column-page or page to the value for page typesetting, while \pcol@flushcolumn and \pcol@imakeflushedpage do that by \pcol@makecol giving the register to it. The other usage of the register is to calculate background painting parameter H_T by \pcol@ bg@textheight, and to determine the bottom edge of the backgrounds of columns and column-separating gaps through the argument of \pcol@buildcolseprule given by \pcol@ioutputelt, \pcol@imakeflushedpage and \pcol@iflushfloats. The register is also referred to by \pcol@unvbox@cclv to go back the last baseline of the main vertical list in \box255, and by \pcol@deferredfootins to let \splitmaxdepth have its value to cap the depth of the first half of footnotes split from Φ .
- \@colht is a \dimen register to have the height of columns in a page possibly shrunk from \textheight by spanning stuff. The usages of the register are as follows.
 - In \pcol@startpage, \pcol@output@start, \pcol@flushfloats and \pcol@output@end, it is initialized to \textheight. In first two, the value of the register is reduced to reflect spanning stuff if exists and then set into $\pi^h(p)$, while the setting by the third is referred to by its callee \pcol@iflushfloats.
 - In \pcol@getpelt, \pcol@sync, \pcol@flushcolumn, \pcol@makeflushedpage and \pcol@imakeflushedpage, it is let have $\pi^h(p)$. In addition \pcol@sync examines if \@colht < $V_T + V_B + v(f)$, and \pcol@makefcolumn uses it to initialize the room of a float column as well as the height of $\kappa_c(\beta)$ for it.
 - In \pcol@opcol, it is used to add \pcol@clearcolorstack to the bottom of $\kappa_c(\beta)$ whose height is \@colht.

 $^{^{130}}$ The reference in \pcol@outputpage being IAT_EX's \@outputpage is done after the macro itself makes the assignment, which is of course consistent with those in our macros.

- In \pcol@startcolumn(*), \pcol@flushcolumn(*) and \pcol@freshpage, it is used to let \@colroom have it.
- In \pcol@restartcolumn(*), it is saved and restored for the use as the height cap of deferred footnote \insertion in \pcol@deferredfootins because it can be shrunk by the non-deferred page-wise footnotes.
- In \pcol@output@flush and \pcol@output@clear, it is given to \pcol@make flushedpage as its argument. The macro \pcol@makeflushedpage(*) lets \@colht be the argument if it is less than \@colht and thus is given by \pcol@output@end.

In addition, in the macros with '(*)' above and \pcol@makecol, the register is passed to \pcol@shrinkcolbyfn to shrink the height in it temporarily to keep the space required to put page-wise footnotes in the page they are working on, for the reference by starred macros themselves or \@makecol invoked in \pcol@makecol.

- \colroom is a \dimen register to have the height of a column possibly shrunk from \colht by top and bottom floats. The register is initialized to have \colht by $\col@$ startcolumn, $\col@output@start$, $\col@flushcolumn$ and $\col@freshpage$, the last three of which also save it into $\kappa_c(\beta^r)$. This save operation is also done by $\col@output@switch$ while restoring from it done by $\col@restartcolumn$, but the latter macro may shrink the amount in its callee $\col@putbackmvl$ to capture a spanning text while the former cancel this shrinkage. The macros $\col@output@ output@start$ also refer to this register to let \size have it in the former and to calculate the room for each column-page in the starting page in the latter. The macro $\col@output@ output@end lets$ the register have \textheight for the post-environment stuff because the column-pages above it simply precedes the stuff in the main vertical list. The other users $\col@makefcolumn$ and $\col@makefcolelt$ use this register to accumulate the total size of floats to be put in a float column temporarily.
- \@pageht is a \dimen register to be used in IATEX's \@specialoutput to have the height of \@holdpg. It is referred to by \pcol@addmarginpar to determine the position at which a marginal note is placed. We also use it as a scratchpad to have V_P in \pcol@sync and \pcol@measurecolumn, and to save $\pi^h(p_t)$ in \pcol@flushcolumn for the reference in itself, and to do so in \pcol@makeflushedpage for \pcol@imakeflushedpage.
- \@toproom is a \dimen register to have the room for top floats. The register is saved in $\kappa_c(\rho_t)$ by \pcol@setcurrcol and restored from it by \pcol@iigetcurrcol. The macro \pcol@makefcolumn uses this register as a flag to indicate that $\kappa_c(\lambda_t)$ of the column c having $\kappa_c(\rho_t) = \infty$ contains floats to be put in its last float column possibly as top floats so that it is examined by \pcol@flushcolumn and \pcol@imakeflushedpage, the former of which then lets $\kappa_c(\rho_t) = 0$ to mean the floats are put in a float column in a non-last page by the macro.
- \@botroom is a \dimen register to have the room for bottom floats. The register is saved in $\kappa_c(\rho_b)$ by \pcol@setcurrcol and restored from it by \pcol@iigetcurrcol.
- \@fpmin is a \dimen register to have \floatpagefraction × \@colht being the minimum total size of floats for which an ordinary (not flushed) float column can be build. It is referred

to by \pcol@makefcolumn as the threshold below which floats in the last float column can be put as top floats.

- \@mparbottom is a \dimen register to have the bottom position of the last \marginpar stuff. Its value at \begin{paracol} is referred to by \pcol@output@start to let M_L^l or M_L^r of $\pi^m(0)$ has an element based on it, while the tail of one of the lists in $\pi^m(p_t)$ defines the value at \end{paracol} which \pcol@output@end lets the register have. The register is also updated by \pcol@getmparbottom and \pcol@getmpbelt to let \pcol@ @addmarginpar being IATEX's original \@addmarginpar know the uppermost available position for the marginal note to be added. This update is, however, just for communication between these macros and thus is ineffective for typesetting posterior to that, as well as the update in \pcol@eaddmarginpar, because whole information for marginal note placement is kept in $\pi^m(p)$ in Π^+ .
- θ textfloatsheight is a \dimen register to have the combined height of mid floats and their separators. It is initialize to be 0 by \pcol@floatplacement, saved in $\kappa_c(\eta)$ by \pcol@ setcurrcol, and restored from it by \pcol@iigetcurrcol.

\dimen@ is a \dimen register for temporary use. It is used in the following macros.

- \pcol@buildcolseprule, \pcol@buildcselt@S and \pcol@buildcselt to have the argument $d \in \{ \text{Qmaxdepth}, 0 \}$ of the first macro.
- \pcol@bg@paintregion@i to have y_1 of $R_a^{[c]}$.
- \pcol@bias@mpbout@i{y}{t}{b} to have t and then t + y.
- \pcol@output@switch to have the height of pre-spanning-text stuff in \pcol@ prespan, or 0 if it is \perp .
- \pcol@sync to have V or $V D_T + V_E$.
- \pcol@addflhd and \pcol@hdflelt to measure the height of top and bottom floats, \pcol@makecol and \pcol@output@switch to measure the height of pre-spanningtext stuff including the top floats, and \pcol@measurecolumn for top and bottom floats and V_T , V_B and V_P .
- \pcol@setcolwidth@s and \pcol@setcw@accumwd to accumulate W being the sum of natural widths of column/gap specifications, and then used by \pcol@setcw@ calcfactors to calculate W/W_T and $W W_T$.

\dimen@ii is a \dimen register for temporary use. It is used in the following macros.

- \pcol@makecol to measure the total height of top floats by \pcol@addflhd.
- \pcol@bg@addext to have $e = pcol@bg@ext@.d.@.{a.@.c, a}$ and then 10000 pt -e to calculate an extension of background painting.
- \pcol@bias@mpbout@i{y}{t}{b} to have b and then b + y.
- \pcol@measurecolumn to measure V_T , V_P and D_P .
- \pcol@setcolwidth@s and \pcol@setcw@accumwd to accumulate F being the sum of infinite stretch factors in column/gap specifications with the unit of pt, and then used by \pcol@setcw@calcfactors to calculate $(W W_T)/F$, where W is the sum of natural widths.
- $\col@setcw@calcfactors to have (W W_T)/F$ above or 0 to be used in $\col@def@extract@fil@iii through \col@setcw@filunit made \let-equal to the register by <math>\col@setcolwidth@s$.

\@tempdima is a \dimen register for temporary use. The usages of this register are as follows.

- In $\colomatic pcolomatic pcolostart page, it is used to throw <math>\pi^h(p_t)$ away when we get it by $\cologet currpinfo$ because we don't need it.
- In \pcol@outputelt, it has $\pi^h(p)$ to examine if p is a float page.
- In \pcol@ioutputelt, it has $\pi^h(p)$ possibly shrunk by page-wise footnotes to know the backgrounds to be painted for columns etc. After that it has w_c being the width of each \hbox into which the column-page of each column c is put.
- In \pcol@buildcolseprule and its callees \pcol@buildcselt@S and \pcol@ buildcselt, the register has the first argument $H = \pi^h(p)$ of the caller macro.
- In \Coutputpage, it has the sum of \topmargin, \headheight and \headsep being the distance between tops of imaginary page and its text area.
- In \pcol@startcolumn, it is used to save \@colht which can be shrunk temporarily by page-wise footnotes.
- In \pcol@bg@paintregion@i, it is let have x_0 of $R_a^{[c]}$.
- In \pcol@output@start, it is used to have the room for each column-page in the starting page, and then the height-plus-depth of the pre-environment stuff.
- In \pcol@output@switch, it is used to throw π^h(p) away when we get it by \pcol@ getcurrpinfo because we don't need it.
- In \pcol@shiftspanning, it is let have the left-shift amount of a spanning text in column-swapping.
- In \pcol@restartcolumn, it is used to save \@colht which can be shrunk temporarily by page-wise footnotes.
- In \pcol@unvbox@cclv(*ins*), it has the depth of \box255 for going back to the baseline of the box, and then has the natural component of \skip(*ins*) to add its stretch and shrink components only.
- In \pcol@addmarginpar, at first it has the distance between left edges of the leftmost and current columns. Then it is let have the distance between top edges of the column and the marginal text to be put.
- In $\collected production \langle t \rangle \langle h \rangle$ and $\collected product \langle t_i \rangle \langle b_i \rangle$, it at first has t and then is let have b_i when the marginal note cannot be put at t.
- In $\col@sync, \col@measurecolumn and \pcol@synccolumn, it has <math>V_T$ being the maximum combined height of top floats and the main vertical list.
- In \pcol@makefcolumn and \pcol@makefcolelt, it has the room for floats to be put in a float column.
- In \pcol@makeflushedpage, it has the height-plus-depth of spanning stuffin $\pi^i(p_t)$.
- In \pcol@output@end, at first it is let have $V'_P H$, where H is the height(-plusdepth) of \@outputbox having the ship-out image of the last page, being the negative counterpart of the height-plus-depth of spanning stuff in the last page for setting \mathcal{M} , and then have H to be set in \pcol@bg@preposttop for the background painting of post-environment stuff.
- In \pcol@setcolwidth@r, it has \textwidth $-(C^1 C^0 1)$ \columnsep being the base of w_c .

- In \pcol@setcw@getspec@i, it is let have the natural width of a column/gap specification, to be used in \pcol@setcolwidth@s, \pcol@setcw@accumwd and \pcol@ setcw@set, while in the last of them it finally has w_c or g_c .
- In \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$, at first it has y, then $y/2^{k_2}$, and then $\lceil y/2^{k_2+k_3} \rceil$, where k_2 and k_3 are scaling parameters for good approximation.
- In \pcol@switchcol, it is let have what \pcol@ensurevspace has so that the dimensional expression in it is evaluated in the macro and the evaluation result is assigned to $V_E =$ \pcol@@ensurevspace.
- In \ensurevspace{space}, it is let have $\langle space \rangle$ to ensure the argument is a dimension including forced one.
- In \pcol@fntextbody, it has the height-plus-depth of the \vbox in which the footnote is encapsulated.
- In \pcol@set@color@push, it has the width of the \vbox to be \inserted, which is m sp for a math-mode push of γ_{i,m} or 0 for a non-math one γ_i.
- In \pcol@bg@defext{d}{e}, it is let have e to confirm e is a proper dimension.

\Otempdimb is a \dimen register for temporary use. The usages of this register are as follows.

- In \pcol@makecol, it is used to measure the height-plus-depth h_i of decapsulated \box255 and its original form to add an element $span(H_i, h_i)$ to $\pi^s(p_t)$ for a spanning text captured in the box.
- In \pcol@ioutputelt, if has the height-plus-depth of spanning stuff $\pi^b(q)$ to be temporarily added to \topmargin.
- In \pcol@buildcolseprule it has H_0+h_0 , while in its callee \pcol@buildcselt $\langle H_i \rangle$ $\langle h_i \rangle$ it has $H_{i-1} + h_{i-1}$ and then $H_i + h_i$ where $span(H_i, h_i) \in \pi^s(p)$.
- In \pcol@bg@paintregion@i, it is let have y_0 of $R_a^{[c]}$.
- In \pcol@output@switch, it is let have the height-plus-depth h_i of \@holdpg having a spanning text to add an element $span(H_i, h_i)$ to $\pi^s(p_t)$.
- In \pcol@shrinkcolbyfn, it is let have the inverse of the \skip component of the argument \insert register of the macro, so that in \pcol@startcolumn and \pcol@restartcolumn it has that of $\pi^f(p)$ if p has page-wise footnotes, or 0 otherwise, and then is referred to by \pcol@deferredfootins which then lets the register have the height cap of Φ splitting.
- In \pcol@addmarginpar, \pcol@getmparbottom and \pcol@getmpbelt, it is let have the vertical space to be occupied by the marginal text to be put, being the second argument of \pcol@getmparbottom.
- In \pcol@sync and \pcol@measurecolumn, it has V_B and then, in the former, it has $V_P + v(f)$, V_T or $V_T + V_B + v(f)$ according to the contents of the page to be synchronized.
- In \pcol@makefcolelt, it has the size of vertical space consumed by a float.
- In \pcol@synccolumn, it has $V_T v_c(t)$ being the vertical space from the bottom of $\kappa_c(\beta^b)$ to the synchronization point. If the synchronization point is defined by a column without main vertical list but with top floats, then the register is let have $V_T v_c(t) + \text{textfloatsep} \text{loatsep} + 10000 \text{ pt}$ to be set in $\kappa_c(\xi) = \text{pcol@textfloatsep}$ as the space below the MVL-float biased by 10000 pt to indicate the last float is the MVL-float.

- In \pcol@setcolwidth@r, it has \textwidth $-(C^1 C^0 1)$ \columnsep $-\sum_{d=0}^{k-1} w_d$ being the base of w_c for $c \in [C^0+k, C^1)$ where k is the number of fractions given in the argument of \columnratio.
- In \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$, at first it is let have x, then $x \cdot 2^{k_1}$, then $z' = \lfloor (x \cdot 2^{k_1}) / \lceil y/2^{k_2+k_3} \rceil \rfloor$, and finally $Z = z \times 1 \text{ pt} = z' \cdot 2^{16-k}$ referred to by \pcol@ setcw@calcfactors as $\phi_f = (W_T W)/F$, where k_1, k_2 and k_3 are scaling parameters for good approximation and $k = k_1 + k_2 + k_3$.
- In \pcol@extract@fil@ii and \pcol@extract@fil@iii, it is let have the infinite stretch factor of a column/gap specification represented with the unit \pcol@setcw@ filunit, to be used in \pcol@setcolwidth@s, \pcol@setcw@accumwd, and \pcol@ setcw@set.
- In \pcol@fntextbody, it has \textheight \skip\footins as the cap of the footnote.

\Ctempdimc is a \dimen register for temporary use. It is let have values as follows.

- $H_i (H_{i-1} + h_{i-1})$ in \pcol@buildcselt $\langle H_i \rangle \langle h_i \rangle$.
- x_1 of $R_a^{[c]}$ in \pcol@bg@paintregion@i.
- t + h in \pcol@getmparbottom $\langle t \rangle \langle h \rangle$.
- $\max(t, b_{i-1}) + h$ in \pcol@getmpbelt $\langle t_i \rangle \langle b_i \rangle$ invoked from \pcol@getmparbottom $\langle t \rangle \langle h \rangle$.
- D_T in \pcol@sync, \pcol@measurecolumn and \pcol@synccolumn.
- \floatsep or \@fpsep in \pcol@makefcolumn and \pcol@makefcolelt.
- w_c being the width of column c in \pcol@setcolwidth@r.
- $W_T W$ in \pcol@setcw@calcfactors.
- At first for calculation of $y/2^{k_2}$ and then $z'/2^k \approx x/y$ in \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$ where k_2 and k are scaling parameters for good approximation.

2.1.4 Skip Registers

- \baselineskip is TEX's primitive register to have the vertical skip to separate adjacent baselines. It is referred to by \pcol@output and \pcol@output@start to examine if \@colroom is unexpectedly small, and by \pcol@switchcol to give it to \ensurevspace to let \pcol@ensurevspace have the default value.
- **\topskip** is T_EX's primitive register to have the vertical skip from the top edge of a page to the baseline of its first vertical item. It is let be 0 by \pcol@output@start if we have pre-environment stuff and is saved in $\pi^t(0)$, while \pcol@startpage lets it be \pcol@ topskip, into which \pcol@zparacol saves the value outside paracol environment, saving the value in $\pi^t(p)$. Then the register is restored from $\pi^t(p)$ by \pcol@getpelt and \pcol@sync, while \pcol@synccolumn refers to the value restored by the latter to adjust a synchronization point. The macro \pcol@putbackmvl lets the register have 0 when it starts a spanning text because it originally follows pre-spanning-text stuff in the column-page to be restarted rather than at the page top. The macro \pcol@output@end temporarily lets the register have 0 if we have non-empty columns in the last page, while \endparacol restores it from \pcol@topskip for the pages outside paracol environment.

- splittopskip is T_EX's primitive register to have the vertical skip inserted at the beginning of the second half of the box split by vsplit or T_EX's internal operation for splitting an insert at a page break. The register is temporarily let have 0 by pcol@deferredfootins when it splits Φ so that the second half does not have any skip at the top. The register is also let have footnotesep in pcol@fntextbody for footnote typesetting.
- \parskip is TEX's primitive register to have the vertical skip inserted above each paragraph. It is referred to by \pcol@zparacol to nullify the insertion going to be made by the first \item of a list-like environment, when the macro finds the paracol environment to start is at the very beginning of a list-like environment.
- \fill is an API \skip register to have a skip 0pt plus 1fill. In our macros, however, it is used as a keyword in \pcol@setcw@getspec, \pcol@setcw@getspec@i and \pcol@ setcw@fill to extract the infinite stretch factor f given as f\fill in the specification.
- \itemsep is an API \skip register to have the vertical skip inserted above each non-first \item
 in list-like environments. It is referred to by \pcol@zparacol to nullify the insertion
 going to be made by the first \item of a list-like environment, when the macro finds
 the paracol environment to start is at the very beginning of a list-like environment.
- \floatsep is an API \skip register to have the vertical skip between adjacent floats. It is referred to by \pcol@cflt to cancel the skip following the last float, by \pcol@makefcolumn to let \pcol@makefcolelt examine the capacity of a float column in the last page, by \pcol@addflhd and \pcol@hdflelt to measure the total height of top and bottom floats, and by \pcol@sync to calculate the space below the MVL-float.
- \dblfloatsep is an API \skip register to have the vertical skip between adjacent page-wise floats, and is used in \pcol@startpage to cancel the skip below the last float.
- \dbltextfloatsep is an API \skip register to have the vertical skip between the last pagewise float and the top of columns, and is used in \pcol@startpage to put the skip.
- \@topsep is a \skip register to have the vertical skip inserted above the first \item of a listlike environment. The actual value is determined by \@trivlist from API parameters \topsep, \partopsep and \parskip depending on how the environment appears. The skip in the register is inserted by \pcol@zparacol when it finds the paracol environment to start is at the very beginning of a list-like environment.
- \@fptop is a \skip register to have the vertical skip inserted at the top of a float column, and is used in \pcol@makefcolpage.
- \@fpsep is a \skip register to have the vertical skip between adjacent floats in a float column, and is used in \pcol@makefcolpage.

\@fpbot is a \skip register to have the vertical skip inserted at the bottom of a float column, and is used in \pcol@makefcolpage.

\Ctempskipa is a \skip register for temporary use. It is used in the following macros.

- \pcol@makecol, \pcol@startpage, \pcol@outputelt, \pcol@output@switch, \pcol@flushcolumn and \pcol@makeflushedpage to throw $\pi^t(p)$ away because we don't need it.
- \pcol@output@start to determine \topskip for the starting page.
- \pcol@setcw@getspec@i and \pcol@setcw@fill to have the width specification of a column or gap.

It is also used in the top level invocation of \pcol@defkw with a glue of 0 pt plus 1 fil minus 1 fil.

2.1.5 Box Registers

- \strutbox is an API \box register to have the strut for the current font size. It is used in \pcol@fntextbody{text} to let \splitmaxdepth have its depth, and to let the last line of the footnote (text) have its depth at shallowest.
- $\climits box register but TEX defines that it has the main vertical list when <math>\up t$ routine is invoked. It is referred to by $\col@makecol when it has a broken spanning text to measure its height-plus-depth for the element to be added to <math>\pi^s(p_t)$ and to update it combining its contents with pre-spanning-text stuff optionally shifting it left by passing the register to $\col@shiftspanning$. The macro also uses the register together with its callee $\col@unvbox@cclv to add stretch/shrink factor of <math>\skip\footins at its bottom for a column-page in a page having page-wise footnotes. The macro <math>\col@makenormalcol, \col@invokeoutput$. The other users $\col@output@start, \col@makenormalcol, \col@flushcolumn and <math>\col@imakeflushedpage$ let the register have the main vertical list of pre-environment stuff or a column to be passed to $\makecol, and \col@ flushcolumn also takes care the skip above page-wise footnotes.$
- $\$ always. It is used to initialize $\$ and $\$ always. It is used to initialize $\$ and $\$ and $\$ always. It is used to initialize $\$ by the following macros.
 - \pcol@makecol to make \pcol@currfoot void unless page-wise footnotes in \foot ins is saved into π^f(p).
 - \pcol@startpage to let πⁱ(p_t) = ⊥ if the new top page does not have spanning stuff and π^f(p_t) = ⊥ for all float pages and the new top page.
 - \pcol@outputelt to initialize \@outputbox.
 - \pcol@ioutputelt to examine if S_c is empty.
 - \pcol@output@start to let $\pi^f(0) = \bot$, and $\gamma_0^c = \bot$ if $\hat{\gamma}_0^c$ is undefined.
 - \pcol@output@switch to let $\kappa_c(\tau^b) = \bot$ if the column does not have column-wise footnotes.
 - \pcol@getcurrfoot to let \footins be void if so.
 - \pcol@setcurrcolnf to let $\kappa_c(\tau^b) = \bot$ because the column *c* does not have columnwise footnotes.

- \pcol@putbackmvl to let \pcol@prespan = \perp if a spanning text really starts from the top of a column-page, and $\Gamma_s = \perp$ if the column-page $\kappa_c(\beta)$ to be restarted is non-empty.
- \pcol@savecolorstack to let $\Gamma_s = \bot$ or its first item be \bot if Γ^c or γ_0^c is \bot , respectively.
- \pcol@savefootins to let its argument macro have a void box if \@freelist is exhausted.
- \pcol@makeflushedpage to initialize \@outputbox and \pcol@rightpage to be \perp if the flushed page does not have spanning stuff, and to let $\pi^f(p_t) = \perp$ after putting it in the last page so that \pcol@output@end will be unaware of the page-wise and non-merged footnotes.
- \pcol@flushfloats to let \pcol@rightpage = \perp if parallel-paging is not in effect.
- \pcol@output@end to let \pcol@rightpage = \perp if the last page has nothing other than spanning stuff being page-wise floats and thus we don't have the right parallelpage. The macro also lets $\gamma_0^c = \perp$ for all c and $\Gamma = \perp$.
- \pcol@com@flushpage and \pcol@com@clearpage gives the void box to \pcol@ flushclear as its argument to mean these macros are only aware of \ifpcol@flush as the result of pre-flushing column height check. The macro \endparacol also does that if the footnote typesetting is merged.
- \Choldpg is a \box register to have the main vertical list when \output is invoked with a special \penalty code. It is let have that by \pcolOspecialoutput, and is referred to by \pcolOoutputOstart and \pcolOmakenormalcol for pre-environment stuff, and by \pcolOoutputOswitch for the column from which we are leaving.
- \Coutputbox is a \box register to have a partial or the complete ship-out image of a column or a page. The usages of the register are as follows.
 - In \pcol@@makecol, it has a column-page made by \@makecol for \pcol@flush column and \pcol@imakeflushedpage.
 - In \pcol@combinefloats, it has a column-page to which top and bottom floats are combined.
 - In \pcol@cflt, it has a column-page to which top floats are combined.
 - In \pcol@opcol, it has the complete column-page built by \@makecol.
 - In \pcol@startpage, it has the complete float page built by \@tryfcolumn.
 - In \pcol@outputelt, it has the complete (left parallel-) page to be shipped out by \@outputpage.
 - In \pcol@outputpage@r, it is temporarily made \let-equal to \pcol@rightpage so that the box is shipped out by \pcol@@outputpage being LATEX's \@outputpage instead of the real \@outputbox.
 - In \pcol@output@start, it has the pre-environment stuff built by \pcol@ makenormalcol.
 - In \pcol@combinefootins, it is let have the pre-environment stuff with footnotes.
 - In \pcol@flushcolumn, it has a flushed column-page built by \@makecol or a float column built by \@makefcolumn.

- In \pcol@output@flush and \pcol@output@clear, it has a flushed page built by \pcol@makeflushedpage and \pcol@imakeflushedpage in which it has each of flushed column-page built by \@makecol.
- In \pcol@flushfloats, it has the complete (left parallel) page for flushed float columns.
- In \pcol@iflushfloats, it has a float column built by \pcol@makefcolumn.
- In \pcol@output@end, it has the ship-out image of the last page of a paracol environment built by \pcol@makeflushedpage and \pcol@imakeflushedpage.

\@tempboxa is a \box register for temporary use. The usages of the register are as follows.

- In \pcol@makecol, it is used to decapsulate \box255 containing a broken spanning text. In the macro and \pcol@output@switch, it is also used as a waste basket to make \footins void when it contains page-wise footnotes in a non-top page.
- In \pcol@cflt and \pcol@startpage, it has top column-/page-wise floats combined by the application of \@comflelt/\@comdblflelt to \@toplist/\@dbltoplist respectively.
- In $\colorbantom\langle b \rangle$, it has an empty box whose height and depth are equal to those of the argument box b.
- By \pcol@buildcolseprule and its callees \pcol@buildcselt@S and \pcol@ buildcselt, it is let have the painted backgrounds for columns, column-separating gaps and spanning texts in a page, and then is put into the ship-out image of the page by \pcol@ioutputelt, \pcol@imakeflushedpage or \pcol@iflushfloats.
- In \Coutputpage, it is let have the painted background of the right page referred to by its callee \pcolCoutputpageOr.
- In \pcol@bg@paint@i{body}, it is let have painted backgrounds built by $\langle body \rangle$.
- In \pcol@bg@paintregion $\langle a \rangle \langle c \rangle$, it is let have painted background of the region $R_a^{[c]}$.
- In \pcol@specialoutput, it is used to discard the dummy \vbox put by \pcol@ invokeoutput.
- In \pcol@makenormalcol, it is used to save \footins into it and make it ⊥ temporarily to exclude merged footnotes from spanning stuff for pre-environment stuff.
- In $\collinewidth{pcollinewidthen} \langle box \rangle \langle then \rangle \langle else \rangle$, it is used to examine if $\langle box \rangle$ is empty.
- In \pcol@scancst(box) and \pcol@iscancst, it is used to have what Γ or Γ_s has after the scan of $\langle box \rangle \in \{\Gamma, \Gamma_s\}$.
- In \pcol@savecolorstack, it is used to have the \vbox for γ₀^c to be placed at the top of Γ_s.
- In \pcol@deferredfootins, it is used to have the first half split from Φ being the deferred footnotes to be \inserted.
- In \collectrony{text} , it is used to encapsulate $\langle text \rangle$ in it.
- In \pcol@icolumncolor, it is used to have a \vbox to be \inserted for the update of γ₀^c.
- In \pcol@set@color@push, it is used to have a \vbox to be \inserted to push γ_i or γ_{i,m} to Γ_r.
- In \pcol@reset@color@pop and \pcol@reset@color@mpop, it is used to have a \vbox to be \inserted to add γ_i⁻ or γ_{i,m}⁻ to Γ_r.

2.1.6 Token Registers

- \output is T_EX 's primitive to have \output routine. It is let have \pcol@output as its sole token by \pcol@zparacol.
- \everypar is TEX's primitive to have tokens inserted at the beginning of each paragraph. In \pcol@sptext and \pcol@com@endcolumn, it is \globalized to keep its contents after the end of a group. In \pcol@output@switch, its contents are broadcasted to $\kappa_c(\varepsilon)$ for all $c \in [0, C)$ if columns are synchronized with a spanning text. Then these values or that simply given in a column are saved into $\kappa_c(\varepsilon)$ by \pcol@setcurrcol, and then restored from it by \pcol@iigetcurrcol.
- \everyvbox is TEX's primitive to have tokens inserted at the beginning of each \vbox. In \pcol@zparacol, after tokens in it are saved into \pcol@everyvbox, it is let have a \therefore reference to \pcol@everyvbox and \pcol@innertrue to turn \ifpcol@inner = true, and then the register itself is made \let-equal to \pcol@everyvbox. In addition, it is let have tokens in \pcol@everyvbox if a \global assignment to the register is made in the paracol just having been closed. Another usage of this register is to insert a painted page background to the \vbox to be \shipout by \pcol@outputpage@l and \pcol@ outputpage@l, and is used for this purpose by \pcol@outputpage@l and \pcol@ outputpage@r, and by \pcol@outputpage@ev to nullify this special function for other inside \vboxes.
- \@temptokena is a \toks register for temporary use. It is used in \pcol@output@switch to broadcast \everypar to $\kappa_c(\varepsilon)$ for all $c \in [0, C)$.

2.1.7 Switches

- \if@twocolumn is a switch to be *true* iff multi-column pages are being typeset. It is turned *true* by \pcol@zparacol, and then turned *false* by \endparacol. In addition, it is turned *false* when \pcol@output finds that the \output request for a page break outside paracol is sneaked into our own \output routine, in order to avoid that LATEX's original \output routine misunderstands it is working on a two-columned document. The switch is examined by LATEX's own macros including old \end@dblfloat kept in our own \pcol@ end@dblfloat. It is also examined by \pcol@zparacol before being turned *true* to ensure it is *false* or to complain about the inappropriateness otherwise.
- \if@firstcolumn is a switch to be true iff the first column is being typeset. Its truth
 value is determined by \pcol@addmarginpar to tell \pcol@addmarginpar, \pcol@
 getmparbottom@i and \pcol@setmpbelt@i the margin which a marginal note goes to.
- \if@twoside is a switch to be true iff two-sided page typesetting is in effect and thus even numbered page may have their own left margins, headers and footers different from those for odd numbered pages. Besides the initialization by the main class file such as article.cls according to the class option twoside, the switch is \globally turned false by \pcol@ twosided for the case in which API macro \twosided does not have 'p' in its optional argument, and then \globally turned true by \pcol@twosided@p which is invoked when the argument contains 'p', or the API macro does not have the argument at all. Then the switch is referred to by \pcol@outputpage@l, \pcol@outputpage@r and \pcol@bg@ swappage to decide the left margin of even numbered pages, i.e., \evensidemargin if the switch is true or \oddsidemargin otherwise. The switch is also referred to by \pcol@ com@cleardoublepage to have a blank page if the switch is true and the command \cleardoublepage is used in an odd-numbered page.

- \if@reversemargin is a switch to be *true* iff \reversemarginpar is specified to reverse the side which marginal notes go to. It is examined by \pcol@addmarginpar as a factor to decide the margin which a marginal note goes to, and by \pcol@do@mpbout@i for the same purpose but for marginal notes in pre-environment or post-environment stuff.
- \if@mparswitch is a switch to be true iff it is specified by, for example, twoside option of a
 class such as article, that marginal notes in even numbered pages go to the left margin.
 It is examined by \pcol@do@mpbout@i as a factor to decide the margin which a marginal
 note goes to in pre-environment or post-environment stuff.
- \if@nobreak is a switch to be *true* iff the last paragraph is for a sectioning command. The switch is saved into $\kappa_c(\sigma)$ together with \if@afterindent by \pcol@setcurrcol, and then restored from it by \pcol@igetcurrcol. The macro \pcol@output@switch refers to it to broadcast its value set by a spanning text to $\kappa_c(\sigma)$ for all $c \in [0, C)$, while \pcol@output@start and \pcol@restartcolumn insert \penalty = 10000 by \nobreak if the switch is *true*. This conditional \nobreak is also done by \pcol@icolumncolor, \pcol@set@color@push, \pcol@reset@color@pop and \pcol@reset@color@mpop to avoid a break after an \insert. The macro \pcol@zparacol also examines the switch, but with the truth value in it given outside paracol environment, to invoke \@nbitem if *true* when the macro finds the paracol environment to start is at the very beginning of a list-like environment.
- \if@newlist is a switch to be *true* in the duration after a list-like environment starts and until its first \item appears. The switch is examined by \pcol@zparacol to know if the paracol environment to start is at the very beginning of a list-like environment and, if so, is turned *false* by the macro after it inserts vertical skips pretending the first \item is given.
- \if@inlabel is a switch to be true in the duration after an \item appears and until its
 first paragraph is given. The switch is examined by \pcol@zparacol together with
 \if@newlist to know if the paracol environment to start is at the very beginning of a
 list-like environment (false) and not trivlist-like one (true).
- \if@afterindent is a switch to be *true* iff a sectioning command tells that the first paragraph following it is to be indented. The switch is saved into $\kappa_c(\sigma)$ together with \if@nobreak by \pcol@setcurrcol, and then restored from it by \pcol@iigetcurrcol. The macro \pcol@output@switch refers to it to broadcast its value set by a spanning text to $\kappa_c(\sigma)$ for all $c \in [0, C)$.
- $\label{eq:lighted_li$

\if@tempswa is a switch for temporary use. The usages of the switch are as follows.

- In \pcol@checkshipped, it is turned *true* iff S_c for all $c \in [0, C)$ have column-pages to be shipped out, and then it is examined by \pcol@opcol.
- In \pcol@nextpage and \pcol@nextpelt, it is *true* until \pcol@nextpelt finds the first q such that q > p and $\pi^h(q) \ge 0$ to mean q is not for a float page, so that we let p = q to skip float pages following to the old p if any.
- In \pcol@outputcolumns and \pcol@outputelt, it is *true* until \pcol@outputelt finds the first q such that $q \ge p_b$ and $\pi^h(q) \ge 0$ to mean q is not for a float page, and the argument of \pcol@outputcolumns is 0 to mean that it is not for page flushing, so that we ship out q and all float pages following it if any.
- In \Coutputpage it is let have the value of \ifpcol@bg@painted indicating if background painting for the left page is done, and then it is examined by \pcol@ outputpage@l to determine whether the background is put into the final ship-out image.
- In \pcol@makenormalcol, it is *true* iff the footnotes in pre-environment stuff is included in \@outputbox which the macro builds.
- In \pcol@output@switch, at first it holds \if@nobreak of the spanning text if columns are synchronized with it to broadcast \if@nobreak to all $\kappa_c(\sigma)$. Then it is turned *true* iff \ifpcol@sync = *true* for synchronization or \ifpcol@clear = *true* for flushing, so as to invoke \pcol@sync. And finally, it is turned *true* iff \ifpcol@clear = *false* or \ifpcol@sync = *true*, so as to invoke \pcol@ restartcolumn.
- In \pcol@restartcolumn, it is turned *true* iff footnote typesetting is page-wise and $p < p_t$.
- In \pcol@scancst, it is initialized to be *true*. Then it is referred to by \pcol@ iscancst for each $\gamma \in \Gamma_r$ to update γ_0^c and then turned *false* when the first one is found.
- In \pcol@savecolorstack, it is true iff either Γ ≠ ⊥ or γ₀^c ≠ ⊥, i.e., Γ^c to be saved is not ⊥.
- In \pcol@getmparbottom, it is initialized to be *false* and then may be turned *true* by \pcol@getmpbelt if it finds a gap between two marginal notes to accommodate that to be added, and then examined by \pcol@getmparbottom to know the fact.
- In \pcol@sync, it is turned *true* iff the synchronized or flushed page can be built by \pcol@synccolumn.
- In \pcol@makefcolumn having non-empty $\kappa_c(\lambda_t)$, it is turned false iff the macro is acting on a column in the last page, $\kappa_c(\lambda_d)$ is emptied by the macro itself, and the total size of the floats to be put in the float column being built by the macro is less than \@fpmin, to mean it is possible that the floats in $\kappa_c(\lambda_t)$ is put in the float column as top floats.
- In \collemeasurecolumn and \collemedfield , it is set to be *false* iff both top floats and the main vertical list are empty, so that \collemeasureupdate examines it for the update of V_T and D_T . Then it is kept *false* iff both of footnotes and bottom floats are empty, so that \collemeasurecolumn examines it for the update of V_P and \collemeasureupdate does for V'_P and D_P .
- In \pcol@makeflushedpage, it is made false iff p_t is the last page, $V'_P = -\infty$ to mean all columns are empty and $\pi^f(p_t) = \bot$, so as to make the spanning stuff in $\pi^i(p_t)$ a float in post-environment stuff if \ifpcol@dfloats also false. Then it is

kept false if $\filt coll dfloats = false$ or $\pi^i(p_t) = \bot$ to mean nothing is shipped out for last page. Then it is made false iff p_t is the last page without deferred floats and merged footnote typesetting is in effect, i.e., the switch is *true* iff page-wise footnotes are put in the page to be flushed.

- In \pcol@imakeflushedpage, it is turned true iff $\kappa_c(\rho_t) = \infty$ and $V'_P = \pi^h(p_t)$ to mean the floats in $\kappa_c(\lambda_t)$ should be put in a float column in the last page as usual.
- In \pcol@iflushfloats, it is turned *true* iff one or more columns have non-empty $\kappa_c(\lambda_d)$ after shipping a page for float columns out, so that \if@fcolmade is let have its value after scanning all columns.
- In \pcol@output@end, it is turned *true* iff we built float columns, or the main vertical list in the last page is empty and the page is not the starting page, so that we create a new page for the post-environment stuff.
- In \globalcounter{ctr}, it is turned true iff $\langle ctr \rangle \in \Theta^g$ already.
- In $\constraints defined true iff <math>\theta$ is not in Θ_0 or $val(\theta) \neq val_0(\theta)$, so that θ is added to $\constraints defined the list of local counters to be synchronized.$
- In \pcol@switchcolumn[d], it is turned false iff 0 ≤ d < C so that we complain c is invalid if the switch is true.
- In \pcol@ac@caption@def $\langle s \rangle \langle t \rangle$, \@tempswatrue or \@tempswafalse is given as its first argument s by \pcol@ac@caption@enable or \pcol@ac@caption@disable respectively, so that \if@ac@caption@if@.t is made \let-equal to s and \pcol@ac@ caption examines it for enabling/disabling \addcontentsline respectively. The macros \pcol@ac@caption@if@lof and \pcol@ac@caption@if@lot are initialized to be \let-equal to \@tempswatrue as the default.
- In \pcol@icolumncolor, it is turned *true* iff we are in a \vbox or in restricted horizontal or math mode.
- In \pcol@backgroundcolor@i, it is examined if the root of the invocation chain is \backgroundcolor which turns the switch *true*, or \nobackgroundcolor which turns it *false*, to determine whether the background of a region is painted or not.

2.2 Macros

2.2.1 Procedural Macros

- \par is T_EX's primitive to end/start paragraphs, but may be modified by LAT_EX to have some special functionality occasionally. The macro \pcol@output makes it \let-equal to \@@par in which the T_EX's original definition is kept, while \pcol@zparacol and \pcol@ par use it as is.
- \space is an API macro to have a space token. It is used in \pcol@output, \pcol@
 icolumncolor, \pcol@defcseprulecolor@i and \pcol@backgroundcolor@ii for warn ing messages, and in \pcol@def@extract@fil to \define the macro \pcol@extract@fil
 having spaces in its argument specification.
- \nointerlineskip is an API macro to let \prevdepth = -1000 pt to inhibit TEX's baseline progress mechanism. It is used in \pcol@ioutputelt, \pcol@makeflushedpage and \pcol@imakeflushedpage to joint boxes without \baselineskip between them, in \pcol@outputpage@ev to suppress the \baselineskip insertion after the first box of painted background in the final ship-out image, and in \pcol@bg@paint@i for the same purpose for the box having painted backgrounds.

- \offinterlineskip is an API macro to let \baselineskip = -1000 pt, \lineskip = 0
 and \lineskiplimit = \maxdimen to suppress \baselineskip insertion for all boxes
 following this macro. It is used in \pcol@bg@paint@i to do that in the box in which
 painted backgrounds are built.
- \thepage is an API macro to have the representation of the counter page. It is used in \pcol@ output for a warning message.
- $\label{eq:linear} $$ \theta = \theta = \theta^{-1} -$
- $\text{stepcounter}\langle\theta\rangle$ is an API macro to increment the counter θ and zero-clear its descendant counters. It is used in $\col@startpage$ for the counter page, and in $\col@startpage$ for the counter page, and in $\col@startpage$.
- \nobreak is an API macro to insert \penalty = 10000 to inhibit line or page breaks. It
 is used in \pcol@output@start, \pcol@restartcolumn, \pcol@icolumncolor, \pcol@
 set@color@push, \pcol@reset@color@pop and \pcol@reset@color@mpop to meet the
 page-break inhibition request made by \if@nobreak = true.
- $\label{eq:penly} $$ an API macro to insert a page break \penalty = \langle pen \rangle$ if \ifOnobreak = false. The \penalty is inserted removing the last vertical skip which is reinserted after the \penalty. The macro is used in \pcolOoutputOstart and \pcolOrestartcolumn to insert \interlinepenalty if \ifOnobreak = false, while \pcolOzparacol uses it to insert \Obeginparpenalty when it finds the paracol environment to start is at the very beginning of a list-like environment.$
- \footnotesize is an API macro to set the font size for footnotes. It is used in \pcol@ fntextbody for footnote typesetting.
- $[r]{w}{h}$ is an API macro to draw a vertical rule of w width and h tall, optionally raised by r. It is used in pcol@fntextbody to have the rule of w = r = 0 and h = footnotesep to make the first line of the footnote is at least as tall as footnotesep.
- \addcontentsline(file)(sec)(entry) is an API macro to put \addtocontents for the arguments to .aux file. The original definition of the macro is kept in \pcol@addcontentsline so that \pcol@ac@disable@toc and \pcol@ac@caption make the macro regain its original definition after temporarily disabling its function by making it \let-equal to \pcol@ gobblethree.
- $\mbox{marginpar[left]{right}}$ is an API macro to put marginal note $\langle left \rangle$ or $\langle right \rangle$ to the left or right margin. In \clicklent is made $\let-equal$ to \clicklent for the emulation of $\mbox{marginnote}$, while its original version is kept in \clicklent is \clicklent .

- $\text\$ is an API macro to give a footnote $\langle text \rangle$ optionally with its number $\langle num \rangle$. In \colorparacol it is made $\let-equal$ to $\colorparacol \circ$ in $\colorparacol \circ$ is made $\let-equal$ to $\colorparacol \circ$ in $\colorparacol \circ$ is starred version and the adjustment of footnote at $\colorparacol \circ$, while its original version is kept in \colorotote .
- \footnotemark[num] is an API macro to give a footnote mark optionally with the number \langle num \rangle which the mark represents. In \pcol@zparacol it is made \let-equal to \pcol@ footnotemark to implement its starred version and the adjustment of footnote at \end {paracol}, while its original version is kept in \pcol@footnotemark.
- \footnotetext[num]{text} is an API macro to give a footnote (text) optionally with its
 number (num) but without putting the mark in the footnoted text. In \pcol@zparacol
 it is made \let-equal to \pcol@footnotetext to implement its starred version, while its
 original version is kept in \pcol@@footnotetext.
- \footnoterule is an API macro to draw a horizontal line above footnotes, or to insert whatever it has above them. With page-wise footnote typesetting, it is redefined in \pcol@zparacol so that it refers to \textwidth instead of \columnwidth for drawing the horizontal line or whatever defined, while the original version is kept in \pcol@footnoterule. Then it is used in \pcol@putfootins to separate footnotes from the stuff above them, with the original or modified definition.
- \newpage is an API macro to break a page. It is used in \pcol@switchcol as the argument
 of \pcol@visitallcols to break the column-pages visited in the column-scan when the
 synchronized column-switching requires explicit page breaks.
- \dblfigrule is an API macro to draw a horizontal line between the last page-wise floats and the main vertical list, or to insert whatever it has between them. The macro is used in \pcol@startpage to build spanning stuff in the page p in $\pi^b(p)$.
- \topfigrule is an API macro to draw a horizontal line between the last column-wise top float and the main vertical list, or to insert whatever it has between them. The macro is used in \pcol@cflt and \pcol@synccolumn to insert it below the last (real) top float. It is also made \let-equal to \relax temporarily by \pcol@imakeflushedpage when it put floats in a float column as top floats. Note that the macro and its bottom counterpart \botfigrule should produce a vertical list whose total height and depth is 0, because IATEX's float mechanism and thus our macros believe so.
- \normalcolor is an API macro to have color specification stuff for normal coloring. The macro
 is used in \pcol@putfootins to specify the color of footnotes to be put in \@outputbox,
 in \normalcolumncolor[c] to define that the default color of the column c is the normal
 color, in \normalcolseprulecolor to specify that the color for column-separating rules
 is \normalcolor, and in the initial definition of \pcol@colseprulecolor to give the
 default color for column-separating rules.
- \color[mode]{color} is an API macro defined in coloring packages to start text coloring with \color\ optionally with \mode\. The macro is used in \pcol@xcolumncolor[mode] {color}[c] and \pcol@ycolumncolor{color}[c] to define the default color of the column c is \color\ optionally with \mode\, in \pcol@defcseprulecolor@x and \pcol@ defcseprulecolor@y to define the color of column-separating rules, and in \pcol@ backgroundcolor@x to define the color for background painting of a region.

- \pfmtname is an API macro defined in pLATEX to have its format name pLaTeX2e (so far). It is used in the top level assignment of the constant switch \ifpcol@bfbottom.
- $\label{eq:processing} $$ PackageError$ $$ package $$$
- \PackageWarning\langle pkg\langle msg\langle is a developer's API macro to report a warning message \langle msg\langle with the package identification \langle pkg\rangle. The macro is used in \pcol@ignore to complain an API macro appears in paracol inappropriately, in \pcol@fntextbody if the footnote is taller than \textheight \skip\footins, in \pcol@mn@warning to show \marginnote is emulated, and in \pcol@icolumncolor, \pcol@defcseprulecolor@ i and \pcol@backgroundcolor@ii to complain \columncolor/\normalcolumncolor, \colseprulecolor/\normalcolseprulecolor or \backgroundcolor is used without coloring packages respectively.
- $PackageInfo\langle pkg \rangle \langle msg \rangle$ is a developer's API macro to report an informational message $\langle msg \rangle$ with the package identification $\langle pkg \rangle$. The macro is used if the footmisc package is loaded to inform about the footnotelayout alias being unavailable.
- \@@par is an internal macro to keep T_EX's original primitive \par in it. The macro is used in \pcol@output to let \par act with its original definition, and in \pcol@switchcol and \pcol@flushclear as the argument given to \pcol@visitallcols to give T_EX's page builder the chance of page break in column-scanning.
- \@height is an internal macro having the keyword height. It is used in \pcol@buildcolsep rule, \pcol@buildcselt, \pcol@bg@paintregion@i, \pcol@output@start, and \pcol@ putbackmvl to draw a \hrule for column-separating rule in the first two, a \vrule to be painted in the third, and an invisible \hrule in the fourth and last.
- \@width is an internal macro having the keyword width. It is used in \pcol@buildcolsep rule, \pcol@buildcselt, \pcol@bg@paintregion@i, \pcol@output@start, and \pcol@ putbackmvl to draw a \hrule for column-separating rule in the first two, a \vrule to be painted in the third, and an invisible \hrule in the fourth and last.

\@plus is an internal macro having the keyword plus. It is used in the following macros.

- \pcol@makecol to \define \@textbottom with the body of a vertical skip with small infinite stretch and shrink.
- \pcol@combinefloats for a skip of the same amount in \@textbottom above and that of negative amount to *move* the effect.
- \pcol@hfil for skips having 1fil infinite stretch with g_c or $g_c/2$ to make it sure the series of columns and column-separating gaps does not cause underfull.
- \pcol@synccolumn to put a 1fil infinite stretch below the main vertical list together with a small infinite shrink in the column-page being flushed and having a synchronization point, and a vertical skip with a small infinite stretch to push up the main vertical list above a synchronization point.
- \pcol@setcw@getspec@i to add 0pt plus 1000pt minus 1000pt to \@tempskipa to ensure the register have stretch and shrink components.
- \pcol@setcw@fill to let \@tempskipa = 0pt plus f fil as the infinite stretch factor of f.

It is also used in the top level assignment of 0 pt plus 1 fil minus 1 fil to \@tempskipa for the invocation of \pcol@defkw.

\Cminus is an internal macro having the keyword minus. It is used in the following macros.

- \pcol@makecol to \define \@textbottom with the body of a vertical skip with small infinite stretch and shrink.
- \pcol@combinefloats for a skip of the same amount and that of negative amount.
- \pcol@synccolumn to put a small infinite shrink together with a stretch of 1 fil at the bottom of the main vertical list in a column-page being flushed and having a synchronization point.
- \pcol@setcw@getspec@i to add 0pt plus 1000pt minus 1000pt to \@tempskipa to ensure the register have stretch and shrink components.

It is also used in the top level assignment of 0 pt plus 1 fil minus 1 fil to \@tempskipa for the invocation of \pcol@defkw.

- \hb@xt@ is an internal macro having the sequence "\hbox to". It is used in \pcol@
 ioutputelt, \pcol@imakeflushedpage and \pcol@iflushfloats to put each columnpage in a \hbox of \columnwidth wide and to enclose all of them in a \hbox of
 \textwidth wide.
- - \pcol@zparacol for \column* and \pcol@com@column*.
 - \pcol@remctrelt $\langle \theta \rangle$ for \cl@ $\cdot \theta$.
 - \definethecounter $\langle \theta \rangle \langle c \rangle \langle rep \rangle$ for \pcol@thectr@ $\cdot \theta \cdot c$,
 - \pcol@loadctrelt $\langle \theta \rangle \langle val_c(\theta) \rangle$ for \pcol@ctr@ $\cdot \theta$.
 - \pcol@defcolumn for \pcol@com@column*.
 - \pcol@defcseprulecolor@i for \pcol@colseprulecolor[.c].

We also use this macro in top level \definitions of \pcol@com@nthcolumn*, \pcol@ com@leftcolumn* and \pcol@com@rightcolumn* for the starter of the environments nthcolumn*, leftcolumn* and rightcolumn*.

- \pcol@bg@addext $\langle z \rangle$ {s}{d} for \pcol@bg@ext@.d.@.{ $a \cdot @.c, a$ }.
- $\colorsymbol{pcolorsymbol{Q}} columnleft for \colorsymbol{Q} columnwidth c and \colorsymbol{Q} columnsep c.$

- \pcol@bg@columnwidth for \pcol@columnwidth.c.
- \pcol@bg@columnsep for \pcol@columnsep.c.
- \pcol@ccuse for $\gamma_0^c = \col@columncolor@box.c or \hat{\gamma}_0^c = \col@columncolor.c.$
- \column* for \pcol@column*.
- \pcol@zparacol for \pcol@colpream·0.
- \pcol@storectrelt $\langle \theta \rangle$ for \pcol@ctr@ $\cdot \theta$.
- $\col@cmpctrelt(\theta)$ for $\c@.\theta$ and $\col@ctr@.\theta$.
- $\col@synccounter for \col@counters.c for the column c.$
- \pcol@syncctrelt $\langle \theta \rangle$ for \c@ $\cdot \theta$.
- \pcol@stepcounter $\langle \theta \rangle$ for \pcol@counters.c for the column c, and for \cl@. θ .
- \pcol@switchcol to the column c for \pcol@colpream c.
- \pcol@aconlyelt $\langle t \rangle \langle c \rangle$ for \pcol@ac@def@.t.
- \pcol@ac@def@lof $\langle eord \rangle$ and \pcol@ac@def@lot $\langle eord \rangle$ for \pcol@ac@caption@- $\langle eord \rangle$.
- $\col@ac@caption(type)[(lcap)](cap) for \pcol@ac@caption@if@.t and for \ext@(type).$
- \footnoteplacement{l} for pcol@fnlayout@.l.
- \pcol@twosided[T] for pcol@twosided@ $\cdot t$ where $t \in T$.
- \@gobble(arg) discards its argument (arg). It is used in \pcol@output@start, \pcol@
 icolumncolor and \pcol@set@color@push for temporarily letting \aftergroup be
 \@gobble to nullify \aftergroup with \reset@color invoked in \pcol@set@color, being
 the original version of \set@color, and in \pcol@zparacol to make \pcol@bg@paintbox
 \let-equal to \@gobble to nullify it if any coloring packages have not been loaded. In
 addition, the macros \pcol@F and \pcol@Fe for logging are made \let-equal to \@gobble
 at the top level to nullify them.
- $\label{eq:lined_$
- $\langle char \rangle \langle then \rangle \langle else \rangle$ is an internal macro to do $\langle then \rangle$ or $\langle else \rangle$ if the character following to the macro is $\langle char \rangle$ or not respectively. It is used in the following macros to examine if they are followed by a '['.

\paracol, \pcol@zparacol, \columnratio, \pcol@com@column* (initial definition), \pcol@com@switchcolumn, \pcol@iswitchcolumn, \pcol@adjustfnctr, \pcol@ifootnotetext, \twosided, \marginparthreshold, \columncolor, \pcol@columncolor, \normalcolumncolor. \colseprulecolor, \pcol@defcseprulecolor, \normalcolseprulecolor, \pcol@backgroundcolor, \pcol@backgroundcolor@w. It is also used in \pcol@backgroundcolor@iii and \pcol@backgroundcolor@iv if they are followed by a '('.

- \@ifstar(then)(else) is an internal macro to do (then) or (else) if the character following to the macro is '*'. It is used in \pcol@yparacol, \globalcounter, \pcol@switchcolumn, \pcol@footnote, \pcol@footnotemark and \pcol@footnotetext to examine if the optional '*' is specified.
- \@whilesw(sw)\fi(body) is an internal macro to iterate (body) while the switch (sw) is true. It is used in \pcol@output, \pcol@startpage, \pcol@output@clear, \pcol@flushfloats, \pcol@freshpage and \pcol@output@end to iterate building process of float columns or float pages while \if@fcolmade = true, and in \pcol@switchcol and \pcol@flushclear to iterate the height check of synchronized or flushed pages while \ifpcol@flush = true.
- $\langle whilenum \langle ifnum \rangle \langle do \langle body \rangle$ is an internal macro to iterate $\langle body \rangle$ while the integer comparison expression $\langle ifnum \rangle$ is *true*. The macro is used in the following macros to iterate their own procedures for all columns $c \in [0, C)$.

\pcol@checkshipped, \pcol@output@start, \pcol@output@switch, \pcol@sync, \pcol@makeflushedpage, \pcol@freshpage, \pcol@output@end, \pcol@synccounter, \pcol@com@syncallcounters, \pcol@stepcounter, \pcol@visitallcols.

The macro is also used in the following macros for the ranges following macro name, where $(C^0, C^1) \in \{(0, C_L), (C_L, C)\}$ and c is the column they are working on.

The other users have a little bit more complicated range as follows.

- \pcol@flushcolumn to iterate float column building for a column c in pages q such that $q \in (\kappa_c(\beta^p), p_t)$.
- \pcol@setcolwidth@r to make assignment of w_c for $c \in [\min(C^0+k, C^1-1), C^1)$ where k is the number of fractions given as the first or second argument of \columnratio and kept in \pcol@columnratioleft or \pcol@columnratioright, respectively.
- \pcol@setcw@calcf $\langle x \rangle \langle y \rangle \langle z \rangle$ to calculate $\lceil y/2^{k_2+k_3} \rceil$ finding k_3 by iterating y/2 until the result becomes less than 2^{15} , to calculate $z'/2^k$ with the range [0, k), to calculate $z'/2^{k-16}$ with the range [0, k-16), and to calculate $z' \cdot 2^{16-k}$ with the range [0, 16-k), where $z' \cdot 2^{16-k} = Z = z \times 1 \, \text{pt}$ and k_2 , k_3 and k are scaling parameters for good approximation.
- $\begin{aligned} & \texttt{Cwhiledim}\langle ifdim\rangle \texttt{do}\langle body\rangle \text{ is an internal macro to iterate } \langle body\rangle \text{ while the dimensional com$ $parison expression } \langle ifdim\rangle \text{ is } true. The macro is used in <math display="block">\texttt{pcol@setcw@calcf}\langle x\rangle\langle y\rangle\langle z\rangle \\ & \texttt{twice, at first to find } k_1 = \min\{k \mid x \cdot 2^k \geq 2^{13}\,\texttt{pt}\} \text{ and to have } x \cdot 2^{k_1}, \text{ and then to find } \\ & k_2 = \max\{k \mid y \bmod 2^k = 0\} \text{ and to have } y/2^{k_2}. \end{aligned}$

- $\comma-separated \langle list \rangle \ is an internal macro to iterate \langle body \rangle \ for each element of the comma-separated <math>\langle list \rangle$ letting $\langle cs \rangle$ have the element. The macro is used in $\col@setcolwidth@r to scan its argument \langle ratio \rangle \ defined \ by \columnratio, and in \pcol@setcw@scan to scan its argument <math>\langle spec \rangle \ defined \ by \setcolumnwidth.$
- $\times control contr$
- $\langle elm \rangle \langle lst \rangle \langle suc \rangle \langle fail \rangle$ is an internal macro to remove the first element from $\langle lst \rangle$, $\langle define \langle elm \rangle$ to have the first element, and then do $\langle suc \rangle$, if $\langle lst \rangle$ is not empty. Otherwise, it performs $\langle fail \rangle$. The macro is used in the following macros to obtain an $\langle nsert$ from $\langle freelist$.
 - \pcol@opcol for the completed column-page.
 - \pcol@startpage for float pages and spanning stuff for page-wise top floats.
 - \pcol@output@start for the pre-environment stuff, and column-pages and γ_0^c of all columns.
 - \pcol@output@switch for the column-page from which we are leaving.
 - \pcol@iscancst for γ_0^c .
 - \pcol@savefootins for footnotes.
 - \pcol@flushcolumn for float columns and the empty column-page in p_t .
 - \pcol@synccolumn for an MVL-float on a synchronization if its point defined by a column whose main vertical list is empty.
 - \pcol@output@end for the page-wise floats in the last page if the main vertical list of the page is empty.
 - \pcol@icolumncolor for γ_0^c .

The macro is also used in \pcolloutputelt to obtain completed column-pages from S_c .

 $\langle lst \rangle \langle elm \rangle$ is an internal macro to add $\langle lst \rangle$.

- \pcol@makecol to add span(H,h) to the tail of $\pi^{s}(p_{t})$.
- \pcol@opcol to add the completed current column-page $\kappa_c(\beta)$ to S_c .
- \pcol@startpage to add $\pi(p_t 1)$ and float pages to Π .
- \pcol@outputelt to return spanning stuff $\pi^i(q)$ in a shipped-out float page q to \@freelist, or to add $\pi(q)$ to Π if the page q is kept.
- \pcol@ioutputelt to return spanning stuff $\pi^i(q)$, page-wise footnotes $\pi^f(q)$ and/or column-pages $s_c(q)$ for all $c \in [0, C)$ in a shipped-out page q to \@freelist.
- \pcol@output@start to return the current column-page $\kappa_0(\beta)$ to \@freelist.

- \pcol@output@switch to add span(H,h) to the tail of $\pi^{s}(p_{t})$.
- \pcol@restartcolumn to return the current column-page $\kappa_c(\beta)$ to be resumed, and its footnotes $\kappa_c(\tau)$ if any, to \@freelist.
- \pcol@getmparbottom $\langle t \rangle \langle h \rangle$ to add $mpar(\max(t, b_n), \max(t, b_n) + h)$ to the tail of the list $M_{\{L,R\}}^{\{l,r\}}$, and its callee \pcol@getmpbelt $\langle t_i \rangle \langle b_i \rangle$ to add $mpar(t_i, b_i)$ or $mpar(\max(t, b_{i-1}), \max(t, b_{i-1}) + h)$ to the so-far tail of the list in rebuilding.
- \pcol@flushcolumn to return footnotes $\kappa_c(\tau)$ in the current column-page of c to be flushed to \@freelist if any, and to add the flushed column-page and float columns to S_c .
- \pcol@makefcolelt to add a float to \@toplist or $\kappa_c(\lambda_d)$.
- \pcol@synccolumn to add an MVL-float for synchronization to $\kappa_c(\lambda_t)$.
- \pcol@makeflushedpage to return spanning stuff $\pi^i(p_t)$ and/or page-wise footnotes $\pi^f(p_t)$ in the top page to be flushed to \@freelist if any.
- \pcol@imakeflushedpage to return column-wise footnotes in $\kappa_c(\tau)$ s.t. $\kappa_c(\beta^p) = p_t$ to \@freelist if any.
- \pcol@output@end to return $\pi^f(p_t)$, all current column-pages $\kappa_c(\beta)$, and all $\gamma_0^c \neq \bot$ to \@freelist.
- \pcol@end@dblfloat to add a page-wise float in \@currbox to \@dbldeferlist.
- \globalcounter $\langle \theta \rangle$ to add a global counter θ to Θ^g .
- \pcol@iremctrelt $\langle \theta \rangle$ to add a local counter θ to Θ^l .
- \pcol@storectrelt $\langle \theta \rangle$ to add a pair $\langle \theta, val_c(\theta) \rangle$ to Θ_c for a column c.
- \pcol@savectrelt $\langle \theta \rangle$ to add a pair $\langle \theta, val(\theta) \rangle$ to Θ_c for a column c.
- \pcol@cmpctrelt(θ) to add a counter θ to the list of local counters to be synchronized.
- \addcontentsonly $\langle t \rangle \langle c \rangle$ to add a pair $\langle t, c \rangle$ to T.
- \pcol@backgroundcolor@ii to add a region whose background is painted to \pcol@ bg@defined.
- $\langle cdr \langle a_1 \rangle \langle a_2 \rangle \cdots \langle a_n \rangle \langle cnil \text{ is an internal macro to be expanded to } \langle a_2 \rangle \cdots \langle a_n \rangle$. It is used in \pcol@getcurrpinfo $\langle cs \rangle$ to extract $\pi(p_t)$ from \pcol@currpage = $\langle clt \langle \pi(p_t) \rangle$ and to \define $\langle cs \rangle$ letting it have $\pi(p_t)$.
- $\label{eq:latex@warning@no@line(msg)}$ is an internal macro to report a warning message $\langle msg \rangle$ without the line number in which the cause lies. It is used in \coleoutput if a page with floats and very short main vertical list is built.
- \@eha is an internal macro having a help message saying the command causing an error is ignored. It is used in \pcol@zparacol, \pcol@setcw@calcf, \pcol@switchcolumn, \pcol@switchenv, and \addcontentsonly as the argument of \PackageError.
- \Cehb is an internal macro having a help message saying the error causes a serious problem. It is used in \pcolCovf, \pcolCzparacol and \pcolCsetCcolorCpush as the argument of \PackageError.

- \@parmoderr is an internal macro to complain about misplacement of a macro or environment which is expected to appear in "outer par mode". It is used in \pcol@zparacol if it finds \ifinner = true.
- \@Esphack is an internal macro to put back the horizontal skip and space factor saved by \@bsphack at the end of an environment. It is used in \pcol@end@dblfloat.
- \reset@font is an internal macro \let-equal to \normalfont to use a standard font. It is
 used in \pcol@fntextbody for footnote typesetting.
- \set@color is an internal macro to start coloring of texts following it. By default it is \relax
 but may have a definition to put a \special for coloring with the color in \current@
 color. In the following macros, it is examined if \set@color = \relax and/or some
 local definition is given to \set@color.
 - \pcol@output lets \set@color = \pcol@set@color i.e., lets it regain its original definition because we don't need any special operations in \output routine.
 - \Coutputpage performs background painting if $\setCcolor \neq \relax$.
 - \pcol@zparacol performs set-up operations for text coloring, including making \set@color \let-equal to \pcol@set@color@push saving its original definition into \pcol@set@color, and enabling background painting macros if \set@color ≠ \relax, while these background painting macros are nullified otherwise.
 - \pcol@icolumncolor complains that no color packages have been loaded if \set@ color = \relax, and then otherwise temporarily lets it be the original saved in \pcol@set@color to \insert a \vbox to update γ_0^c or to do the update immediately.
 - \pcol@iicolumncolor temporarily lets \set@color = \relax so that \color or \normalcolor invoked in the macro just defines \current@color to be set into $\hat{\gamma}_0^c$ without doing any other coloring operations.
 - \pcol@defcseprulecolor@i complains that no color packages have been loaded if \set@color = \relax, while otherwise the macro temporarily lets \set@color = \relax to invoke \color (or \normalcolor) to check if its arguments are properly given.
 - \pcol@backgroundcolor@ii complains that no color packages have been loaded if \set@color = \relax, while otherwise its descendent \pcol@backgroundcolor@x temporarily lets \set@color = \pcol@backgroundcolor@y to \define \pcol@bg@ color@a[@.c] to be \current@color.
- \reset@color is an internal macro to finish text coloring started by \set@color. By default it is undefined but may have some definition to put a \special to finish coloring. It is used in \pcol@clearcolorstack so as to apply it to all elements in Γ^c , in \pcol@iscancst to put it to the main vertical list in the case that γ_0^c was \perp and then updated, in \pcol@ icolumncolor to apply it to all elements in $\hat{\Gamma}^c$, and in \pcol@reset@color@pop and \pcol@reset@color@mpop to have an uncoloring \special in the \vbox for γ_i and $\gamma_{i,m}$.
- \color@begingroup is an internal macro to open a group in which a color is specified. It
 is used in \pcol@putfootins to enclose footnotes with \normalcolor, and in \pcol@
 fntextbody{text} to enclose the coloring in the footnote (text).
- \color@endgroup is an internal macro to close a group in which a color is specified. It
 is used in \pcol@putfootins to enclose footnotes with \normalcolor, and in \pcol@
 fntextbody{text} to enclose the coloring in the footnote (text).

- $(\texttt{@stpelt}\langle\theta\rangle)$ is an internal macro to zero-clear the counter θ for the implementation of stepcounter. It is used in pcol@stepcounter to clear the descendent counters of a global counter θ^g listed in $\texttt{pcol@cl@}.\theta^g$.
- \@nbitem is an internal macro to insert a vertical skip of \@outerparskip \parskip above the first \item of a list-like environment when \if@nobreak = true. It is used by \pcol@zparacol when it finds the paracol environment to start is at the very beginning of a list-like environment and \if@nobreak = true.
- \@parboxrestore is an internal macro to set up typesetting parameters for paragraphs encapsulated in a box. It is used in \pcol@fntextbody for paragraphs in a footnote.
- $\langle \texttt{Ofinalstrut} \langle box \rangle$ is an internal macro to add an invisible vertical rule whose depth is that of a $\langle box \rangle$. It is used in $\colored fntextbody$ to make the last line of the footnotes is as deep as $\langle \texttt{strutbox}$ at shallowest.
- \@sect is an internal macro to implement sectioning commands. The original definition of the macro is kept in \pcol@ac@enable@toc, while \pcol@ac@def@toc makes it \let-equal to \pcol@ac@enable@toc or \pcol@ac@disable@toc, the latter of which uses the original version temporarily disabling \addcontentsline.
- \@svsechd is an internal macro (locally) \defined in \@sect and \@ssect to keep the section header of a sectioning command such as \paragraph which puts the header as the leading text of the paragraph following the command rather than putting it as an individual paragraph. The macro is \globalized in \pcol@sptext so that it is properly referred to in \everypar for the paragraph led by the text in case that a spanning text has the sectioning command only and thus the \definition of the macro must survive after we close the group in which the spanning text is put.
- \@svsec is an internal macro (locally) \defined in \@sect to keep \thesection etc. to be displayed as the leading part of the section header. The macro is \globalized in \pcol@ sptext together with \@svsechd because it is in the body of \@svsechd.
- \@caption is an internal macro to implement \caption. The original definition of the macro is kept in \pcol@ac@caption@latex, while \pcol@ac@caption@def makes it \let-equal to \pcol@ac@caption which uses the original version temporarily disabling \addcontentsline if necessary.
- \end@float is an internal macro to close a column-wise float environment. It is used in \pcol@
 end@dblfloat (but never invoked because we have \if@twocolumn true always).
- \Cendfloatbox is an internal macro to close a \vbox for a float. It is used in \pcolCendC dblfloat.
- \@largefloatcheck is an internal macro to examine if a float is too large. It is used in \pcol@
 end@dblfloat.
- \@floatplacement is an internal macro for \output routine to reinitialize column-wise float placement parameters. It is used in our own version of it, \pcol@floatplacement.

- \@dblfloatplacement is an internal macro for \output routine to reinitialize page-wise float placement parameters. It is used in \pcol@startpage and \pcol@output@clear prior to processing page-wise floats in \@dbldeferlist. As discussed in item-(2) of §1.8, this macro in 2015 or later version of LATEX lets \f@depth = 1sp.
- \@xympar is an internal macro to perform the last operations for \marginpar. In \pcol@
 zparacol it is made \let-equal to \pcol@xympar for the emulation of \marginnote,
 while its original version is kept in \pcol@@xympar.
- \p@footnote is an internal macro to have the prefix to \thefootnote in the printed reference
 of the counter footnote. It is used in \pcol@fntextbody to produce \@currentlabel.
- \Cthefnmark is an internal macro to have \thefootnote¹³¹. It is used in \pcolCfntextbody to produce \Ccurrentlabel.
- $(footnotetext{text})$ is an internal macro to implement $footnote and footnotetext for <math>\langle text \rangle$. In pcol@zparacol, it is made let-equal to pcol@fntext.
- $\mbox{Gmakefntext}{fn}$ is an internal macro to typeset the footnote $\langle fn \rangle$. It is used in \pcol@ fntextbody{*text*} to typeset the footnote $\langle text \rangle$ with some other stuff.
- \@emptycol is an internal macro for \output routine to put back an empty page to the main vertical list. It is used \pcol@output if a page with floats and very short main vertical list is built.
- \@specialoutput is an internal macro for \output routine to process an \output request made by IATEX's original \clearpage, \end{float} and \marginpar. It is used in \pcol@ specialoutput to process the request for floats or marginal notes.
- \@opcol is an internal macro for \output routine to output a page or to keep the first column until the second one is completed. This macro is used in \pcol@output to process a sneaked \output request from outside of paracol, and in \pcol@output@end for the case page-wise floats are left at \end{paracol} and they are put in float pages.
- \@makecol is an internal macro for \output routine to build the ship-out image of a column in \@outputbox consisting of top floats, main vertical list in \box255, footnotes in \footins, and bottom floats¹³². It is used in \pcol@output to process a sneaked \output request from outside of paracol, in \pcol@makecol for a column-page to be flushed by \pcol@ flushcolumn and \pcol@makeflushedpage, in \pcol@makecol for an ordinary column-page, and in \pcol@output@start and \pcol@makenormalcol for pre-environment stuff.
- \@textbottom is an internal macro for \output routine to be put at the bottom of \@outputbox in which a column-page is stored, by \@makecol. This macro is temporarily re\defined by \pcol@makecol for a column-page having synchronization points so that it has a vertical skip of infinite stretch and shrink to push up/down the stuff below the last synchronization point in order to adjust its top to the point. After that, its original definition kept in \pcol@textbottom is restored. Another modifiers of the macro are as follows; \pcol@makenormalcol to make the macro \let-equal to \relax temporarily to avoid the insertion of whatever the macro has in \@makecol; and \pcol@makeflushedpage to let the macro have \vfil temporarily so that empty columns in a last page are made *full size* without underfull.

 $^{^{131}\}mathrm{Or}$ \thempfootnote in minipage environment.

 $^{^{132}}$ In pLATEX, the order of footnotes and bottom floats are reversed.

- \Coutputpage is an internal macro for \output routine to output a page kept in \Coutputbox together with the header and footer. The original definition of this macro is saved in \pcolCoutputpage to be used in \pcolCoutputpageCl and \pcolCoutputpageCr being callees of our own revised version of \Coutputpage. Therefore, any \output request to result in page ship-out reaches our own \Coutputpage and then LATEX's one after we perform operations for parallel-paging and background painting onto the ship-out image.
- \@combinefloats is an internal macro for \output routine to combine top and bottom floats in \@toplist and \@botlist respectively with \@outputbox in which the main vertical list and footnotes¹³³ have been put by \@makecol, and to have the result in \@outputbox again. In \pcol@zparacol, it is made \let-equal to our own \pcol@combinefloats so that \@makecol and \pcol@makenormalcol uses it instead of the original one. However, if \pcol@output finds that the \output request for a page break outside paracol is sneaked into our own \output routine, it makes this macro \let-equal to \pcol@combinefloats in which LATEX's version is kept so that LATEX's original \output routine works perfectly as original.
- \@cflt is an internal macro for \output routine to put all top floats in \@toplist and related stuff such as the vertical skip of \textfloatsep into \@outputbox together with its old contents being the main vertical list and footnotes¹³³. It is used in \pcol@combinefloats if the column-page being processed does not have synchronization points.
- \@cflb is an internal macro for \output routine to put all bottom floats in \@botlist and related stuff such as the vertical skip of \textfloatsep into \@outputbox together with its old contents being top floats, the main vertical list and footnotes¹³³. It is used in \pcol@combinefloats.
- $\langle \texttt{Comflelt} \langle flt \rangle$ is an internal macro for $\langle \texttt{output}$ routine to put $\langle flt \rangle$ being a column-wise top or bottom float to the tail of $\langle \texttt{Ctempboxa}$ which finally has all top/bottom floats in a column. It is used in pcol@cflt to apply it to each element of $\langle \texttt{Ctoplist}$.
- $\comdblflelt\langle flt \rangle$ is an internal macro for \output routine to put $\langle flt \rangle$ being a page-wise float to the tail of \compboxa which finally has the spanning stuff for page-wise floats. It is used in \compboxa to apply to each element of \complex to have the spanning stuff.
- \@startcolumn is an internal macro for \output routine which tries to build a float column for the floats in \@deferlist and, if the column is not built, tries to move floats to \@toplist and \@botlist. This macro is used in \pcol@output to process a sneaked \output request from outside of paracol, and in \pcol@output@end for the case pagewise floats are left at \end{paracol} after which they become column-wise ones.
- $\langle \texttt{Ctryfcolumn}\langle lst \rangle$ is an internal macro for $\langle \texttt{output}$ routine which examines if a float column or a float page can be built with some floats in $\langle lst \rangle$ and, if so, builds the page in Coutputboxremoving floats put in the page from $\langle lst \rangle$. It is used in pcol@startpage for page-wise floats in Cdbldeferlist, and in pcol@startcolumn for column-wise floats in $\kappa_c(\lambda_d)$.
- $\langle gscolelt \langle flt \rangle$ is an internal macro for $\langle output$ routine which examines if a column-wise float $\langle flt \rangle$ can be added to $\langle @toplist$ or $\langle @botlist$ being the list of the floats to be put at the top or bottom of a page respectively. Then, if the examination succeeds, $\langle flt \rangle$ is added to $\langle @toplist$ or $\langle @botlist, while it is added$ to $\langle @deferlist$ otherwise. It is used in $\langle pcol@trynextcolumn$ to apply to each element of (the copy of) $\kappa_c(\lambda_d)$.

 $^{^{133}}$ In pLAT_EX, footnotes are not in \Coutputbox because of the reversal of footnotes and bottom floats.

- \@addmarginpar is an internal macro for \output routine to add a marginal note. Its original definition is kept in \pcol@addmarginpar and used in \pcol@addmarginpar being our own \@addmarginpar.
- $\mbox{Cmakefcolumn}\langle lst \rangle$ is an internal macro for \mbox{output} routine to build a float column with some floats at the head of a float list $\langle lst \rangle$ and to remove the floats from the list. It is used in $\mbox{pcol@flushcolumn}$ and $\mbox{pcol@flushfloats}$ for $\kappa_c(\lambda_d)$ of column-wise floats, and in $\mbox{pcol@output@clear}$ for $\mbox{Qdbldeferlist}$ of page-wise floats.

2.2.2 Structural Macros

- $\langle \texttt{delt} \langle a_1 \rangle \cdots \langle a_n \rangle$ is an internal control sequence to represent a list element having n subelements. The sequence is often made $\langle \texttt{let}$ -equal to a macro which processes $\langle a_1 \rangle \cdots \langle a_n \rangle$ and is applied to all members in a list. It is also made $\langle \texttt{let}$ -equal to $\langle \texttt{relax}$ on a manipulation of a list, such as element addition and concatenation, by $\langle \texttt{edef}$ or $\backslash \texttt{xdef}$. The usages of the sequence are as follows.
 - \pcol@F@count \defines \@elt as a macro to increment \@tempcnta by one to measure the cardinality of \@freelist.
 - \pcol@cflt lets \@elt = \@comflelt for $\kappa_c(\lambda_t)$, and then \@elt = \relax to concatenate \@freelist and $\kappa_c(\lambda_t)$.
 - \pcol@setpageno lets \@elt = \pcol@setpnoelt for Π .
 - \pcol@setpnoelt and \pcol@setmpbelt let \@elt = \relax to add $\pi(q)$ to Π . It also uses \@elt to \define \pcol@currpage with \@elt{ $\pi^p(q)$ } $\langle \pi^i(q) \rangle \langle \pi^f(q) \rangle$ { $\pi^s(p)$ }{ $\pi^m(p)$ }.
 - \pcol@defcurrpage lets \@elt = \relax to \xdefine \pcol@currpage with $\ensuremath{\mathbb{Q}}\$
 - \pcol@nextpage lets \@elt = \pcol@nextpelt for Π .
 - \pcol@getcurrpage lets $\ensuremath{\col@getpelt}$ for Π^+ .
 - \pcol@startpage lets \@elt = \@sdblcolelt for (the copy of) \@dbldeferlist, and \@elt = \@comdblflelt for \@dbltoplist. It also lets \@elt = \relax for the concatenation of \@dbldeferlist and \@deferlist, and that of \@freelist and \@dbltoplist.
 - \pcol@outputcolumns lets \@elt = \pcol@outputelt with two arguments for (the copy of) Π.
 - \pcol@ioutputelt \defines \pcol@bg@footnoteheight and \pcol@bg@float height with \@elt to let painting macros add elements in them to have the height of the background regions $R_{\{n,N\}}$ and $R_{\{f,F\}}$ to be painted.
 - \pcol@buildcolseprule lets \@elt = \pcol@buildcselt@S and then \@elt = \pcol@buildcselt for $\pi^s(p)$, and then \defines \pcol@bg@columnheight with \@elt to add H'_n and \@maxdepth or 0 for the background region $R^c_{\{c,g\}}(n+1)$ where $n = |\pi^s(p)|$.

- \pcol@buildcselt@S \defines \pcol@bg@spanningtop and \pcol@bg@spanning height with \@elt to define the region $R_S(i)$.
- \pcol@buildcselt \defines \pcol@bg@columnheight, \pcol@bg@spanningtop and \pcol@bg@spanningheight with \@elt to define regions $R^c_{\{c,g\}}(i)$ and $R_s(i)$.
- \pcol@bg@calculate $\langle z \rangle \langle z_0 \rangle \{F\}$ lets \@elt = \pcol@bg@advance to let \@elt $\langle f \rangle$ in F do $z \leftarrow z + f$.
- \pcol@bg@negative{F⁻} lets \@elt = \pcol@bg@nadvance to let \@elt⟨f⟩ in F⁻ do z ← z − f, and then lets \@elt = \pcol@bg@advance to go back to addition.
- \pcol@output@start lets all floats f imported in \@dbldeferlist have depth 0 by \defining \@elt $\langle f \rangle$ to do it, \edefines \pcol@bg@textheight with \@elt having height-plus-depth of pre-environment stuff for background painting of it, and \defines $\pi^m(0)$ having one element in M_L^l or M_L^r for \@mparbottom in pre-environment stuff.
- \pcol@makenormalcol lets \@elt = \relax to concatenate \@freelist and \@midlist.
- \pcol@trynextcolumn lets \@elt = \@scolelt for (the copy of) $\kappa_c(\lambda_d)$.
- \pcol@setcurrcol lets \@elt = \relax to \xdefine κ_c with $\kappa_c(\lambda_t) = \$ @toplist, $\kappa_c(\lambda_m) = \$ @midlist, $\kappa_c(\lambda_b) = \$ @botlist and $\kappa_c(\lambda_d) = \$ @deferlist.
- \pcol@scancst and \pcol@iscancst let \@elt = \relax to \edefine the list $M = (m \mid \gamma_{j,m}^- \in \Gamma_r, j \ge i)$ for $\gamma_{i,*}^-$, and then the latter \defines \@elt as a macro with an argument m to examine $m \in M$ for $\gamma_{i,m}$.
- \pcol@addmarginpar lets \@elt = \pcol@setmpbelt for Π^+ .
- \pcol@getmparbottom lets \@elt = \pcol@getmpbelt for the list $M_{\{L,R\}}^{\{l,r\}}$. It also lets \@elt = \relax for the addition of $mpar(h_i, t_i)$ to the list by itself and \pcol@ getmpbelt.
- \pcol@mparbottom@zero has \@elt in its body to have mpar(0,0) for each $M \in \{M_X^x \mid X \in \{L, R\}, x \in \{l, r\}\}$ the macro has.
- $\col@bias@mpbout@i{y}\@elt{t}{b}\@nil has \@elt in its argument specification, and \defines \reserved@b with \@elt for <math>mpar(t + y, b + y)$.
- \pcol@getmparbottom@last@i{y}mpar(t_1, b_1) · · · mpar(t_n, b_n)\@nil at first \defines \reserved@b with \@elt for mpar(y, y) and then \defines \@elt to do it for mpar(t_i, b_i) for all $i \in [1, n]$.
- \pcol@makefcolumn lets \@elt = \pcol@makefcolelt for (the copy of) $\kappa_c(\lambda_d)$ to examine if each float in it can be put in a float column to be built, and then \define it to put floats in $\kappa_c(\lambda_t)$ into $\kappa_c(\beta^b)$.
- \pcol@addflhd lets \@elt = \pcol@hdflelt for its argument $\kappa_c(\lambda_t)$ or $\kappa_c(\lambda_b)$, and then \@elt = \relax to give the default.
- \pcol@makeflushedpage \edefines \pcol@bg@floatheight with \@elt letting it be \relax.
- \pcol@imakeflushedpage \defines \pcol@bg@footnoteheight with \@elt.
- \pcol@output@end uses \@elt in the argument specification of the \definition of \pcol@do@mpbout@elem, lets \@elt = \relax to add the spanning stuff of the last page to the head of \@dbldeferlist, and uses it in the body of \pcol@bg@textheight and \pcol@bg@footnoteheight to be \defined for background painting of page-wise footnotes.

- \pcol@zparacol lets \@elt = \pcol@remctrelt for Θ^g , \@elt = \pcol@thectrelt for Θ^l , \@elt = \pcol@loadctrelt for Θ_0 , \@elt = \pcol@cmpctrelt for Θ^l , \@elt = \pcol@defcomelt for \pcol@localcommands, and then \@elt = \relax to give the default.
- \globalcounter{*ctr*} defines \Qelt{ θ } for Θ^g to check if there is $\theta \in \Theta^g$ such that $\theta = \langle ctr \rangle$.
- \pcol@localcommands has the sequence of $\ensuremath{\texttt{Com}}\$ for all local commands $\com\$.
- \pcol@gcounters has \@elt{page} as its initial definition.
- \pcol@removecounter $\langle \Theta' \rangle \langle \theta \rangle$ lets \@elt = \pcol@iremctrelt for (the copy of) its argument Θ' to remove θ from it.
- \pcol@sscounters $\langle elt \rangle$ lets \@elt = $\langle elt \rangle$, where $\langle elt \rangle$ = \pcol@storectrelt or $\langle elt \rangle$ = \pcol@savectrelt, for Θ^l , and then \@elt = \relax to \xdefine Θ_c .
- \pcol@com@synccounter(θ) gives \@elt{ θ } as the argument of \pcol@synccounter.
- \pcol@synccounter $\langle lst \rangle$ lets \@elt = \relax to have the list $\langle lst \rangle$ in \reserved@a by \edef, \@elt = \pcol@loadctrelt for Θ_c , and then \@elt = \pcol@syncctrelt for $\langle lst \rangle$.
- \pcol@stepcounter $\langle \theta \rangle$ lets \@elt = \pcol@stpldelt for Θ^l , \@elt = \pcol@ stpclelt for $\zeta(\theta)$, and then \@elt = \@stpelt for $\zeta(\theta)$.
- \pcol@switchcol lets \@elt = \pcol@setctrelt for Θ_c , \@elt = \pcol@ aconlyelt for T, and then \@elt = \relax to give the default.
- \pcol@icolumncolor \defines \Qelt $\langle \hat{\gamma}_i \rangle$ to apply \reset@color for rewinding and \pcol@set@color for reestablishing to each $\hat{\gamma}_i \in \hat{\Gamma}^c = (\hat{\gamma}_0^c, \hat{\Gamma})$ by \pcol@scancst@ shadow, in which \Qelt is explicitly applied to $\hat{\gamma}_0^c$ if it is defined and then implicitly done to $\hat{\Gamma} =$ \pcol@colorstack@shadow.
- \pcol@set@color@push lets \@elt = \relax to push a color information into $\overline{\Gamma}$, with save/restore of its original value.
- \resetbackgroundcolor lets $\ensuremath{\collimits{collimits}}\ \$ to let $\prol@bg@color.a'_i$ for each of i.

\Cempty is a macro always having nothing. Its major usages are to examine if a macro often having a list is empty, and to make such a macro empty. The following macros use \Cempty to examine the emptiness of the objects in parentheses.

The following macros use \@empty to empty the objects in parentheses.

 $\label{eq:constraint} $$ \ (\kappa_c(\lambda_t)) \\ \ (\kappa_c(\lambda_t)) \\ \ (\kappa_c(\lambda_d), (db)deferlist, (deferlist, (db)toplist)) \\ \ (\kappa_c(\lambda_d)) \\ \ (\kappa_c(\lambda_d), \kappa_c(\lambda_t)) \\ \ (\kappa_c(\lambda_d),$

- \@currentlabel is an internal macro to have the reference to be associated with the \label following it. It is defined in \pcol@fntextbody to have the reference to the footnote with \@thefnmark.
- \ext@figure is an internal macro having "lof" being the extension of the file for list of figures. It is used in \pcol@ac@caption $\langle type \rangle [\langle lcap \rangle] \langle cap \rangle$ to have "lof" when $\langle type \rangle =$ figure.
- \ext@table is an internal macro having "lot" being the extension of the file for list of tables. It is used in \pcol@ac@caption $\langle type \rangle [\langle lcap \rangle] \langle cap \rangle$ to have "lot" when $\langle type \rangle = table$.
- \Ccurrbox is an internal macro which conventionally has an \insert for floats, etc. The following macros use \Ccurrbox having the objects in parentheses.

```
\collopcol(\kappa_c(\beta))
\pcol@startpage (\pi^i(p_t))
\pcol@ioutputelt (s_c(q))
\pcol@output@start (\pi^i(0), \kappa_c(\beta), \gamma_0^c)
\collocutput@switch(\kappa_c(\beta))
\colorestartcolumn (\kappa_c(\beta))
\climits \
\clicklinet
\clickmvl(\kappa_c(\beta))
\pcol@iscancst (\gamma_0^c)
\pcol@addmarginpar (left marginal note)
\pcol@flushcolumn (\kappa_c(\beta), s_c(q))
\colomakefcolumn (\kappa_c(\beta))
\colored measurecolumn (\kappa_c(\beta))
\colorsynccolumn (\kappa_c(\beta))
\pcol@imakeflushedpage (\kappa_c(\beta))
```

- \Cmarbox is an internal macro which has an \insert for left marginal notes. It is used in \pcolCxympar.
- \@currlist is an internal macro which has an list of \inserts for floats and marginal notes given to output. It is used in \pcol@addmarginpar to get the right marginal note from its head.
- \@freelist is an internal macro having available \inserts for floats originally, but also column-pages, spanning stuff, footnotes and default column-color in our usage. Besides the acquisition of an \insert from it shown in the description of \@next, it is used by the following macros to return the the objects in parentheses to \@freelist.

In addition \pcol@F@count scans its element to have its cardinality.

- \@nil is an internal control sequence which is conventionally used to terminate a variable length argument. It is used in the following macros.
 - \pcol@getcurrpinfo for the invocation of \@cdr.
 - \pcol@bias@mpbout@i{y}\@elt{t}{b}\@nil to capture t and b following the convention in \pcol@do@mpb@all@ii.
 - \pcol@getmparbottom@last@i {y} $mpar(t_1, b_1) \cdots mpar(t_n, b_n)$ \@nil to capture $mpar(t_i, b_i)$ for all $i \in [1, n]$.
 - \pcol@do@mpb@all@i{ M_L^l }{ M_L^r }{ M_R^r } to terminate the list $M \in \{M_X^x \mid X \in \{L, R\}, x \in \{l, r\}\}$ in the invocation of \pcol@do@mpb@all@ii.
 - \pcol@do@mpb@all@ii{y} mpar(t_1, b_1) \cdots mpar(t_n, b_n)\@nil to capture mpar(t_i, b_i) for all $i \in [1, n]$, and then to terminate them passed to \pcol@bias@mpbout@i or \pcol@getmparbottom@last.
 - \pcol@setcw@scan for the invocation of \pcol@setcw@getspec $\langle w'_d \rangle / \langle g'_d \rangle / \langle garbage \rangle$ \@nil.

- \pcol@setcw@getspec@i for the invocation of \pcol@extract@fil(n) plus (f) minus(garbage)\@nil and thus in the \definition of it in \pcol@def@extract@fil.
- \pcol@defkw has \@nil in its argument specification to terminate the argument 0pt plus 1fil minus 1fil.
- \pcol@extract@fil@i, \pcol@extract@fil@ii and \pcol@extract@fil@iii have \@nil in their argument specifications as the terminator, and thus \@nil appears in their invocations in \pcol@extract@fil, \pcol@extract@fil@i and \pcol@ extract@fil@ii respectively, and in the \definition of \pcol@extract@fil@iii in \pcol@def@extract@fil@iii.
- \pcol@iadjustfnctr and \pcol@iifootnotetext to terminate their argument [[+-] disp] passed to \pcol@calcfnctr.
- \backgroundcolor and \nobackgroundcolor to terminate their first argument given to \pcol@backgroundcolor so that its descendants \pcol@backgroundcolor@ x and \pcol@backgroundcolor@z finally capture everything not processed by their ancestors.
- \current@color is an internal macro having color information to be put into .dvi as a part
 of the argument of coloring \special. It is referred to by \pcol@bg@paintregion@i,
 \pcol@output@start, \pcol@icolumncolor, \pcol@iicolumncolor, and \pcol@set@
 color@push, \pcol@backgroundcolor@y.
- \@dbldeferlist is an internal macro having the list of page-wise floats whose page appearance are not yet fixed. It is scanned and then updated in \pcol@startpage and \pcol@ output@clear, while \pcol@output@start lets it have \@deferlist made before \begin {paracol}, and \pcol@output@end adds page-wise floats to be put in the empty last page to it and then move the whole of the list to \@deferlist. As discussed in §1.8, 2015 or later version of IATEX no longer uses this list, but we stick with it for page-wise floats produced in paracol environments and thus have its top level definition with empty body in paracol.
- \@dbltoplist is an internal macro having the list of page-wise floats which \@sdblcolelt decided to be put in the new page. The macro \pcol@startpage scans it to put all floats into the page p_t as its spanning stuff $\pi^i(p_t)$, and then empties it after returning all floats to \@freelist.
- \@deferlist is an internal macro having the list of column-wise floats whose page appearance are not yet fixed. It is scanned and then updated in \pcol@startcolumn, \pcol@ trynextcolumn, \pcol@flushcolumn, \pcol@makefcolumn and \pcol@iflushfloats, while the following macros also act on it.
 - \pcol@output@start moves it to \@dbldeferlist because it is created before \begin{paracol}.
 - \pcol@startpage uses it as the interface with \@addtodblcol of 2015 or later version of LATEX as discussed in item-(3) of §1.8.
 - \pcol@setcurrcol and \pcol@igetcurrcol saves/restores it into/from $\kappa_c(\lambda_d)$, respectively.
 - \pcol@makefcolelt $\langle flt \rangle$ returns $\langle flt \rangle$ to the list if $\langle flt \rangle$ cannot be put in the float column which the macro is working on.

- \pcol@measurecolumn examines its emptiness to let \ifpcol@dfloats = true iff not empty.
- \pcol@output@end lets it have \@dbldeferlist so that it processed as column-wise floats after \end{paracol}.
- $\label{eq:list} $$ an internal macro having the list of column-wise floats which is decided to be put at the top of the current column-page by float environments or by \pcol@trynextcolumn. This list is scanned by \pcol@cflt if its invoker \pcol@combinefloats finds the macro is not empty. The list is also scanned by \pcol@makecol, \pcol@output@switch and \pcol@measurecolumn using \pcol@addflhd for the measurement of the combined size of top floats, while \pcol@setcurrcol and \pcol@igetcurrcol saves/restores the list into/from <math display="inline">\kappa_c(\lambda_t)$ respectively. In addition our macros may add an element or build the entire list in the following two cases. One case is for a synchronization for which \pcol@synccolumn lets the main vertical list in $\kappa_c(\beta^b)$ be a float, namely MVL-float to be added to this list. Another case is for a float column in the last page for which \pcol@makefcolumn and \pcol@makefcolelt build this list for deferred floats. In the latter case, the list is scanned by \pcol@makefcolpage invoked from \pcol@makefcolumn itself, \pcol@flushcolumn and \pcol@makeflushedpage.
- \@midlist is an internal macro having the list of in-text floats which has already been put in the current column-page but is kept to check the ordering of the succeeding floats. The list is emptied by \pcol@makenormalcol after returning all elements in it to \@freelist, while \pcol@setcurrcol and \pcol@igetcurrcol saves/restores the list into/from $\kappa_c(\lambda_m)$ respectively.
- \f@depth is an internal macro having 1sp or being \let-equal to \z@ to specify the float category, page-wise or column-wise respectively, which float-related macros work on. As discussed in item-(2) of §1.8, this feature introduced in 2015 version of IATEX is nullified in paracol environments and thus the setting with 1sp done by \@dblfloatplacement is overridden by \pcol@startpage and \pcol@output@clear when they invoke the macro.
- \cl@@ckpt is an internal macro having the list of all counters defined by \newcounter and the counter page. The original usage of this macro is to log the values of all counters into .aux by \include, but we use it to obtain all counters in \pcol@zparacol and \pcol@ globalcounter@s.
- $cl@.\theta$ is an internal macro having the list $\zeta(\theta)$ of descendant counters of the counter θ whose increment by stepcounter lets them 0. The macro pcol@remctrelt moves it to $pcol@cl@.\theta$ and redefines it to have $pcol@stepcounter{\theta}$.

\reserved@a is an internal macro for temporary use. Its usages are as follows.

- In \pcol@Fe, it is used to keep the cardinality of \@freelist in \pcol@F@n to log it by \pcol@FF after \pcol@F@n is let have another measurement result.
- In \pcol@setpageno, it has Π^+ so that we update Π and $\pi(p_t)$ scanning their original contents.
- In \pcol@getcurrpinfo, it has π(p_t) so that we give its five components to \pcol@getpinfo as its first five arguments.
- In \Coutputpage, it has a sequence of background painting for both left and right parallel-pages to be shipped out outside paracol environment.
- In \pcol@outputpage@ev, it has the expansion result of \meaning\yoko to be compared with \reserved@b having \string\yoko for examining if \yoko is a primitive of underlying T_FX.
- In \pcol@bg@paintregion $\langle a \rangle \langle c \rangle$, it is let have $a' = a \cdot @ \cdot c$ or a' = a, and then referred to by \pcol@bg@paintregion@i to use \pcol@bg@color.a', and by \pcol@bg@addext $\langle z \rangle \{s\} \{d\}$ to use \pcol@bg@ext@.d.@.a'.
- In \pcol@specialoutput, it is \let-equal to \pcol@output@.f corresponding to \outputpenalty = \pcol@op@.f, or \@specialoutput.
- In \pcol@output@start, it is let have a background painting macro \pcol@bg@ paintbox and the definition of a parameter \pcol@bg@textheight for it.
- In \pcol@output@switch, it is \let-equal to \@nobreaktrue or \@nobreakfalse according to \if@nobreak in the leaving column to broadcast it to other columns.
- In \pcol@ifempty(box)(then)(else), it has (then) or (else) according to the emptiness of (box).
- In \pcol@clearcolorstack, it is \defined to put an uncoloring \special by \reset@color for its argument γ_i in \pcol@iscancst.
- In \pcol@restorecst, it is \defined to put a coloring \special in its argument γ_i by \unvbox done in \pcol@iscancst.
- In \pcol@addmarginpar, at first it is made let equal to 0 or C_L according to $c < C_L$ or not. Then it is let have Π^+ to be scanned to find $\pi^m(p)$.
- In \pcol@getmparbottom@i, it is let have one of $M_{\{L,R\}}^{\{l,r\}}$ according to the side margin which the marginal note to be added goes to, and then it is referred to by \pcol@ getmparbottom.
- In \pcol@setmpbelt@i, it is let have what $\pi^m(p)$ should have after the update of a list of marginal notes in it, and then \pcol@setmpbelt updates $\pi(p)$ with the new $\pi^m(p)$ in the macro.
- In \pcol@bias@mpbout{y} and \pcol@getmparbottom@last{y}, it is let have \pcol@bias@mpbout@i{y} and \pcol@getmparbottom@last@i{y} respectively, so that they are invoked in \pcol@do@mpb@all@ii.
- In \colomakeflushedpage , it is let have an invocation of $\colombol{pcolog0paintbox}$ for page-wise floats in $\pi^i(p_t)$ together with the condition of the background painting.
- In \pcol@output@end, it is let have the invocation of \pcol@bg@paintbox for background painting of page-wise footnotes with the condition to do it and a \definition of \pcol@bg@footnoteheight.

- In \pcol@defcomelt(com), it is used to implement $\left| \det \left(com \right) = \left| \operatorname{pcol@com@} \left(com \right) \right|$.
- In \pcol@setcolumnwidth, it is made \let-equal to \pcol@setcolwidth@s or \pcol@setcolwidth@r according to \pcol@columnratioleft = \relax or not.
- In \pcol@setcolwidth@r, it is used to have the fraction r_d being a comma-separated list element in its argument $\langle ratio \rangle$ defined by \columnratio and scanned by a \@for loop.
- In \pcol@setcw@scan $\langle C^0 \rangle \langle C^1 \rangle \{spec\}$, at first it is let have $\langle spec \rangle$, then the result of adding ',' as many as $C^1 C^0$ to the tail, and finally each element in the extended $\langle spec \rangle$ in a \@for loop.
- In \pcol@setcw@getspec@i $\langle default \rangle \langle x'_d \rangle$, it is let have $\langle x'_d \rangle$ from which all space tokens are removed.
- In \pcol@setcw@calcfactors, it is used as a waste basket to throw away (W_T W)/(F × 1 pt) calculated by \pcol@setcw@calcf.
- In $\coldextract@fil@i(n).(m\cdotunit)\Cnil, it has (n).(m\cdotunit), and is referred to by \pcol@extract@fil@ii.$
- In \clicklinesize{ctr} , it is used to have $\langle ctr \rangle$ for the \ifx -comparison with each $\theta \in \Theta^g$.
- In \pcol@remctrelt $\langle \theta \rangle$, it is used to implement \let\pcol@cl@ $\cdot \theta = \cl@ \cdot \theta$,
- In \pcol@removecounter $\langle \Theta' \rangle \{\theta\}$, it is used to have θ for the \ifx-comparison in \pcol@iremctrelt.
- In \pcol@thectrelt $\langle \theta \rangle$, it is used to implement \let\pcol@thectr@ $\cdot \theta$ = \the $\cdot \theta$, and then is made \let-equal to \pcol@thectr@ $\cdot \theta \cdot 0$.
- In $\clustrel lst$, it has $\langle lst \rangle$.
- In \pcol@setctrelt $\langle \theta \rangle \langle val_c(\theta) \rangle$, it is made \let-equal to \pcol@thectr@ $\cdot \theta$ or \pcol@thectr@ $\cdot \theta \cdot c$.
- In \pcol@switchenv, it is used to save \switchcolumn which is redefined in the macro, and then to invoke \switchcolumn with the original definition.
- In \pcol@fntext{text}, it is \let-equal to \pcol@fntextother or \pcol@fntext top according to the footnote $\langle text \rangle$ is deferred or not.
- In \pcol@calcfnctr(num)\@nil, it has the first token of (num) for \ifx-comparison with '+' and '-'.
- In \pcol@twosided[T], it is let have each non-space token in T given by a \@tfor loop.

\reserved@b is an internal macro for temporary use. It is used in the following macros to keep a list shown in parentheses so that we update the list in the scan of list elements.

```
\label{eq:loss} $$ \collector} $$
```

In addition, it is used in the following macros.

- In \pcol@outputpage@ev, it has the expansion result of \string\yoko to be compared with \reserved@a having \meaning\yoko for examining if \yoko is a primitive of underlying T_EX.
- In $\colored bg@paint@ii</code>, it has a token in the arguments <math>K_b$, K_g and K_c of the macro scanned by $\colored bg$.
- In \pcol@output@switch, it is \let-equal to \@afterindenttrue or \@after indentfalse according to \if@afterindent in the leaving column to broadcast it to other columns.
- In \pcol@clearcolorstack, it is \defined to put an uncoloring \special by \reset@color for its argument γ_0^c in \pcol@scancst.
- In \pcol@restorecst, it is \defined to put a coloring \special in its argument γ₀^c by \unvcopy done in \pcol@scancst.
- In \pcol@scancst and \pcol@iscancst, after the reference for the purposes shown in the two items above, it has $M = (m | \gamma_{j,m} \in \Gamma_r, j \ge i)$ for $\gamma_{i,*}^-$ and in the latter is scanned to find m for $\gamma_{i,m}$ in M.
- In \pcol@addmarginpar, it is made let equal to C_L or C according to $c < C_L$ or not.
- In \pcol@bias@mpbout@i{y}\@elt{t}{b}\@nil, it is let have mpar(t + y, b + y), and in \pcol@getmparbottom@last@i{y} $mpar(t_1, b_1) \cdots mpar(t_n, b_n)$ \@nil it is let have mpar(y, y) or $mpar(t_n, b_n)$, so that they are let be a $M_{\{L,R\}}^{\{l,r\}}$ by \pcol@do@mpb@ all@ii.
- In \pcol@setcw@getspec@i(default)(x'_d), it is let have each non-space token in (x'_d) to remove space tokens from it.
- In \pcol@extract@fil@ii(*unit*)\@nil, it is let have (*unit*).
- In \pcol@iremctrelt $\langle \Theta' \rangle \{\theta\}$, it has θ for \ifx-comparison with θ' to be removed from Θ^g or Θ .
- In \pcol@calcfnctr(num)\@nil, it has '+' and then '-' for \ifx-comparison with the first token of (num).
- In \pcol@backgroundcolor@ii, it has \pcol@backgroundcolor@x or \pcol@back groundcolor@z according that the region of background painting and its color is defined or undefined.
- \reserved@c is an internal macro for temporary use. It is used in \pcol@startpage to save \@deferlist in it and then to restore the list from it, and in \pcol@scancst to have \relax or the macro itself to iterate the macro recursively.
- \reserved@d is an internal macro for temporary use. It is used in \pcol@iscancst as a \chardef register to have 0 if m for $\gamma_{i,m}$ is not in the list $M = (n \mid \gamma_{j,n}^- \in \Gamma_r, j \ge i)$, or 1 if found.
- \@gtempa is an internal macro used as a \globally modifiable scratchpad. Its usages are as follows.
 - In $\collinewidth{\collinewidth} box \collinewidth{\collinewidth} box \collinewidth$

- In \pcol@addmarginpar, it is given to \@xnext as the target to have the second and successive elements of \@currlist which we cannot modify.
- In \pcol@zparacol and \pcol@cmpctrelt, it has the list of counters to be synchronized.
- In \pcol@setcw@getspec@i $\langle default \rangle \langle x'_d \rangle$, it is made \@empty or \relax according to x'_d has \fill or not.
- In \pcol@storectrelt, \pcol@savectrelt and \pcol@sscounters, it has the new version of Θ_c.

3 Register Declaration

3.1 \count Registers

Here we declare registers and switches. The first group is for \count registers.

\pcol@currcol The register \pcol@currcol has the zero-origin ordinal c of the column which we were in when \output is invoked. Therefore, for example, in the process of \switchcolumn, the register has c from which we are switching to another column. The register is initialized to be 0 by \pcol@ output@start, and then set to \pcol@nextcol = d by \pcol@restartcolumn to switch to (or stay in) d. Note that these two assignments are \global while other macros may *locally* use the register to, for example, scan all columns $c \in [0, C)$. Besides two macros above, the following macros refer to the register to know which column we are in (or which column is processed by their invokers).

```
\pcol@Log@iii, \pcol@Log@ii, \pcol@FF, \pcol@makecol, \pcol@opcol,
\pcol@bg@columnleft, \pcol@bg@columnwidth, \pcol@bg@columnsep,
\pcol@output@switch, \pcol@getcurrcol, \pcol@setcurrcol,
\pcol@clearcolorstack, \pcol@restorecolorstack, \pcol@addmarginpar,
\pcol@getmparbottom@i, \pcol@setmpbelt@i, \pcol@invokeoutput<sup>134</sup>,
\thecolumn, \pcol@sscounters, \pcol@setctrelt, \pcol@com@switchcolumn,
\pcol@switchcol, \pcol@visitallcols, \pcol@aconlyelt, \pcol@flushclear.
\pcol@columncolor, \normalcolumncolor, \pcol@icolumncolor,
```

Among the macros above, \columncolor and \normalcolumncolor could refer to the register outside paracol environment and thus before the initialization by \pcol@output@start. Therefore, the register is also initialized to be 0 after its declaration to assure safe reference.

The following macros use the register for the scan of all $c \in [0, C)$ by themselves or their invokers.

```
\pcol@output@start, \pcol@output@switch, \pcol@sync, \pcol@flushcolumn,
\pcol@measurecolumn, \pcol@synccolumn, \pcol@makeflushedpage,
\pcol@flushfloats, \pcol@freshpage, \pcol@output@end,
\pcol@synccounter, \pcol@com@syncallcounters, \pcol@stepcounter.
```

The macros $\colored pcolored page and \pcolored pcolored pcolore$

In addition \pcol@ccuse, \pcol@ifccdefined and \pcol@ccxdef refer to the register to have the control sequence \pcol@columncolor $\cdot c = \hat{\gamma}_0^c$ or \pcol@columncolor@box $\cdot c = \gamma_0^c$ where c is for the current column or for all columns depending on their invokers.

¹³⁴Only for logging.

\pcol@ncol The register \pcol@ncol has the number of columns C given as the argument of \paracol, \pcol@ncolleft whose callee \pcol@zparacol being the sole modifier of the register \globally assigns C to the register to give safe reference to \@outputbox invoked after a paracol is closed. In addition for the reference in \@outputbox before the first paracol, the register is initialized with zero after the declaration.

The following macros refer to the register to scan all columns $c \in [0, C)$.

\pcol@checkshipped, \pcol@output@start, \pcol@output@switch, \pcol@sync, \pcol@makeflushedpage, \pcol@freshpage, \pcol@output@end, \pcol@synccounter, \pcol@com@syncallcounters, \pcol@stepcounter, \pcol@visitallcols.

The register \collectleft has C_L being the number of columns in the left *parallel-page* if parallel-paging is in effect, or have C otherwise. Similar to C, the number C_L is given as the optional argument of \collectleft and is \collectleft assigned to the register by the sole modifier \collectleft is found. The reason of the \collectleft assignment and the initial zeroclearing after the declaration is same as that for C, i.e., for the reference in \collectleft outside paracol.

The following macros examines if $C_L < C$, i.e., if parallel-paging is in effect.

\pcol@outputelt, \@outputpage, \pcol@output@start, \pcol@output@flush, \pcol@output@clear, \pcol@makeflushedpage, \pcol@flushfloats, \pcol@output@end, \pcol@zparacol,

In the macros listed above, \clicklinetic{listed} and \clicklinetic{listed} and

They also pass the pair to $\pol@buildcolseprule$ which then passes it to $\pol@bg@paintcolumns$ and $\pol@bg@paintbox$ by binding it to $[C_b^0, C_b^1) = [\pol@bg@from, \pol@bg@to)$ referred to by $\pol@bg@paint@i$ and its callee $\pol@bg@paint@ii$ to define the range of columns to be painted is $[C_b^0, C_b^1)$. Similar passing is done by (our own version of) $\pol@utputpage$, but it directly uses $[0, C_L)$ and $[C_L, C)$ as the sources and the target painting macros are $\pol@bg@paintpage$, $\pol@bg@@paintpage$ and $\pol@bg@paintbox$. Note that C_b^1 is initialized to be $\to C$ because it may be referred to without binding¹³⁵.

The macro $\colored colored c$

 $^{^{135}\}mathrm{This}$ meaningless reference has no harmful side effects.

Similar column-range specification is done for the argument pair $[C^0, C^1)$ of $\pcol@setcolumnwidth invoked from <math>\pcol@setcolwidth@s$, the arguments are passed to the callees $\pcol@setcolwidth@r$ or $\pcol@setcolwidth@s$, the latter of which also passes them to its callee $\pcol@setcw@scan$, to define the width of columns in $[C^0, C^1)$ and their separators.

The other references to C are made by $\col@com@switchcolumn$ and $\col@switchcolumn$ to examine c < C, to wraparound C - 1 to 0 for the former and to complain if $c \ge C$ for the latter.

- \pcol@page The register \pcol@page has the zero-origin ordinal p of the page which we are in. The register is initialized to be 0 not only by \pcol@output@start to give the obvious starting point, but also by \pcol@freshpage for page flushing which clears $\Pi = \pcol@pages$ to give us another type of starting point. Then the register is incremented by \pcol@textpage to advance one page, by \pcol@nextpelt to skip a float page, and by \pcol@startpage for a float page to be created. The other type of updates of the register is done by \pcol@ restartcolumn which lets p be $\kappa_c(\beta^p)$ when we revisit the column c belonging to the page p. Note that, besides these \global updates, \pcol@freshpage also performs local updates but in more weird manner. Besides the updates discussed above, the macros \pcol@getcurrpage, \pcol@ ii, \pcol@otFF, \pcol@makecol, \pcol@opcol, \pcol@stpageno, \pcol@getcurrpage, \pcol@ startcolumn, \pcol@output@switch, \pcol@addmarginpar and \pcol@fntext refer to the register to know which page they are operating on.
- \pcol@basepage The register \pcol@basepage has the ordinal p_b of the base page being the oldest page not shipped out yet. The register is initialized to be 0 by \pcol@output@start and \pcol@ freshpage together with \pcol@page, and then incremented by \pcol@outputelt when it ships the page p_b out. The macros \pcol@setpageno, \pcol@nextpage, \pcol@getcurrpage and \pcol@addmarginpar refer to the register in their scans of Π or Π^+ to know the zero-origin ordinal of the element for the current page p is $p - p_b$.
- - \pcol@nfootnotes The register \pcol@nfootnotes is to accumulate the number of footnotes n_f in a paracol environment. Therefore, it is zero-cleared by \pcol@zparacol, then incremented by \pcol@ ifootnote and \pcol@ifootnotemark for \footnote and \footnotemark, and finally referred to by \endparacol to let \c@footnote = $b_f + n_f$.
 - \pcol@mcid The register \pcol@mcid has the number of pushes of color stack by coloring commands in math mode between two consecutive invocations of \output. The register is zero-cleared by \pcol@

output because we are definitely in the main vertical mode and thus all pops corresponding to pushes in math mode must have been applied to .tex's color stack. Then the register is referred to by \pcol@set@color@push when it is invoked in math mode, to increment it and then examine if it does not exceed the limit \pcol@mcpushlimit to mean the math-mode coloring still can be made. The macro then uses the value of the register as the identifier of the push operation given to \output through an \insertion.

1
2 %% Register Declaration
3
4 \newcount\pcol@currcol \global\pcol@currcol\z@
5 \newcount\pcol@nextcol
6 \newcount\pcol@ncol \global\pcol@ncol\z@
7 \newcount\pcol@ncolleft \global\pcol@ncolleft\z@
8 \newcount\pcol@page
9 \newcount\pcol@basepage
10 \newcount\pcol@toppage
11 \newcount\pcol@footnotebase
12 \newcount\pcol@ncotnotes
13 \newcount\pcol@mcid

3.2 Switches

The second declaration group is for switches.

- \ifpcol@output The switch \ifpcol@output is true iff \pcol@output@start which turns the switch true has been invoked but \pcol@output@end which does false has not yet. Then the switch is examined by \pcol@output to detect an \output request sneaked from outside of the paracol environment. The other users \@outputpage and \pcol@reset@color@pop examine this switch to know if the macro is invoked inside or outside of paracol environment, while the macro \pcol@output@start temporarily turns the switch false when it ships out a page having preenvironment stuff only.
- \ifpcol@nospan The switch \ifpcol@nospan is *true* iff a page p does not have spanning stuff, i.e., $\pi^i(p) = \bot$. It is set by by \pcol@getpinfo for the examination in \pcol@ioutputelt, \pcol@makeflushedpage and \pcol@output@end.
- \ifpcol@sync The switch \ifpcol@sync is true iff \pcol@output@switch is invoked for synchronized columnswitching by \switchcolumn* or its relative environment openers, or pre-flushing column height check prior to page flushing or environment closing. Therefore, the switch is \globally turned true by \pcol@iswitchcolumn and \pcol@sptext for the synchronizing column-switchinging but then temporarily turned false by \pcol@switchcol invoked by them for column-scanning and then turned true again by the macro. For pre-flushing column height check, the macro \pcol@flushclear turns the switch true. The other macro turns this switch is \pcol@output@ switch at the end of which the switch is turned false to go back to the default state. The macros examining this switch are \pcol@output@switch, \pcol@putbackmvl, \pcol@sync, \pcol@invokeoutput (for logging) and \pcol@switchcol.
- \ifpcol@sptextstart The switch \ifpcol@sptextstart is *true* iff \pcol@output@switch is invoked from \pcol@ \ifpcol@sptext sptext prior to a spanning text. That is, the switch is \globally¹³⁶ let *true* and then *false* by

 $^{^{136}}$ Not necessary to be **\global**ly turned but we dare to do that to clearly distinguish that from the local turning in **\pcol@putbackmvl**.

 $\col@sptext$ before and after the invocation of synchronized $\col@switchcol</code> prior to the spanning text. Then the switch is examined by <math>\col@putbackmvl</code> after the synchronization to save the$ *pre-spanning-text stuff* $, being all stuff in main vertical list prior to the synchronization, so that the spanning text is split from the stuff and is captured afterward by <math>\col@makecol$ and/or $\col@output@switch$. The macro also locally turns the switch *false* if it does not follow the synchronization, i.e., its invocation is for column-scanning or is caused by pre-synchronization page break, to do the saving only when it follows the synchronization. The switch is also examined in $\col@output to inhibit$ the warning and forced page break even when $\kappa_0(\beta^r) = \colroom < 1.5\baselineskip$, because we may let it have a small value when the spanning text starts near the page bottom to capture the text portion in the page by $\col@makecol$. In addition, it is examined by $\col@switchcol to invoke <math>\col@colpream c$, where c = -1 if *true* or $c = \col@currcol otherwise$.

The macro \pcol@sptext then \globally turns another switch \ifpcol@sptext true before putting the spanning text into the main vertical list so that \pcol@makecol for the page break in the text and \pcol@output@switch for closing capture the text to place it appropriately especially when column-swapping is in effect. Then the switch is \globally turned false by \pcol@ output@switch to give the default state after it broadcasts \if@nobreak, \if@afterindent and \everypar to all columns.

- \ifpcol@clear The switch \ifpcol@clear is true iff \pcol@output@switch is invoked for pre-flushing column height check, page flushing or environment closing. Therefore, the switch is turned true by \pcol@flushclear in the first case, and by \pcol@makeflushedpage in the latter two. These two macros also turned the switch false after the direct/indirect invocation of \pcol@output@ switch to give the default state. The switch is examined by \pcol@output@switch and its descendants \pcol@sync, \pcol@flushcolumn and \pcol@synccolumn for synchronization, and by \pcol@invokeoutput for logging.
- \ifpcol@flush The switch \ifpcol@flush is turned *true* by \pcol@sync iff it finds that the page to be synchronized or to be flushed is too tall because the sum of the total height of top floats and main text in a column and that of bottom floats and footnotes in another column is larger than $\pi^h(p_t) - v^f - V_E$, where v^f is the total height-plus-depth of the page-wise footnotes if p_t has them or 0 otherwise, and V_E is the amount given by \ensurevspace in synchronization or 0 in flushing. Then the switch is examined in \pcol@sync itself to restart the tallest column if *true*, in \pcol@putbackmvl to check if a spanning text is really to start, in \pcol@switchcol to have a explicit page break in each column if *true*, and in \pcol@flushclear also to have a page break if *true*. The last examiner \pcol@flushclear may turn the switch *true* when it is invoked from \endparacol if the last page leaves deferred and non-merged page-wise footnotes for which an explicit page break is also required.
- $\label{eq:lipcoloutputflt} \end{subscript{blt}} \$

\ifpcol@lastpage The switch \ifpcol@lastpage is used to know whether the following macros work on the *last* \ifpcol@lastpagesave *page* of a paracol environment to do special operations if so.

- \pcol@combinefloats adds \textfloatsep below bottom floats of each column if any so that the floats are well separated from the post-environment stuff.
- \pcol@sync examines V'_P instead of V_P for the pre-flushing column height check.
- \pcol@makefcolumn tries to make deferred floats as top floats.
- \pcol@makeflushedpage builds a short page of V'_P tall, leaves spanning stuff from shipout if $V'_P = \pcol@colht = -\infty$ so that it becomes a float in post-environment stuff, and leaves page-wise footnotes untouched if merged footnote typesetting is in effect. This macro itself turns this switch *false* if \ifpcol@dfloats = *true* to mean one or more columns in the last page have deferred column-wise floats and thus the last page must be *full size*.
- \pcol@imakeflushedpage leaves the background of page-wise footnotes unpainted, and lets the depth of the last page be 0 in background painting and packing of column-pages.

The switch is initialized to be *false* by \pcol@zparacol, then turned *true* by \endparacol, and then finally turned *false* by \pcol@output@end again for float pages following the last page if any. The macro \pcol@flushcolumn saves the switch into \ifpcol@lastpagesave then turning it *false* during it works on column-pages in non-top and thus non-last pages to keep \@makecol and \pcol@makefcolumn from misunderstanding the pages are last, and then restore the switch when the macro reaches to the top page. This saving and temporary turning *false* is also done in \pcol@flushclear when it forces a page break so that the \output routine working on the broken non-last page correctly recognizes that. Another temporary turning is made by \pcol@makenormalcol but in reverse to let the switch be *true* so that its indirect callee \pcol@combinefloats puts a vertical skip of \textfloatsep below the bottom floats in pre-environment stuff.

- \ifpcol@scfnote The switch \ifpcol@scfnote is turned true by \pcol@fnlayout@p and \pcol@fnlayout@m
 (through \pcol@fnlayout@p) to indicate footnotes in all columns are merged and page-wise,
 while \pcol@fnlayout@c turns it false to make footnote typesetting column-wise, being default
 as well. The switch is examined by the following macros to do special operations for page-wise
 footnotes if it is true.
 - \pcol@makecol shrinks \@colht and put the stretch/shrink factor of \skip\footins at the bottom of the column-page to be built by the macro if the page has footnotes. If the column-page is in the top page p_t , the macro also saves \footins into \pcol@currfoot which then will be saved into $\pi^f(p_t)$ by \pcol@startpage, or \footins is discarded otherwise.
 - \pcol@startcolumn, if it is invoked from \pcol@output to start a column-page in a page p, \inserts π^f(p) through \footins, and also the deferred footnotes in Φ by \pcol@ deferredfootins, if p = p_t.
 - \pcol@output@switch saves \footins into $\pi^f(p_t)$ if the macro is to leave a column-page in the top page, or discards it otherwise.
 - \pcol@restartcolumn to restart a column-page in a page p \inserts $\pi^{f}(p)$ through \footins, and also the deferred footnotes in Φ by \pcol@deferredfootins, if $p = p_t$.
 - \pcol@sync examines whether the total height of page-wise footnotes is too large to let them reside in the page to be synchronized or flushed as a whole.

- \pcol@zparacol redefines \footnoterule so that it refers to \textwidth rather than \columnwidth to determine the width of the rule above footnotes.
- \pcol@fntext invokes \pcol@fntextother to add the footnote given to it to Φ as a deferred footnote if $p < p_t$.
- \pcol@fntextbody lets \hsize be \textwidth rather than \columnwidth to typeset the footnote given to it.
- \ifpcol@mgfnote The switch \ifpcol@mgfnote is turned true by \pcol@fnlayout@m to indicate footnotes in the starting page and last page of a paracol environment are merged with those in pre- and post-environment stuff, while \pcol@fnlayout@p and \pcol@fnlayout@c turn it false to put them above/below the columns in the starting/last page respectively, being default as well. The switch is examined by the following macros to do special operations for merged page-wise footnotes if it is true.
 - \pcol@makenormalcol leaves \footins untouched rather than putting it as a part of pre-environment stuff.
 - \pcol@makeflushedpage leaves \footins untouched rather than putting it as a part of the last page of paracol if it works on the page.
 - \endparacol does not let \pcol@flushclear examine the existence of deferred footnotes in pre-flushing column height check for the last page.
- $\label{eq:lipcol@fncounteradjustment} $$ the API macro \fncounteradjustment is turned true by the API macro \fncounter adjustment, which is also invoked from \pcol@fnlayout@p and \pcol@fnlayout@m (through \pcol@fnlayout@p), to let \c@footnote = b_f + n_f by \endparacol. The macro \nofncounter adjustment turns the switch false to give the default state.$
 - \ifpcol@inner The switch \ifpcol@inner is turned false by \pcol@zparacol to mean we are outside any \vboxes, while the macro also lets \everyvbox in the paracol environment has the operation to turn the switch true so that it is true whenever we are in a \vbox. The switch is examined by \pcol@set@color@push and \pcol@icolumncolor, the former of which also turns it true if we are in restricted horizontal mode, to make an \output request for color stack manipulation and, in the former, to reserve the stack popper by \aftergroup, iff the switch is false.

 - \ifpcol@havelastpage The switch \ifpcol@havelastpage is, after an initial false, \globally turned true by \pcol@
 output@end if it finds the last page of the paracol environment is connected to the postenvironment stuff, or false otherwise. Then the switch is examined by (our own version of)
 \@outputpage which paints the background of the page to be printed iff the switch is true
 because a part of the page was produced by a paracol environment. Then the macro \globally
 turns the switch false because so far background painting should be disabled.

\ifpcol@paired The switch \ifpcol@paired is true if the parallel-paged typesetting should be done in paired mode in which the pair of left and right parallel-pages comprises a virtual page, while it is *false* if non-paired to treat the left and right pages as individual ones. Therefore, the switch is for the number of columns in the left parallel-page followed by *, or turned *true* otherwise by \paracol for giving default or by \pcol@zparacol if it finds $C_L \ge C$ to mean parallel-paging is not in effect in reality¹³⁷.

> Then the switch is examined by \pcol@setpnoelt and \pcol@startpage so that, if the switch is false, they let page(q) = page(q-1) + 2 where $\kappa_0(\beta^p) < q \leq p_t$ in the former and $q = p_t$ in the latter, instead of page(q) = page(q-1) + 1 in the usual true case, because the left/right pair of parallel-pages is treated as two pages rather than one.

> The other macros \pcol@ioutputelt, (our own version of) \@outputpage, \pcol@output@ start, \pcol@imakeflushedpage, \pcol@iflushfloats and \pcol@output@end also refer to the switch so that, if *false*, they temporarily let $\cepage = page(p) + 1$ in building the shipout image of the right component of the parallel-page pair of the page p in order to have the appropriate page number parity for the right component. Among them, \Coutputpage has another mode dependant operation, if the switch is *true*, to decrement \c@page by one before shipping out the right component to cancel the increment in the ship-out process of the left component. The macro \pcol@addmarginpar also examines the switch to decide the margin for marginal notes in non-paired parallel-pages. Another examiner \pcol@zparacol lets ifpcol@swapcolumn = false only in the paracol environment to start if the switch is truebecause column-swapping is meaningless in non-paired parallel-paging.

\ifpcol@swapcolumn The switch \ifpcol@swapcolumn, \ifpcol@swapmarginpar and \ifpcol@bg@swap specify \ifpcol@swapmarginpar that, if true, columns, marginal notes, and background painting in even numbered pages are \ifpcol@swap swapped, respectively. That is, \ifpcol@swapcolumn lets columns be put from right to left, \ifpcol@bg@@swap \ifpcol@swapmarginpar lets marginal notes go to the opposite side from that in odd numbered pages, and \ifpcol@bg@swap makes background painting mirrored.

> Besides the initial setting to let them false \globally after the declaration, the switches are \globally turned false by \pcol@twosided for the cases in which API macro \twosided does not have 'c', 'm' or 'b' in its optional argument respectively, and then \globally turned true by $\col@twosided@k$ ($k \in \{c, m, b\}$) which is invoked when the argument contains 'c', 'm' or 'b' respectively, or the API macro does not have the argument at all¹³⁸. The switch \ifpcol@swapcolumn is also turned false by \pcol@zparacol but locally if non-paired parallelpaging is specified because column-swapping is meaningless in the environment. Another modifier is (our own version of) \@outputpage, but setting and examining the switch in this macro is also local and is to decide the ship-out order of left and right parallel-pages.

> Besides the local use by \Coutputpage, \ifpcol@swapcolumn is then examined by the following macros to do special operations if it is *true* and we are in an even numbered page.

- \pcol@swapcolumn to reverse the order of column visiting in \pcol@ioutputelt, \pcol@ imakeflushedpage and \pcol@iflushfloats.
- \pcol@shiftspanning to shift a spanning text to the left edge of text area.
- \pcol@bg@paint@ii to mirror the background painting of columns and column-separating gaps.

¹³⁷The initialization to let the switch *false* is not necessary because it is examined only after the first \paracol even in the \Coutputpage outside paracol environment, but we dare to do this for the sake of clarity.

¹³⁸\ifpcol@swapcolumn is also turned *true* and *false* by backward compatible API macros \swapcolumnineven pages and \noswapcolumninevenpages respectively.

On the other hand, examiners of \ifpcol@swapmarginpar and \ifpcol@bg@swap are sole for each, namely \pcol@addmarginpar and \pcol@bg@paint@i respectively. If each switch is *true* and we are in an even numbered page, the former reverses \if@firstcolumn from the value having been set for non-swapping case, while the latter mirrors the background painting of the regions excepting columns and column-separating gaps.

A related switch \ifpcol@bg@@swap is let be *true* if \ifpcol@swapcolumn or \ifpcol@bg@ swap is *true* and we are working on a even numbered page by \pcol@bg@swappage for mirrored background painting of columns and column-separating gaps, or other regions respectively, and then examined by \pcol@bg@paintregion@i for mirroring.

- \ifpcol@bg@painted The switch \ifpcol@bg@painted is \globally turned false at the beginning of \pcol@bg@ paint@i, and then \globally turned true by \pcol@bg@paintregion if it paint the region specified by its argument, i.e., \backgroundcolor for the region is declared. Then the switch is examined by \pcol@bg@paint@i to combine the painted region with others, by (our own version of) \@outputpage and \pcol@outputpage@r to incorporate painted regions into shipout image.

 - \ifpcol@dfloats The switch \ifpcol@dfloats is *true* iff one or more columns (in a last page) have deferred column-wise floats. Therefore, it is turned *false* by \pcol@sync before it invokes \pcol@measurecolumn which turns it *true* when it finds a column c such that $\kappa_c(\lambda_d) \neq \emptyset$. Then the switch is examined by \pcol@makeflushedpage to make a last page *full size*, and by \pcol@output@end to flush these floats.

14 \newif\ifpcol@output \global\pcol@outputfalse 15 \newif\ifpcol@nospan 16 \newif\ifpcol@sync \pcol@syncfalse 17 \newif\ifpcol@sptextstart \pcol@sptextstartfalse 18 \newif\ifpcol@sptext \pcol@sptextfalse 19 \newif\ifpcol@clear \pcol@clearfalse 20 \newif\ifpcol@flush 21 \newif\ifpcol@outputflt 22 \newif\ifpcol@lastpage 23 \newif\ifpcol@lastpagesave 24 \newif\ifpcol@scfnote \pcol@scfnotefalse 25 \newif\ifpcol@mgfnote \pcol@mgfnotefalse 26 \newif\ifpcol@fncounteradjustment \pcol@fncounteradjustmentfalse 27 \newif\ifpcol@inner 28 \newif\ifpcol@firstpage 29 \newif\ifpcol@havelastpage \global\pcol@havelastpagefalse 30 \newif\ifpcol@paired \global\pcol@pairedtrue 31 \newif\ifpcol@swapcolumn \global\pcol@swapcolumnfalse 32 \newif\ifpcol@swapmarginpar \global\pcol@swapmarginparfalse 33 \newif\ifpcol@bg@swap \global\pcol@bg@swapfalse 34 \newif\ifpcol@bg@@swap 35 \newif\ifpcol@bg@painted 36 \newif\ifpcol@bfbottom

```
37 \def\reserved@a{pLaTeX2e}
38 \ifx\reserved@a\pfmtname \pcol@bfbottomfalse \else \pcol@bfbottomtrue \fi
39 \newif\ifpcol@dfloats
```

3.3 \dimen and \skip Registers

The next declaration group is for six \dimen and one \skip registers.

- \pcol@prevdepth The \dimen register \pcol@prevdepth is set to the depth of the last item added to the main vertical list of column c from which we switch to another column d, i.e., \prevdepth seen in \pcol@invokeoutput before \output request. The value of the register is then set into \prevdepth also by \pcol@invokeoutput after \output for the column d. The value of the register is stored in $\kappa_c(\delta)$ by \pcol@setcurrcol and then restored into the register by \pcol@ igetcurrcol for the use in \pcol@invokeoutput above and in \pcol@measurecolumn, which may let the register and $\kappa_c(\delta)$ have ∞ if the column-page c is empty. The register is also updated by \pcol@synccolumn for empty main vertical list case, and by \pcol@output@end to be set into \prevdepth for the first vertical item of post-environment stuff.
 - \pcol@colht The \dimen register \pcol@colht has V'_P being the height of the tallest column in the last page taking \textfloatsep below bottom floats into account if any. The register is initialized to be $-\mbox{maxdimen}$ by \pcol@sync and then is examined and updated in \pcol@ measurecolumn to find the tallest column. Besides the internal use of this exploration, its result is referred to by \pcol@sync as the threshold of pre-flushing column height check, and by \pcol@makeflushedpage through its argument given by \pcol@output@end to know the height of multi-column stuff in the last page. The macro \pcol@makeflushedpage also lets the register have 0 if the last page has nothing but non-merged page-wise footnote. The other usage of this register is in \pcol@freshpage to keep the value of \@colht of the page made by \flushpage or \clearpage so that it is given to \@colroom = $\kappa_c(\beta^r)$ of each column c in case a column c' s.t. c' < c made another page for float columns updating \@colht.

```
\col@lrmargin The \dimen register \pcol@lrmargin is let have <math>\mu = \textwidth - \linewidth by \pcol@ \pcol@bg@leftmargin zparacol, so that \linewidth for column c is let have <math>w_c - \mu by \pcol@invokeoutput, which also sets \parshape if \mu > 0.
```

The other usage of this register is to have the left or right margin for background painting in the alias \pcol@bg@leftmargin for strict local use in \pcol@bg@paint@i and its descendent macros for background painting. That is, the register is aliased as \pcol@bg@leftmargin by \pcol@bg@paint@i, let have left or right margin by \pcol@bg@swappage, and then referred to by \pcol@bg@pageleft.

- \pagerim The API \dimen register \pagerim has the size of page rims specified by users. Since the rims
 are the area for which background painting is inhibited, the register is used in area specification
 macros \pcol@bg@paperwidth, \pcol@bg@paperheight, \pcol@bg@pageleft and \pcol@bg@
 pagetop, in which the register has the negative counterpart of the specified value set by \pcol@
 bg@paint@i.
- \pcol@topskip The \skip register \pcol@topskip keeps the value of \topskip at \begin{paracol} for the ordinary usage of \topskip which may have 0 in the starting and last page temporarily. After the initialization by \pcol@zparacol, it is referred to by \pcol@getpinfo for pages without spanning stuff and thus pre-environment stuff, by \pcol@startpage to let \topskip and $\pi^t(p)$ has it for non-starting page p, by \pcol@output@start for the second page if it finds pre-environment stuff is too large to combine with the multi-column stuff, and by \endparacol to recover \topskip for the pages following the last page.
- \belowfootnoteskip The API \skip register \belowfootnoteskip has the amount of the space added below non-merged pre-environment footnotes. The register is initialized with the default 0 pt, and then used in \pcol@output@start to measure the room in the first page, and in \pcol@ combinefootins to add the space.

40 \newdimen\pcol@prevdepth
41 \newdimen\pcol@colht
42 \newdimen\pcol@textfloatsep
43 \newdimen\pcol@Irmargin
44 \newdimen\pagerim \pagerim\z@
45 \newskip\pcol@topskip
46 \newskip\belowfootnoteskip \belowfootnoteskip\z@

3.4 \box Registers

The next declaration group is for the following \box registers.

- $\label{eq:product} $$ The \box register \pcol@topfnotes is the implementation of $$ $$ to have the list of deferred footnotes. The register is made void by \pcol@output@start and then is made grown by \pcol@fntextother with a deferred footnote added by the macro. The macro \pcol@deferredfootins invoked from \pcol@startcolumn and \pcol@restartcolumn tries to \insert the contents of the register through \footins but may keep some of trailing ones in it if the total height of the footnotes is too large, while \pcol@output@end does the \insertion without height capping. The macro \endparacol with non-merged page-wise footnote type-setting also refers to the register to pass it to \pcol@flushclear as its argument so as to make an explicit page break if the register has some deferred footnotes.$
 - \pcol@prespan The \box register \pcol@prespan keeps the pre-spanning-text stuff during a spanning text is processed by TEX and our own \output routine. That is, the macro \pcol@putbackmvl saves the contents $\kappa_0(\beta^b)$ of the column 0 to be restarted into the register instead of putting it back to the main vertical list, or makes the register \perp if the column has nothing, when the restart follows the synchronization with \ifpcol@sptextstart = true. Then the contents of the register is put back to the main vertical list together with the box having spanning text after its vertical size is registered in the list $\pi^s(p)$ of spanning text positions and heights, by \pcol@makecol when the text sees a page break, or by \pcol@output@switch when the text is completed.
- \pcol@rightpage The \box register \pcol@rightpage is used to build (a part of) the ship-out image of a right parallel-page in it. The macros;

\pcol@outputelt, \pcol@ioutputelt, \pcol@makeflushedpage, \pcol@flushfloats, \pcol@output@flush, and \pcol@output@clear

work on the register together with \@outputbox for the left parallel-page to pass both of them to (our of version of) \@outputpage. The macro \pcol@output@end also uses the register to paint the background of the empty counterpart of non-merged page-wise footnotes in it, or to make the register \perp when it have an empty last page but with spanning stuff of page-wise floats. After closing a paracol environment, the contents of the register will be shipped out by \@outputpage invoked outside paracol environment when the post-environment stuff sees a page break, or referred to by \pcol@output@start as the pre-environment stuff in the right parallel-page. This right pre-environment stuff then will be combined with column-pages in the right parallel-page by \pcol@ioutputelt or \pcol@imakeflushedpage for shipping-out, or by the latter indirectly invoked from \pcol@output@end as the last right parallel-page again. Therefore the \setbox of the register in \pcol@output@start, \pcol@makeflushedpage, \pcol@imakeflushedpage and \pcol@output@end must be done \globally¹³⁹.

 $\label{eq:local_local_stack@saved} The \box register \pcol@colorstack@saved is Γ_s to keep the color context Γ^c of column c until its current column-page becomes non-empty to avoid that the column-page only has coloring \specials for color stack establishing and rewinding to let \pcol@ifempty misjudge the column-page is non-empty. It is let have γ_0^c, if defined, and Γ by \pcol@savecolorstack invoked from \pcol@startcolumn and \pcol@output@start, and from \pcol@restartcolumn through \pcol@putbackmvl when we know or find the (re)starting column-page is empty. The macro \pcol@putbackmvl also makes the \box register $\prol@start_ when the restarting column-page is not empty and thus the column-page has had coloring \specials for establishing color context at its beginning. Then the register is given to \pcol@restorecst by \pcol@clearcst@unvbox to put leading coloring \specials for establishing of the column-page when we complete it by \pcol@opcol or leave from it by \pcol@output@switch.$

\pcol@tempboxa The \box register \pcol@tempboxa is used to have stuff temporarily as follows.

- The macro \pcol@buildcolseprule and its callee \pcol@buildcselt builds the columnseparating rule in the register for a page to be shipped out, while its contents is put into each column-separating gap by \pcol@hfil.
- In (our own version of) \Coutputpage, the register has the background painting of the (left parallel-) page, which is inserted into the ship-out image by its callee \pcolC outputpageCl through \everyvbox and its contents \pcolCoutputpageCev.
- In \pcol@scancst and its callee \pcol@iscancst to scan Γ_r^c , Γ^c or Γ_s , the sequence of (un)coloring \specials to be put into the main vertical list is build in it.
- \pcol@tempboxb The \box register \pcol@tempboxb is used in \pcol@iscancst to extract the top (last) element of Γ , Γ_r or Γ_s .

47	\newbox\pcol@topfnotes
48	\newbox\pcol@prespan \setbox\pcol@prespan\box\voidb@x
49	\newbox\pcol@rightpage \global\setbox\pcol@rightpage\box\voidb@x
50	\newbox\pcol@colorstack@saved
51	\newbox\pcol@tempboxa
52	\newbox\pcol@tempboxb
30 -	

 $^{^{139}}$ The \global setting in \pcol@makeflushedpage and \pcol@imakeflushedpage, together with \@outputbox which does not need \global assignment, is also required by the sake of simplicity in its implementation, incidentally.

3.5 \insert Register Set

The next declaration is for the following \insert register set.

\pcol@colorins The register set \pcol@colorins is to \insert a \vbox containing a (un)coloring \special
for color pushing or popping, or the definition of a new default color of the current column. In
order to make it sure that an \insertion does not affect \pagetotal and is given to \output
with \box255 containing the corresponding coloring \special put in the main vertical list,
 \count\pcol@colorins and \skip\pcol@colorins are let be 0, while \dimen\pcol@colorins
is let be \maxdimen to allow a column-page to have virtually infinite number of \insertions.

The <code>\insertion</code> is done by <code>\pcol@icolumncolor</code> for a default color definition, <code>\pcol@set@color@push</code> for color pushing, and <code>\pcol@reset@color@pop</code> and <code>\pcol@reset@color@mpop</code> for color popping in non-math and math mode respectively. Then <code>\inserted \vboxes</code> are packed into <code>\box\pcol@colorins</code> and is given to <code>\output</code> as Γ_r to be scanned by <code>\pcol@clearcolorstack</code> to reform it as Γ , and then scanned by <code>\pcol@restorecolorstack</code> or saved into $\Gamma_s = \pcol@colorstack@saved$ by <code>\pcol@savecolorstack</code>. The register is also referred to by <code>\pcol@scancst(box)</code> to examine if $\langle box \rangle$ is this register or <code>\pcol@colorstack@saved</code>, and is made \perp by <code>\pcol@output@end</code> after the final reestablishment of the color stack.

53 \newinsert\pcol@colorins

54 \count\pcol@colorins\z@ \skip\pcol@colorins\z@ \dimen\pcol@colorins\maxdimen

3.6 \toks Register

The last declaration is for the following \toks register.

\pcol@everyvbox The register \pcol@everyvbox acts as \everyvbox in paracol environments. That is, by \pcol@zparacol, \everyvbox is made \let-equal to this register so that updates and references of \everyvbox is made to this register, while the real \everyvbox is let have the reference to the register and \pcol@innertrue to make \ifpcol@inner = true in every \vbox. Besides \pcol@zparacol, the register is referred to by \pcol@restoreeveryvbox to examine if it has been \globally updated, i.e., its contents is not \pcol@dummytoken.

```
55 \newtoks\pcol@everyvbox
56
```

4 Logging Tools

Prior to the \definitions of macros to implement paracol's functions, we define a few macros for debug logging.

\pcol@ShowBox The macro \pcol@ShowBox $\langle b \rangle$ puts a logging \message showing the height, depth and width of the \box (or \insert) register b, or "(VOID)" if $b = \bot$. Then, if $b \neq \bot$, b's contents is dumped into .log file making overfull intentionally by putting b into \box0 of null height, together with \vskip of 1 pt if b's height is 0, with setting \vfuzz = 0.

- \pcol@Log(cs){m}{f} is to log the contents of the \insert register f containing footnotes which is referred to by the macro (cs) in a context shown by m. The macro \pcol@Log@ iii (l₁ = 3) logs the detailed contents of f by \pcol@ShowBox, while \pcol@Log@ii (l₁ = 2) just shows the height of f and \pcol@Log@i (l₁ = 1) does nothing.
- \pcol@Logstart{m} and \pcol@Logend{m} put logging \messages 'S:m' and 'E:m' respectively to show the beginning and end of a procedure in the macro whose name is at the head of m, if l₂ = 2 and thus they are \let-equal to \pcol@Logstart@ii and \pcol@Logend@ii. If l₂ = 1, \pcol@Logstart@i and \pcol@Logend@i do nothing.
- \pcol@Logfn{m} puts a logging \message m whose head is the macro name for footnotes whose information such as the ordinal number of the footnote processed by the macro may be shown in m as well, if l₃ = 2 and thus it is \let-equal to \pcol@Logfn@ii. If l₃ = 1, \pcol@Logfn@i does nothing.

```
57 %% Logging Tools
58
59 \def\pcol@ShowBox#1{%
    \ifvoid#1\message{(VOID)}%
60
61
    \else
      \mbox{wessage}(\the\t#1+\the\dp#1)x(\the\wd#1)}%
62
      {\vfuzz\z@ \showboxdepth\@M \showboxbreadth\@M
63
       \setbox\z@\vbox to\z@{\ifdim\ht#1=\z@ \vskip1\p@\fi \copy#1}}%
64
    \fi}
65
66 \def\pcol@LogLevel#1#2#3{%
    \pcol@iLogLevel{#1}{pcol@Log}%
67
    \pcol@iLogLevel{#2}{pcol@Logstart}%
68
    \pcol@iLogLevel{#2}{pcol@Logend}%
69
    \pcol@iLogLevel{#3}{pcol@Logfn}}
70
71 \def\pcol@iLogLevel#1#2{%
72
    \expandafter\let\expandafter\reserved@a
      \csname #2@\romannumeral#1\endcsname
73
    \expandafter\let\csname #2\endcsname\reserved@a}
74
75 \def\pcol@Log@iii#1#2#3{\message{\string#1{#2%
76
      (\number\pcol@page:\number\pcol@currcol/\number\pcol@toppage)}}%
    \pcol@ShowBox#3\message{end\string#1}}
77
78 \def\pcol@Log@ii#1#2#3{\message{\string#1{#2%
      (\number\pcol@page:\number\pcol@currcol/\number\pcol@toppage)}=\the\ht#3}}
79
80 \def\pcol@Log@i#1#2#3{}
81 \def\pcol@Logstart@ii#1{\message{S\string#1}}
82 \def\pcol@Logend@ii#1{\message{E\string#1}}
83 \def\pcol@Logstart@i#1{}
84 \def\pcol@Logend@i#1{}
85 \def\pcol@Logfn@ii#1{\message{\string#1}}
86 \def\pcol@Logfn@i#1{}
87 \pcol@LogLevel111
88
```

debugging *memory leak* caused by missing a release of a register back to \@freelist is that the resulting shortage is revealed long after the leakage to make it hard to find the point of the leakage.

The set of macros is to help such debugging by logging the acquire and release of \insert registers into a file named $\langle job \rangle$.fls associated with \pcol@F@write where $\langle job \rangle$ is given by \jobname. After opened when paracol is loaded, the file is written by \pcol@FF{ m_a }{ m_b } with a line of the following form with text messages m_a and m_b , where p = \pcol@page, c =\pcol@currcol, $p_t =$ \pcol@toppage, $\pi = page(p) =$ \c@page, and $n_b =$ \pcol@F@n is the cardinality of \@deferlist counted by \pcol@F@count.

$$\langle m_a \rangle (\langle p \rangle : \langle c \rangle / \langle p_t \rangle : \langle \pi \rangle) = \langle n_b \rangle \langle m_b \rangle$$

The argument $\langle m_b \rangle$ is empty when $\col@FF$ is invoked from $\col@F\langle m_a \rangle$ for snapshot, while $\langle m_b \rangle = `<=\langle n_b \rangle$ ' when invoked from $\col@Fe\langle m_a \rangle$ paired by $\col@Fb = \col@F@count$ by which the cardinality of $\col@Feelist$ is given to $\langle n_b \rangle$ through $\col@F@n$ and then $\col@Feelist$ a. Therefore, by the pair of $\col@Fb$ and $\col@Fe$, the consumption or restitution in a series of operations surrounded by the pair is logged in the file.

In the production version, the logging is disabled of course by \letting \pcol@F and \pcol@ Fe be \@gobble and \pcol@F be \relax, while the open of \pcol@F@write is disabled as well by a pair of \iffalse and \fi.

```
89 \iffalse
90 \newwrite\pcol@F@write
91 \immediate\openout\pcol@F@write\jobname.fls
92 \fi
93 \def\pcol@F#1{\pcol@FF{#1}{}}
94 \def\pcol@FF#1#2{\pcol@F@count
     \immediate\write\pcol@F@write{#1(\number\pcol@page:\number\pcol@currcol/%
95
       \number\pcol@toppage:\number\c@page)=\pcol@F@n #2}}
96
97 \def\pcol@F@count{{\@tempcnta\z@
       \def\@elt##1{\advance\@tempcnta\@ne}\@freelist
98
       \xdef\pcol@F@n{\number\@tempcnta}}}
99
100 \let\pcol@Fb\pcol@F@count
101 \def\pcol@Fe#1{{\let\reserved@a\pcol@F@n \pcol@FF{#1}{<=\reserved@a}}}</pre>
102 \let\pcol@F\@gobble
103 \let\pcol@Fb\relax
104 \let\pcol@Fe\@gobble
105
```

5 \output Routine

\pcol@ovf Before giving the definitions of macros in \output routine, we define the macro \pcol@ovf invoked if \@freelist is empty on an acquisition of an \insert by \@next and thus we have to abort the execution by \PackageError with a message notifying the shortage. The additional help message is \@ehb as in \@fltovf. This macro is used in \pcol@opcol, \pcol@startpage, \pcol@output@start, \pcol@output@switch, \pcol@iscancst, \pcol@savefootins, \pcol@ flushcolumn, \pcol@synccolumn, \pcol@output@end and \pcol@icolumncolor.

```
106 %% \output Routine
107
108 \def\pcol@ovf{%
109 \PackageError{paracol}{Too many unprocessed columns/floats}\@ehb}
110
```

- $\label{eq:local_cont} $$ \end{tabular} The macro \collocal_contput is the paracol's version of \output which is let have this macro as its sole token by \collocal_cont_control of this macro is same as that of IAT_EX's \output but the following replacements are made^{140}. $$$
 - \@specialoutput → \pcol@specialoutput to process IATEX's genuine functions including the customized marginal note placement, and paracol's own special output functions; starting first page, color context management, column-switching, page flushing with/ without float flushing, and building the multi-column part of the last page.
 - \@makecol → \pcol@makecol for a special care for current column-page having synchronization point and/or page-wise footnotes.
 - $\constant{Qopcol} \rightarrow \constant{Qopcol}$ to hold the current column-page which just has completed.
 - \@startcolumn \rightarrow \pcol@startcolumn to create a new column-page. The argument \@ne is to distinguish the invocation in this macro from that in \pcol@freshpage so that the \insertions of $\pi^f(p)$ and Φ are done only when a new column-page is created with ordinary page break.

In addition, before we start the main body of **\output** routine, we add two operations for coloring. One is to make **\set@color \let**-equal to **\pcol@set@color**, i.e, to let it regain its original definition throughout **\output** routine, because no manipulation of color stack is necessary¹⁴¹. The other is to zero-clear the counter **\pcol@mcid** because we are definitely in the main (non-internal) vertical mode and thus all push/pop pairs of the coloring in math mode have been processed.

Further, before we start the sequence for non-special **\output** request on page breaks, we examine if $\ true$ to mean $\ colCoutputCstart$ has already been invoked in order to cope with \output request sneaking. This sneaking happens when \begin{paracol} is at a critical position of page breaking at which the pre-environment stuff has already exceeds \vsize but TFX cannot make the \output request for the page break at \par at the beginning of \colorbi command just preceding $\ensuremath{\mbox{begin}\mbox{paracol}\)}$. In this case, the request is postponed until TFX see a \penalty less than 10000 and thus it is made with some non-special \outputpenalty greater than -10000 when TFX sees the dummy request of \penalty = -10004 in \pcol@ invokeoutput for \pcol@output@start. At this timing, \pcol@zparacol has already let \output have \pcol@output of course but the request must be processed by original \output because it is made *outside* of the **paracol** environment which has just started. Therefore, if ifpcol@output = false, we have to perform the operation sequence as the original outputdoes. Furthermore, we have to take care of the fact that a few our own settings related to \output routine has already been made in \colorparacol , namely $\ifotwocolumn = true$ and $\combinefloats = \combinefloats$, which should make the macros in the original sequence confused especially by the former. Therefore, we turns if@twocolumn = false and let \Ccombinefloats have the original definition kept in \pcolCCombinefloats¹⁴² temporarily, i.e., only in the group automatically surrounding the invocation of **\output**.

Another addition is to assign $\mbox{Qmaxdepth}$ to $\mbox{maxdepth}$ in order to nullify the temporary setting to 0 done in $\mbox{Qaddtobot}$. By this assignment, in paracol environments T_FX 's

 $^{^{140}\}textsc{Besides}$ the logging with <code>\pcol@Logstart</code> and <code>\pcol@Logend</code>.

 $^{^{141}}$ Though this operation is not necessary because \everyvbox should work for any \set@color because they should be in a \vbox, we dare to do it for clarity.

¹⁴²Though we know \pcol@combinefloats acts exactly as \@combinefloats because \pcol@zparacol initializes \pcol@textfloatsep = ∞ and \ifpcol@lastpage = false. On the other hand, we don't cancel the re\definition of \footnoterule because it should be \textwidth = \columnwidth outside of paracol environments.

page builder always refers to the value in \@maxdepth. Yet another addition is to add \ifpcol@sptextstart = false to the condition for the warning of too short \vsize, because a spanning text can start near the bottom of a page with a small \@colroom less than $1.5 \times$ \baselineskip and thus the warning is unnecessary and inappropriate when \ifpcol@sptextstart = true.

```
111 \def\pcol@output{\let\par\@@par \let\set@color\pcol@set@color
     \global\pcol@mcid\z@
112
113
     \pcol@Logstart{\pcol@output\number\outputpenalty
114
        (\number\c@page:\number\pcol@currcol)}%
115
     \ifnum\outputpenalty<-\@M
116
        \pcol@specialoutput
     \else\ifpcol@output
117
       \pcol@makecol
118
119
       \pcol@opcol
120
       \pcol@startcolumn\@ne
       \@whilesw\if@fcolmade\fi{\pcol@opcol \pcol@startcolumn\@ne}%
121
122
     \else
       \@twocolumnfalse \let\@combinefloats\pcol@@combinefloats
123
       \@makecol
124
       \@opcol
125
       \@startcolumn
126
127
       \@whilesw\if@fcolmade\fi{\@opcol \@startcolumn}%
128
     \fi\fi
129
      \global\maxdepth\@maxdepth
130
     \ifnum\outputpenalty>-\@Miv
        \ifdim\@colroom<1.5\baselineskip
131
          \ifdim\@colroom<\textheight
132
            \ifpcol@sptextstart
133
              \global\vsize\@colroom
134
            \else
135
              \@latex@warning@no@line{Text page \thepage\space
136
                                        contains only floats}%
137
              \@emptycol
138
            \fi
139
140
          \else
141
            \global\vsize\@colroom
142
          \fi
143
       \else
          \global\vsize\@colroom
144
       \fi
145
     \else
146
       \global\vsize\maxdimen
147
148
      \fi
      \pcol@Logend\pcol@output}
149
150
```

6 Completing Column-Page

\pcol@@makecol The macro \pcol@@makecol\d\ is used in \pcol@flushcolumn and \pcol@imakeflushedpage which simply require LATEX's original \@makecol to build the ship-out image of a column-page. The reason why we need our own version is that a variation of LATEX, namely pLATEX for Japanese, carelessly implements its own \@makecol to make the resulting \@outputbox has a
depth larger than $\mbox{maxdepth}$ if the column-page has column-wise footnotes whose last line is unusually deep. To cope with the problem, this macro at first invokes $\mbox{maxecol}$, and then reshape $\mbox{coutputbox}$ assigning $d = \mbox{maxdepth}$ to $\mbox{boxmaxdepth}$ to cap its depth, unless this macro is used for the last page with d = 0 because depth of the last component of the $\mbox{coutputbox}$ is incorporated in \mbox{colht} .

151 %% Completing Column-Page

152

153 \def\pcol@@makecol#1{\@makecol

154 \setbox\@outputbox\vbox to\@colht{\boxmaxdepth#1\unvbox\@outputbox}}

\pcol@makecol The macro \pcol@makecol is invoked solely from \pcol@output to build the shipping image of the current column-page which just has completed in \@outputbox. This macro has two additional functions to its original version \@makecol¹⁴³ invoked in this macro.

> First, if $\kappa_c(\xi) \neq \infty$ to mean the column-page has synchronization points, \@makecol is invoked with a special \definition of \@textbottom to put a vertical skip having 1/10000 fil as its stretch and shrink. This modification is to nullify not only finite stretches (as \raggedbottom does) but also finite shrinks possibly inserted just below the last synchronization point to move up the first visible item upward a little bit if active. Therefore, \flushbottom setting is nullified for column-pages having synchronization points and a small excess from the bottom of a column-page cannot be absorbed by shrinks but visible at the bottom¹⁴⁴. Note that the original definition of \@textbottom is saved in \pcol@textbottom before the invocation of \@makecol and is restored after that¹⁴⁵.

> Second, if $\col@sptext = true$ and c = 0 to mean a spanning text encounters a page break, we have the first half (or second or succeeding part if the text lays across three or more pages) of the text in $\colwed{bx255}$. Therefore, we add an element $span(H_n, h_n)$ to the tail of the list of spanning texts $\pi^s(p_t) = \col@sptextlist$, where H_n is the height of pre-spanning-text stuff in $\colwed{bycol@addflhd}$ with $\kappa_c(\lambda_t) = \colwed{bycol@addflhd}$ with height-plus-depth of $\colwed{bycol@addflhd}$ with h_n are represented in the form of integer and thus we produce them by expansions with \number .

> The addition, however, is not made if $h_n = 0$ because painting its background is harmful if an extension is specified to make the region visible, while not painting or drawing a segment of column-separating rule is very natural. Note that this $h_n = 0$ case includes that in which **\box255** has nothing but its height-plus-depth is non-zero because of discarding leading skips of the spanning text as pre-break skips. This special case is detected by decapsulating **\box255** by **\unvcopy** and examining the height-plus-depth of the result¹⁴⁷. Also note that the list to be added is always for the top page, i.e., $\pi^s(p_t)$ and thus we get and update it by **\pcol@getcurrpinfo** and **\pcol@defcurrpage**, because the spanning text immediately follows a synchronization point in p_t . Then we let **\box255** have the pre-spanning-text stuff followed by the spanning text being the original contents of **\box255**, which may be shifted left by $W_T - w_c =$ **\textwidth** - **\columnwidth** by the macro **\pcol@shiftspanning** if columnswapping is in effect so that its left edge is aligned to that of the leftmost column, i.e., of the text area.

¹⁴³Not \pcol@makecol because the depth capping of \@outputbox is done by \pcol@opcol when it saves the box into $\kappa_c(\beta^b)$.

 $^{^{144}}$ That is, the author gives higher priority to the perfect alignment of the items following a synchronization point.

¹⁴⁵This save/restore cannot be done by a grouping because \@makecol builds \@outputbox by local assignments. ¹⁴⁶Since we have a synchronization point before a spanning text always, pre-spanning-text stuff or its sole contents \vbox has a vertical skip at its tail to make the its depth 0 as discussed in §11.7.

¹⁴⁷We cannot do \setbox\@cclv\vbox{\unvbox\@cclv} because it erases the effect of pre-break skip following some visible material.

The third addition is for page-wise footnotes. If they are presented in \footins, we shrink \@colht by its height plus depth by \pcol@shrinkcolbyfn and put the stretch and shrink factor of \skip\footins at the bottom of \box255 by \pcol@unvbox@cclv to remove footnotes from the column-page but keeping the stretch/shrink contribution to the page breaking by their existence. Then we save \footins into a new \insert to be referred to as \pcol@currfoot¹⁴⁸ by \pcol@savefootins if $p = p_t$ so that it is saved in $\pi^f(p)$ by \pcol@startpage afterward, or simply discard the contents of \footins otherwise because $\pi^f(p)$ has already been fixed. Note that these saving/discarding make \footins void and thus \@makecol will not put footnotes.

On the other hand, if footnote typesetting is column-wise, \footins is kept unchanged so that its contents will be put by \@makecol if it has something. As for \pcol@currfoot, it should have its default value \voidb@x = \bot assigned to it beforehand, so that, if $p = p_t$, \pcol@startpage will make $\pi^f(p) = \bot$ unless page-wise footnotes are given in \footins.

```
155 \def\pcol@makecol{\let\pcol@textbottom\@textbottom
     \ifdim\pcol@textfloatsep=\maxdimen\else
156
       \def\@textbottom{\vskip\z@\@plus.0001fil\@minus.0001fil}\fi
157
158
     \ifpcol@sptext \ifnum\pcol@currcol=\z@
       \pcol@getcurrpinfo\@tempcnta\@tempdima\@tempskipa
159
       \setbox\@tempboxa\vbox{\unvcopy\@cclv}%
160
       \@tempdimb\ht\@tempboxa \advance\@tempdimb\dp\@tempboxa
161
162
       \ifdim\@tempdimb>\z@
163
         \@tempdimb\ht\@cclv \advance\@tempdimb\dp\@cclv
         \dimen@\ht\pcol@prespan \pcol@addflhd\@toplist\pcol@textfloatsep
164
         \@cons\pcol@sptextlist{{\number\dimen@}{\number\@tempdimb}}%
165
       \fi
166
       \pcol@defcurrpage{\number\@tempcnta}\pcol@spanning\pcol@footins
167
                         {\pcol@sptextlist}{\pcol@mparbottom}%
168
       \setbox\@cclv\vbox{\unvbox\pcol@prespan \pcol@shiftspanning\@cclv
169
                           \unvbox\@cclv}%
170
     \fi\fi
171
172
     \def\pcol@currfoot{\voidb@x}%
     \ifpcol@scfnote \ifvoid\footins\else
173
       \pcol@shrinkcolbyfn\@colht\footins\relax
174
       \setbox\@cclv\vbox{\pcol@unvbox@cclv\footins}%
175
176
       \ifnum\pcol@page=\pcol@toppage
177
         \pcol@Log\pcol@makecol{save}\footins
178
         \pcol@Fb
         \pcol@savefootins\pcol@currfoot
179
         \pcol@Fe{makecol(pagefn)}%
180
181
       \else
         \pcol@Log\pcol@makecol{discard}\footins
182
183
         \setbox\@tempboxa\box\footins
       \fi
184
     \fi\fi
185
     \pcol@Logstart\pcol@makecol
186
     \ifvoid\footins\else \pcol@Log\@makecol{put}\footins \fi
187
     \@makecol
188
     \pcol@Logend\pcol@makecol
189
     \let\@textbottom\pcol@textbottom}
190
```

¹⁴⁸Not in \pcol@footins because it is destroyed in \pcol@startpage just before saving operation into $\pi^f(p)$.

also used in **\pcol@makenormalcol** explicitly. The customization is twofold for both of top and bottom floats.

For the top floats, we invoke the original $\Cflt if \kappa_c(\xi) = \infty$ to mean the column-page to be shipped out does not have synchronization points, or otherwise our own \collcflt which we will discuss shortly. Prior to the invocation of \Ccflt , in addition, we let $\maxdepth = \Classical Cflt$ so that the macro refers to the value used throughout a paracol environment instead of that modified by \Claddtobot possibly affect the work in \Ccflt by the following sequence.

 $\label{eq:condition} $$ \colorseparate{condition} $$ \colorseparate{cond$

For the bottom floats, we invoke the original (@cflb always but, if the column-page has synchronization points, we insert vertical skips of <math>s = 0 pt plus 0.0001 fil minus 0.0001 fil and -s before and after the invocation respectively. Since $(@textbottom is let have the skip of s by <math>\col@makecol for a column-page having synchronization points and is inserted below bottom floats by <math>\col@makecol^{149}$, the effect of (@textbottom is canceled by the skip of <math>-s but looks moved above bottom floats. Therefore, if the natural height of the column-page is smaller than $\col lnt$, bottom floats are flushed to the page bottom as if column-page itself is flushed by \newpage etc. On the other hand, if the natural height is larger, more importantly, all shrinks below the last synchronization point is canceled by the infinite shrink in s above the bottom float but we should have sufficient space for shrinks there thanks to \textfloatsep to avoid the interference between the bottom text and bottom floats.

In addition, if $\ifpcol@lastpage = true$ to mean the column-page is in the last page, we insert \textfloatsep in $\@lostputbox below the bottom floats so that they are well separated from post-environment stuff. The switch is also$ *true* $in the invocation from <math>\pcol@makenormalcol$ for pre-environment stuff, so that the bottom floats in it are well separated from the top of multi-column stuff in the starting page.

On the other hand, the original \@combinefloats saved in \pcol@combinefloats by \pcol@zparacol is used in \pcol@output to restore the original when it finds \output request sneaking.

```
191 \def\pcol@combinefloats{%
192
     \global\maxdepth\@maxdepth
193
     \ifx\@toplist\@empty\else
194
       \ifdim\pcol@textfloatsep=\maxdimen \@cflt \else \pcol@cflt \fi
195
     \fi
196
     \ifx\@botlist\@empty\else
       \ifdim\pcol@textfloatsep=\maxdimen \@cflb
197
198
       \else
199
          \setbox\@outputbox\vbox{\unvbox\@outputbox
200
           \vskip\z@\@plus.0001fil\@minus.0001fil}%
201
         \@cflb
         \setbox\@outputbox\vbox{\unvbox\@outputbox
202
203
            \vskip\z@\@plus-.0001fil\@minus-.0001fil}%
204
       \fi
205
       \ifpcol@lastpage
206
         \setbox\@outputbox\vbox{\box\@outputbox \vskip\textfloatsep}%
207
       \fi
208
     \fi}
```

 $^{^{149}\}mathrm{The}$ insertion point is common to $\mathrm{IAT}_{E\!X}$ and $\mathrm{pIAT}_{E\!X}.$

\pcol@cflt The macro \pcol@cflt is invoked solely from \pcol@combinefloats if the column-page for which the macro combines the top floats has synchronization points. The macro has the same structure as LATEX's version \@cflt but has three modifications. The first one is that the floats are packed in a \vbox rather than listed in \@outputbox to nullify the stretch and shrink of \floatsep to keep the synchronization point from moving by them¹⁵⁰. The second is that we use \@maxdepth instead of \maxdepth to make it clear we always use the value common throughout a paracol environment. The third is that the \textfloatsep is replaced with \pcol@textfloatsep = $\kappa_c(\xi)$ (definitely finite) which can have a value different from \textfloatsep when the float space is enlarged for synchronization. If this enlargement is required, $\kappa_c(\xi)$ is biased by 10000 pt and thus is assuredly¹⁵¹ larger than 5000 pt. If so, the insertion of \topfigrule should be inhibited because it has already been inserted by \pcol@ synccolumn or there are no real floats but we only have the float for main vertical list prior to the synchronization point, or MVL-float in short.

```
209 \def\pcol@cflt{%
```

- 210 \let\@elt\@comflelt
- 211 \setbox\@tempboxa\vbox{}%
- 212 \@toplist
- 213 \setbox\@outputbox\vbox{%
- 214 \boxmaxdepth\@maxdepth
- 215 \box\@tempboxa
 216 \vskip-\floatsep
- 217 \ifdim\pcol@textfloatsep>5000\p@
- 218 \advance\pcol@textfloatsep-\@M\p@
- 219 \else
- 220 \topfigrule
- 221 \fi
- 222 \vskip\pcol@textfloatsep
- 223 \unvbox\@outputbox}%
- 224 \let\@elt\relax
- 225 \pcol@Fb
- 226 \xdef\@freelist{\@freelist\@toplist}%
- 227 \pcol@Fe{cflt}%
- 228 \global\let\@toplist\@empty}
- 229
- \pcol@opcol The macro \pcol@opcol is invoked from \pcol@output for the ordinary completed columnpage built by \pcol@makecol, or from the loop creating float columns in \pcol@output or \pcol@freshpage. At first it saves the column-page of column c in \@outputbox, which \pcol@makecol or \@tryfcolumn just has built for an ordinary or float column respectively, in an \insert acquired from \@freelist by \@next, and then adds it to the tail of $S_c = \pcol@shipped c$ by \@cons. In this saving operation, we add the sequence of uncoloring \specials at the bottom to clear color stack by \pcol@clearcst@unvbox giving it \@outputbox to be \unvboxed and possibly coloring \specials for the column-page's color context saved in Γ_s at the top, so that the succeeding column-page in printing order starts with its own color context. For this addition, furthermore, we let \boxmaxdepth = \@maxdepth to keep the depth capping made in the box builder from nullified¹⁵².

Then if c = 0, we fix the page number of the page p having the column-page and let $\pi^p(q)$ have page(p) + (q-p) usually but possibly page(p) + 2(q-p) with non-paired parallel-paging, for

 $^{^{150}\}mathrm{Maybe}$ unnecessary because of <code>\@textbottom</code> inserted by <code>\pcol@makecol</code> but ...

¹⁵¹Though not definitely in theoretical sense.

 $^{^{152}}Or$ to apply the capping dropped from pLATEX's <code>\@makecol</code>, or to do nothing for the box made by <code>\@tryfcolumn</code> and thus being 0 deep.

all $q \in [p+1, p_t]$ by \pcol@setpageno. After that, we invoke \pcol@nextpage to let p = p' for the next column-page of c, where p' = p+1 usually but can be p+k+1 if we have consecutive k float pages from p+1.

Next, we check if the oldest page p_b is made ready to be shipped out by the participation of the completed column-page by \pcol@checkshipped. If so, we invoke \pcol@outputcolumns giving argument 0 to ship out p_b and its successor float pages.

Finally we set up the next page p by $\col@startpage$ if $p > p_t$ meaning it is new one, or by $\col@getcurrpage$ otherwise, and reinitialize parameters for floats by $\col@floatplacement$ before returning to the invoker.

```
230 \def\pcol@opcol{%
                      \pcol@Fb
                 231
                       \@next\@currbox\@freelist{\global\setbox\@currbox\vbox to\@colht{%
                 232
                           \boxmaxdepth\@maxdepth
                 233
                           \pcol@clearcst@unvbox\@outputbox}}\pcol@ovf
                 234
                 235
                       \pcol@Fe{opcol}%
                       \expandafter\@cons\csname pcol@shipped\number\pcol@currcol\endcsname\@currbox
                 236
                       \ifnum\pcol@currcol=\z@ \pcol@setpageno \fi
                 237
                       \pcol@nextpage
                 238
                       \pcol@checkshipped
                 239
                       \if@tempswa \pcol@outputcolumns\z@ \fi
                 240
                       \ifnum\pcol@page>\pcol@toppage \pcol@startpage
                 241
                                                       \pcol@getcurrpage
                 242
                      \else
                      \fi
                 243
                 244
                      \pcol@floatplacement}
                 245
\pcol@setpageno The macro \pcol@setpageno is invoked from \pcol@opcol when it processes the column-page
```

\pcol@setpageno I he macro \pcol@setpageno is invoked from \pcol@opcol when it processes the column-page \pcol@setpnoelt of the first column c = 0 to fix the page number $page(p) \leftarrow page = \c@page of the page <math>p = \pcol@page$ having the column-page. It is also invoked from \pcol@output@switch when it leaves from the first column to reflect a jump of page made in the column building. In both cases, the macro lets $\pi^p(q)$ have page'(q) = page(p) + (q - p), except for the case of non-paired

parallel-paging in which page'(q) = page(p) + 2(q-p) instead, for all $q \in [p, p_t]$. Since we possibly have to update $\pi(q)$ such that $q \ge p$, at first we temporarily let $\Pi^+ =$

246 \def\pcol@setpageno{\begingroup

```
247 \@tempcnta\pcol@page \advance\@tempcnta-\pcol@basepage
```

```
248 \let\@elt\relax \edef\reserved@a{\pcol@pages\pcol@currpage}%
```

- 249 \global\let\pcol@pages\@empty \global\let\pcol@currpage\@empty
- 250 \let\@elt\pcol@setpnoelt \reserved@a
- $251 \ \endgroup\}$

```
252 \def\pcol@setpnoelt#1#2#3#4#5{%
```

```
253 {\let\@elt\relax \xdef\pcol@pages{\pcol@pages\pcol@currpage}}%
```

254 \ifnum\@tempcnta>\z@ \gdef\pcol@currpage{\@elt{#1}#2#3{#4}{#5}}%

```
255 \else \pcol@defcurrpage{\number\c@page}{#2}{#3}{#4}{#5}%
```

```
256 \advance\c@page\@ne
```

```
257 \ifpcol@paired\else \advance\c@page\@ne \fi
```

258 \fi

259 \advance\@tempcnta\m@ne}

```
260 \def\pcol@defcurrpage#1#2#3#4#5{{%
261 \let\@elt\relax \xdef\pcol@currpage{\@elt{#1}#2#3{#4}{#5}}}
262
```

\pcol@nextpage The macro \pcol@nextpage is invoked solely in \pcol@opcol to let p be p + k + 1 where k is \pcol@nextpelt the number of float pages directly following p, i.e., $k = |\{q > p \mid p < \forall q' \le q : \pi(q')^h < 0\}|$. For this update, the macro scans $\pi(q) \in \Pi$ for all $q \in [p_b, p_t)$ applying \pcol@nextpelt to $\pi(q)$, to perform the following where p_0 is p before update and f = if@tempswa being true at initial, to let $p \leftarrow p + k$, and then increments p to have p + k + 1.

$$\langle p, f \rangle \leftarrow \begin{cases} \langle p, f \rangle & q \leq p_0 \\ \langle p+1, f \rangle & q > p_0 \land f \land \pi^i(q) \neq \bot \land \pi^h(q) < 0 \\ \langle p, false \rangle & \text{otherwise} \end{cases}$$

```
263 \def\pcol@nextpage{\begingroup
     \@tempcnta\pcol@page \advance\@tempcnta-\pcol@basepage
264
     \@tempswatrue
265
266
     \let\@elt\pcol@nextpelt \pcol@pages
267
     \global\advance\pcol@page\@ne
268
     \endgroup}
269 \def\pcol@nextpelt#1#2#3#4#5{%
     \ifnum\@tempcnta<\z@
270
271
       \ifvoid#2\@tempswafalse
272
       \else\ifdim\dimen#2<\z@
         \if@tempswa \global\advance\pcol@page\@ne \fi
273
274
       \else \@tempswafalse
       \fi\fi
275
276
     \fi
     \advance\@tempcnta\m@ne}
277
278
```

\pcol@checkshipped The macro \pcol@checkshipped is invoked solely in \pcol@opcol to let \if@tempswa be true iff $S_c = \pcol@shipped c \neq \emptyset$ for all $c \in [0, C)$ to mean the oldest page p_b is ready to be shipped out.

```
279 \def\pcol@checkshipped{\@tempswatrue
280 \@tempcnta\z@ \@whilenum\@tempcnta<\pcol@ncol\do{%
281 \expandafter\ifx\csname pcol@shipped\number\@tempcnta\endcsname\@empty
282 \@tempswafalse \fi
283 \advance\@tempcnta\@ne}}
284</pre>
```

\pcol@getcurrpinfo

```
\label{eq:compared} \begin{array}{ll} \texttt{\ compared} & \texttt{
```

for $p = \ pcol@page \in [p_b, p_t]$. To do that, the macro scans all $\pi(q) \in \Pi^+ = (\Pi, \pi(p_t))$ applying \pcol@getpelt to $\pi(q) = \{\pi^p(q)\}\langle \pi^i(q)\rangle \langle \pi^f(q)\rangle \{\pi^s(q)\}\{\pi^m(q)\}\$ to invoke

 $\texttt{Pcol@getpinfo}\{\pi^p(q)\}\langle \pi^i(q)\rangle \langle \pi^f(q)\rangle \{\pi^s(q)\}\{\pi^m(q)\}\langle pg\rangle \langle ch\rangle \langle ts\rangle$

with the following arguments for \global assignments, if q = p.

Then the macro \collegetpinfo do the obvious assignments to \collegetpinfo , \c

$$\langle \langle ch \rangle, \langle ts \rangle, \texttt{lifpcol@nospan} \rangle = \left\{ \begin{array}{ll} \langle \texttt{\textheight}, \quad \texttt{\basis} \texttt{cl@topskip}, \quad true \rangle & \pi^i(q) = \bot \\ \langle \pi^h(q), & \pi^t(q), & false \rangle & \pi^i(q) \neq \bot \end{array} \right.$$

The other macro $\collegetcurrpinfo\langle pg \rangle \langle ch \rangle \langle ts \rangle$ is invoked in \collemakecol , \collegetcurrpage , $\collegetcurrpinfo \langle pg \rangle \langle ch \rangle \langle ts \rangle$ is invoked in \collemakecol , \collegetcurrpage , \collegetcurrpage , $\collegetcurrpinfo \langle pg \rangle \langle ch \rangle \langle ts \rangle$ is invoked in \collemakecol , \collegetcurrpage , $\collegetcurrpinfo \rangle$, $\collegetcurrpinfo \rangle$, but it is not for $\pi(p)$ but for $\pi(p_t) = \collecurrpage$. The macro $\collegetcurrpinfo \rangle$ has a direct invoker $\collegetcurrpinfo \rangle$ outputelt.

```
285 \def\pcol@getcurrpage{\begingroup
     \@tempcnta\pcol@page \advance\@tempcnta-\pcol@basepage
286
287
     \let\@elt\pcol@getpelt \pcol@pages\pcol@currpage
288
     \endgroup}
289 \def\pcol@getpelt#1#2#3#4#5{%
290
     \ifnum\@tempcnta=\z@
       \pcol@getpinfo{#1}#2#3{#4}{#5}%
291
                      {\global\c@page}{\global\@colht}{\global\topskip}%
292
     \fi
293
     \advance\@tempcnta\m@ne}
294
295 \def\pcol@getpinfo#1#2#3#4#5#6#7#8{\pcol@nospantrue
     \gdef\pcol@spanning{#2}\gdef\pcol@footins{#3}\gdef\pcol@sptextlist{#4}%
296
     \gdef\pcol@mparbottom{#5}%
297
     #6#1\relax
298
     \ifvoid#2\relax #7\textheight #8\pcol@topskip
299
     \else #7\dimen#2\relax #8\skip#2\relax \pcol@nospanfalse
300
301
     \fi}
302 \def\pcol@getcurrpinfo{%
     \edef\reserved@a{\expandafter\@cdr\pcol@currpage\@nil}%
303
     \expandafter\pcol@getpinfo\reserved@a}
304
305
```

\pcol@floatplacement The macro \pcol@floatplacement is invoked from \pcol@opcol, \pcol@output@start, \pcol@flushcolumn, \pcol@freshpage and \pcol@output@end to reinitialize the parameters of column-wise float placement at the beginning of a column-page or that of post-environment stuff. The macro lets \@textfloatsheight be 0 and then invokes \@floatplacement, as \@opcol does its tail¹⁵³. In addition, the macro lets \pcol@textfloatsep be \maxdimen to mean the new column-page does not have synchronization point at initial.

```
306 \def\pcol@floatplacement{%
307 \global\@textfloatsheight\z@ \global\pcol@textfloatsep\maxdimen
308 \@floatplacement}
309
```

¹⁵³But \mathbb{O} are because it is meaningless now.

7 Starting New Page

First, we let $\col@firstprevdepth = \relax$ to mean we have (had) left from the starting page so that $\col@output@end$ will be informed of that. Next we let $p_t = p$ and then, if invoked from $\col@output@end$ will be informed of that. Next we let $p_t = p$ and then, if invoked from $\col@output@end$ will be informed of that. Next we let $p_t = p$ and then, if invoked from $\col@output@end$ will be informed of that. Next we let $p_t = p$ and then, if invoked from $\col@output@end$ will be informed of that. Next we let $p_t = p$ and then, if invoked from $\col@output@end$ will be informed of that. Next we let $p_t = p$ and then, if invoked from $\col@output@end$ will be informed of that. Next we let $\col@currfoot$ into which $\col@makecol saved page-wise footnotes if any. Next we lets <math>\col@page = page(p-1) + 1$ unless non-paired parallel-paging is in effect or in other words if $\ifpcol@paired = true$, or $\col@page = page(p-1) + 2$ otherwise, by \stepcounter . Then we let $\colnt = \textheight$ as the base value without spanning stuff, and $\topskip = \col@ctopskip$ because the new page is the second or succeeding one built in paracol environment.

310 %% Starting New Page

311 312 \def\pcol@startpage{% \global\let\pcol@firstprevdepth\relax 313 \global\pcol@toppage\pcol@page 314\ifx\pcol@currpage\@empty\else 315 \pcol@getcurrpinfo{\global\c@page}\@tempdima\@tempskipa 316 317\@cons\pcol@pages 318 {{\number\c@page}\pcol@spanning\pcol@currfoot 319 {\pcol@sptextlist}{\pcol@mparbottom}}% \stepcounter{page}\ifpcol@paired\else \stepcounter{page}\fi 320 \fi 321 \global\@colht\textheight 322

323 \global\topskip\pcol@topskip

 $\pi^p(p_t) = \texttt{COpage} \quad \pi^b(p_t) = \texttt{COutputbox} \quad \pi^h(p_t) = -\texttt{Maxdimen} \quad \pi^t(p_t) = \texttt{PcolOtopskip} \\ \pi^f(p_t) = \bot \quad \pi^s(p_t) = \emptyset \quad \pi^m(p_t) = \emptyset$

We also increment p and p_t , and also \c@page by one or two according to \ifpcol@paired by \stepcounter, to let them have the values for the page following the float pages.

- \@dblfloatplacement \let\f@depth\z@ 324 325\@tryfcolumn\@dbldeferlist \@whilesw\if@fcolmade\fi{% 326 327 \pcol@Fb 328 \@next\@currbox\@freelist{% 329 \global\setbox\@currbox\box\@outputbox}\pcol@ovf 330 \pcol@Fe{startpage(fcol)}% 331 \global\dimen\@currbox-\maxdimen
- 332 \global\skip\@currbox\pcol@topskip

- 333 \@cons\pcol@pages{{\number\c@page}\@currbox\voidb@x{}{}%
- 334 \stepcounter{page}\ifpcol@paired\else \stepcounter{page}\fi
- 335 \global\advance\pcol@page\@ne \global\pcol@toppage\pcol@page
- 336 \@tryfcolumn\@dbldeferlist}%

Next, we copy **\@dbldeferlist** containing page-wise floats which could not be included in float pages to **\reserved@b**, clear the list, and then scan the copied list by applying **\@sdblcolelt** to each list element to invoke **\@addtodblcol** for adding the element to **\@dbltoplist** or keeping it in **\@dbldeferlist** or **\@deferlist** depending on LATEX's version, as LATEX's **\@startdblcolumn** does. In addition, as discussed in item-(3) of §1.8, we also clear **\@deferlist** after saving it in **\reserved@c** prior to the scan, and then after the scan we concatenate **\@dbldeferlist** and **\@deferlist** to let the former have the result and restore **\@deferlist** from **\reserved@c**.

Then If this scan results in empty \@dbltoplist to mean the new page does not have any spanning stuff, we invoke \pcol@defcurrpage with $\pi^i(p_t) = \pi^f(p_t) = \bot$ and $\pi^s(p_t) = \pi^m(p_t) = \emptyset$ so that $\pi(p_t)$ represents a page perfectly empty.

337 \begingroup

338 \let\reserved@b\@dbldeferlist \let\reserved@c\@deferlist

- 339 \global\let\@dbldeferlist\@empty \global\let\@deferlist\@empty
- 340 \let\@elt\@sdblcolelt
- 341 \reserved@b
- 342 \let\@elt\relax \xdef\@dbldeferlist{\@dbldeferlist}%
- 343 \global\let\@deferlist\reserved@c
- 344 \endgroup
- 345 \ifx\@dbltoplist\@empty
- 346 \pcol@defcurrpage{\number\c@page}\voidb@x\voidb@x{}{}%

Otherwise, i.e., \@dbltoplist is not empty, we scan all elements in it by letting \@elt = \@comdblflelt to have all page-wise floats in \@tempboxa. Then, after returning all elements to \@freelist, we acquire an \insert from \@freelist to be $\pi^i(p_t)$ by \@next and store the contents of \@tempboxa in $\pi^b(p_t)$ after removing the last vertical skip \dblfloatsep and then adding \dblfigrule and the vertical skip \dbltextfloatsep. The other elements of $\pi(p_t)$ are set as follows to represent the page with spanning stuff which makes the height of each column \@colht shrunk from its initial value \textheight by the series of \@addtodblcol.

$$\begin{split} \pi^p(p_t) &= \texttt{\colpage} = page(p_t) \quad \pi^h(p_t) = \texttt{\colpace} \\ \pi^s(p_t) &= \emptyset \quad \pi^m(p_t) = \emptyset \end{split}$$

Finally, regardless of the existence of the page-wise floats, we let $\collection = \bot$ to mean the top page does not have any page-wise footnotes, so far if footnote typesetting is page-wise, or never otherwise.

347	\else
348	\setbox\@tempboxa%
349	\begingroup
350	\let\@elt\@comdblflelt
351	\@dbltoplist
352	\let\@elt\relax
353	\pcol@Fb
354	\xdef\@freelist{\@freelist\@dbltoplist}%
355	\pcol@Fe{startpage(dbltop)}%
356	\global\let\@dbltoplist\@empty
357	\pcol@Fb
358	\@next\@currbox\@freelist{\global\setbox\@currbox%

```
\unvbox\@tempboxa \vskip-\dblfloatsep \dblfigrule
359
           \vskip\dbltextfloatsep}}\pcol@ovf
360
         \pcol@Fe{startpage(spanning)}%
361
         \global\dimen\@currbox\@colht
362
363
         \global\skip\@currbox\pcol@topskip
         \pcol@defcurrpage{\number\c@page}\@currbox\voidb@x{}{}%
364
365
       \endgroup
     \fi
366
     \gdef\pcol@footins{\voidb@x}}
367
368
```

8 Shipping Page Out

\pcol@outputcolumns The macro \pcol@outputcolumns⟨*all*⟩ is invoked from \pcol@opcol with ⟨*all*⟩ = 0 to ship out the page p_b and float pages following it if any, or \pcol@sync with ⟨*all*⟩ = 1 to ship out all pages in Π . It copies Π = \pcol@pages into Π' = \reserved@b and clear Π once to remove pages shipped out from it. Then, after initializing f_o = \if@tempswa = true to ship out (the first) ordinary page and f_f = \ifpcol@outputflt = true to ship out float pages (following the first page), it scans all $\pi(q) \in \Pi'$ applying \pcol@outputelt⟨*all*⟩ to $\pi(q)$ to ship it out or keep it in Π .

369 %% Shipping Page Out

370

 $371 \def\pcol@outputcolumns#1{\begingroup}$

- $\label{lempswatrue \pcol@outputflttrue} 372 $$ \def\equal time \def\equal ti$
- 373 \let\reserved@b\pcol@pages \gdef\pcol@pages{}%
- $374 \ \ensuremath{\texttt{veserved@b}}$
- $375 \setminus endgroup$

```
376 \def\pcol@outputelt#1#2#3#4#5#6{%
```

- 377 \setbox\@outputbox\box\voidb@x
- $\label{eq:linear} 378 \ \label{eq:linear} 378 \ \label{eq:linear} \ \label{eq:linear} 378 \ \label{eq:linear} \ \label{eq:linear} 378 \ \label{eq:linear} \ \label{eq:linear} \ \label{eq:linear} \ \label{eq:linear} 378 \ \label{eq:linear} \ \lab$

Then, we do one of the followings according to h and f_o .

• *h* < 0

It means q is a float page. If $f_f = true$, we let \@outputbox have $\pi^b(q)$ to be shipped out, paint its background with $B_{\{F,f\}}$ by \pcol@bg@paintbox letting the basic height \pcol@bg@floatheight of the paining region $R_{\{F,f\}}$ be $H_T = \text{pcol@bg@textheight} =$ \textheight+\maxdepth, and return \insert $\cdot \pi^i(q)$ to \@freelist by \@cons because it is no longer necessary. Then if $C_L < C$ to mean parallel-paging is in effect, we let \pcol@ rightpage be an empty box but paint its background too, because the right counterpart of left parallel float page should be always blank. Note that we temporarily increment page(q) by one for non-paired right parallel-pages so that the painting macro performs page-parity dependent operations correctly.

On the other hand if $f_f = false$, we simply return $\pi(q)$ back to Π .

379	\ifdim\@tempdima<\z@
380	\ifpcol@outputflt
381	\def\pcol@bg@floatheight{\pcol@bg@textheight}%
382	\setbox\@outputbox\vbox to%
383	\pcol@bg@paintbox{Ff}\unvbox\pcol@spanning}%
384	\pcol@Fb
385	\@cons\@freelist\pcol@spanning
386	\pcol@Fe{outputelt(spanning)}%
387	\ifnum\pcol@ncolleft<\pcol@ncol
388	<pre>\setbox\pcol@rightpage\vbox to%</pre>
389	\ifpcol@paired\else \advance\c@page\@ne \fi
390	\pcol@bg@paintbox{Ff}\vfil}%
391	\fi
392	\else
393	$\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ $
394	\fi

• $h \ge 0 \land f_o = true$

It means q is a non-float page to be shipped out. If $\langle all \rangle = 0$, we let $f_o = false$ to keep succeeding non-float pages from being shipped out. Then we build the ship-out image of the right parallel-page q in \pcol@rightpage by \pcol@ioutputelt giving it the box and the column range $[C_L, C)$ if $C_L < C$ to mean parallel-paging, and then that of the left parallel-page in \@outputbox by \pcol@ioutputelt again but giving it $[0, C_L)$ and \@outputbox. Note that the right-first left-second order is essential, because in the process to build right parallel-page we have to examine the existence of $\pi^i(q)$ and $\pi^f(q)$ and then refer to their height and depth to make the region corresponding to them blank, while the boxes of these \inserts are made void in the building process of the left parallel-page obviously.

Then after the ship-out image building, we \globally let $\flotstpage = false$ to tell $\clothetallocal_prollocal$

```
395
     \else\if@tempswa
       \ifnum#1=\z0 \@tempswafalse \fi
396
       \ifnum\pcol@ncolleft<\pcol@ncol
397
         \pcol@Logstart{\pcol@outputelt{right}}%
398
         \pcol@ioutputelt\pcol@ncolleft\pcol@ncol\pcol@rightpage
399
         \pcol@Logend{\pcol@outputelt{right}}%
400
401
       \fi
       \pcol@Logstart{\pcol@outputelt{left}}%
402
       \pcol@ioutputelt\z@\pcol@ncolleft\@outputbox
403
       \pcol@Logend{\pcol@outputelt{left}}%
404
405
       \global\pcol@firstpagefalse
```

• $h \ge 0 \land f_o = false$

It means q is a non-float page to be kept. Therefore, we let $f_f = false$ to keep float pages following it from being shipped out. Then we return $\pi(q)$ to Π by \@cons.

406 $\ensuremath{\mathsf{lse}}$

```
407 \pcol@outputfltfalse
```

```
408 \@cons\pcol@pages{{#2}#3#4{#5}{#6}}%
```

```
409 \fi\fi
```

Finally, if $\langle 0 \text{outputbox} \neq \bot$ to mean $\pi(q)$ is to be shipped out, we invoke $\langle 0 \text{outputpage}$ to do it and increment p_b to let it has q + 1. Note that since we have let $\langle c0page = page(q)$, the direct and indirect references to it in $\langle 0 \text{outputpage}$ are correctly done. Also note that the $\langle \text{global}$ increment of it by $\langle \text{stepcounter}$ in $\langle 0 \text{outputpage}$ will be overridden by the $\langle \text{global}$ assignment to it done by $\langle \text{pcol}0 \text{startpage}$ or $\langle \text{pcol}0 \text{getcurrpage}$ invoked from $\langle \text{pcol}0 \text{col}0 \text{co$

- 410 \ifvoid\Coutputbox\else
- 411 \global\advance\pcol@basepage\@ne \@outputpage
- 412 \fi}
- 413

\pcol@ioutputelt The macro \pcol@ioutputelt $\langle C^0 \rangle \langle C^1 \rangle \langle b \rangle$ is invoked solely in \pcol@outputelt but can be done twice with $(C^0, C^1, b) = (C_L, C, \pcol@rightpage)$ if parallel-paging is in effect and with $(C^0, C^1, b) = (0, C_L, \@outputbox)$ always, to build the ship-out image of the right or left parallel-page q in the box b respectively.

After opening a $\forall box$ of $\forall textheight$ tall for b, at first we increment page(q) by one for right parallel-page if it is non-paired, so that painting macros perform page-parity dependent operations correctly.

Next, we put materials to be shipped out in the box b as follows. First, if $\pi^f(q) \neq \bot$ to mean the page q has page-wise footnote, we paint their background with $B_{\{N,n\}}$ by \pcol@bg@ paintbox letting the basic height \pcol@bg@footnoteheight of the paining region $R_{\{N,n\}}$ be the height-plus-depth of $\pi^f(q)$. We do the painting at this earliest stage of the image building in order to use the left-top corner of the text area where we are now at as the origin for painting, and to let the region may be overlaid by those of columns and column-separating gaps. We also let $h = \pi^h(q) = \$

```
414 \def\pcol@ioutputelt#1#2#3{\setbox#3\vbox to\textheight{%
```

- 415 \ifpcol@paired\else\ifnum#1=\z@\else \advance\c@page\@ne \fi\fi
- 416 \ifvoid\pcol@footins\else
- 417 \def\pcol@bg@footnoteheight{\@elt{\ht\pcol@footins}\@elt{\dp\pcol@footins}}%
- 418 \pcol@bg@paintbox{Nn}%
- 419 \pcol@shrinkcolbyfn\@tempdima\pcol@footins\relax
- 420 \fi

Second, if $f_{ns} = false$ to mean $\pi(q)$ has spanning stuff in $\pi^b(q)$, we do one of the followings.

- If $C^0 = 0$ to mean the target is the left parallel-page, $\pi^b(q)$ is put by \unvbox, painting its background with $B_{\{F,f\}}$ by \pcol@bg@paintbox letting the basic height \pcol@bg@ floatheight of the paining region $R_{\{F,f\}}$ be the height-plus-depth of $\pi^b(q)$ if q is not the first page and thus $\pi^b(q)$ has page-wise floats. We also return the \insert $\pi^i(q)$ to \@freelist by \@cons.
- If $C^0 \neq 0$ to mean right parallel-page and q is the first page, \pcol@rightpage has pre-environment stuff in the right parallel-page. Therefore, we simply put the box but making its height and depth equal to those of $\pi^b(q)$, without painting because the box has already been painted, and with \nointerlineskip to prevent baseline-skip insertion below the box.
- Otherwise, i.e., $C^0 \neq 0$ and q is not the first page, we put an empty box whose height and depth equal to those of $\pi^b(q)$ by \pcol@phantom, with painting as done for floats in the left parallel-page and with \nointerlineskip.

Note that after putting spanning stuff and/or painting the background, we temporarily increment \topmargin by the height-plus-depth of $\pi^b(q)$, so that painting macros for columns, column-separating gaps and spanning texts assume the top edge of column area as that of text area when they extend the top edges of their regions upward to the page top.

```
\ifpcol@nospan\else
421
       \def\pcol@bg@floatheight{%
422
         \@elt{\ht\pcol@spanning}\@elt{\dp\pcol@spanning}}%
423
       \@tempdimb\ht\pcol@spanning \advance\@tempdimb\dp\pcol@spanning
424
       ifnum#1=\z@
425
         \ifpcol@firstpage\else \pcol@bg@paintbox{Ff}\fi
426
427
         \pcol@Fb
428
         \@cons\@freelist\pcol@spanning \unvbox\pcol@spanning
429
         \pcol@Fe{ioutputelt(spanning)}%
430
       \else\ifpcol@firstpage
431
         \ht\pcol@rightpage\ht\pcol@spanning
432
         \dp\pcol@rightpage\dp\pcol@spanning
         \box\pcol@rightpage \nointerlineskip
433
       \else
434
         \pcol@bg@paintbox{Ff}\pcol@phantom\pcol@spanning \nointerlineskip
435
436
       \fi\fi
437
       \advance\topmargin\@tempdimb
438
     \fi
```

Third, we invoke $\col@buildcolseprule</code> giving it h being <math>\pi^h(q)$ but possibly shrunk by page-wise footnotes, the column range $[C^0, C^1)$, and $\mbox{maxdepth}$ to mean q is non-last page, to draw a column-separating rule possibly broken by the spaces for spanning texts in the box $\col@tempboxa$ and to paint the backgrounds of columns, column-separating gaps and spanning text in the box $\top boxa$ which we put into b immediately.

Fourth, we put a hbox of htextwidth wide having hboxes of $w_c = \text{pcol@columnwidth} c$ wide containing σ_c followed by hss for all $c \in [C^0, C^1)$, where $\sigma_c = \text{box} \cdot s_c(q)$ being the first element removed from S_c by \@next and then returned to \@freelist by \@cons if it is not \bot , or \voidb@x otherwise. We separate hboxes of σ_c by making each hbox preceded by \pcol@@hfil being \relax for the first one and the macro \pcol@hfil for others giving it an argument $c^g = \text{pcol@colsepid} \in \{c, c-1\}$ which we discuss shortly to put a gap of $g_{c^g} = \text{pcol@columnsep} \cdot c^g$ wide optionally having a column-separating rule and being painted.

Note that the scanning order of $c \in [C^0, C^1)$ is usually ascending of course, but is descending if column-swapping is specified and $page(q) \mod 2 = 0$. For this ordering, we invoke $\col@swapcolumn(c')(c)(C^0)(C^1)$ to have c for the $(c'-C^0)$ -th iteration of the scanning where $c' = \col@tempcnta$ and $c = \col@tempcntb$. Another operation done by the macro is to let $c^g = c-1$ if swapped or $c^g = c$ otherwise, because if swapped the column-c is followed by the gap which follows c-1 if not swapped.

```
439
     \pcol@buildcolseprule\@tempdima#1#2\@maxdepth \unvbox\@tempboxa
     \hb@xt@\textwidth{%
440
       \let\pcol@@hfil\relax
441
       \@tempcnta#1\relax \@whilenum\@tempcnta<#2\do{%
442
443
          \pcol@swapcolumn\@tempcnta\@tempcntb#1#2\relax
444
          \expandafter\@next\expandafter\@currbox
           \csname pcol@shipped\number\@tempcntb\endcsname
445
           \relax{\let\@currbox\voidb@x}%
446
         \ifvoid\@currbox\else
447
448
           \pcol@Fb
           \@cons\@freelist\@currbox
449
           \pcol@Fe{ioutputelt(page)}%
450
         \fi
451
452
         \expandafter\@tempdima
```

- 453 \csname pcol@columnwidth\number\@tempcntb \endcsname
- 454 \pcol@Chfil \hb@xt@\@tempdima{\box\@currbox\hss}%
- $\label{lem:state} 455 \qquad \edshift{\col@colsepid}}\$

Fifth, if $\pi^f(q) \neq \bot$ to mean the page q has page-wise footnotes, we put them at the bottom of \Coutputbox by \pcolOputfootins, and return $\pi^f(q)$ to \Cfreelist, if $C^0 = 0$ meaning left parallel-page. Otherwise for the right parallel-page, we simply put an empty box whose height and depth equal to those of $\pi^f(q)$ by \pcolOphantom, preceded by a vertical skip of \skip $\cdot \pi^f(q)$ and then \nointerlineskip to inhibit baseline skip insertion above the box, and followed by null \vskip as done in \pcolOputfootins.

Sixth and finally¹⁵⁴, we let \boxmaxdepth = \@maxdepth to cap the depth of b which we are now closing, as done for each column-page and as expected to be applied to page-wise footnotes.

457	\ifvoid\pcol@footins\else
458	\ifnum#1=\z@
459	\pcol@Log\pcol@outputelt{output}\pcol@footins
460	\pcol@putfootins\pcol@footins
461	\pcol@Fb
462	\@cons\@freelist\pcol@footins
463	\pcol@Fe{ioutputelt(footins)}%
464	\else
465	\vskip\skip\pcol@footins \nointerlineskip
466	<pre>\pcol@phantom\pcol@footins \vskip\z@</pre>
467	\fi
468	\fi
469	\boxmaxdepth\@maxdepth}}

- $\colored phantom$ The macro $\colored phantom \langle b \rangle$ is used in $\colored putlet$, $\colored putlet putlet$ and $\colored putlet putlet point of the argument box b being a kind of page-wise stuff, into <math>\colored putlet page$ for the right parallel-page whose left counterpart has b in it. That is, the macro is used to make a region corresponding to b blank. To put the empty box, we locally let $\colored putlet parallet page is being a depth and depth and depth and depth to those of b and then put it.$
 - 470 \def\pcol@phantom#1{{%
 471 \setbox\@tempboxa\vbox{}\ht\@tempboxa\ht#1\dp\@tempboxa\dp#1\box\@tempboxa}}
 472

\pcol@buildcolseprule The macro \pcol@buildcolseprule $\langle H_{n+1}\rangle\langle C^0\rangle\langle C^1\rangle\langle d\rangle$ is used in \pcol@ioutputelt, \pcol@ \pcol@buildcselt@S imakeflushedpage and \pcol@iflushfloats to build a box containing column-separating \pcol@buildcselt rule possibly broken by spanning texts and to paint backgrounds of columns and columnseparating gaps for $c \in [C^0, C^1)$ and spanning texts in the last page (d = 0) or non-last page $(d = \mbox{Qmaxdepth}) p$ having column-pages of H_{n+1} tall where $n = |\pi^s(p)|$.

> For initializing the drawing and painting process, we let $\mathbb{Q}_{p} = H_0 + h_0 = 0$, $(\mathbb{Q}_{p} = \mathbb{Q}_{p} = \mathbb{Q}_{p} = (C_b^0, C_b^1) = (C^0, C^1)$, and make boxes $b_r = \mathbb{Q}_{p} = \mathbb$

 $^{^{154}}$ Not necessary to be finally, but we placed this assignment at the end of the box to make it clear the depth capping is only for the box.

 h_i if $H_i + h_i < H_{n+1}$ to mean the spanning text is non-last, or $(H_{n+1} - H_i) + d$ if last to fill the narrow strip of d = maxdepth tall below the text for non-last pages.

Then we scan $\pi^{s}(p)$ again but applying \pcol@buildcselt $\langle H_i \rangle \langle h_i \rangle$ to each element $span(H_i, h_i)$ to do the followings.

- 1. To b_r , add a vertical rule whose height is $H'_i = H_i (H_{i-1} + h_{i-1})$ and width is \columnseprule if $H'_i > 0$, and then a vertical skip of h_i , as the rule segment between (i-1)-th and *i*-th spanning texts. Note that H_i and h_i are represented in the form of integers and thus we need **sp** to use them as dimensions.
- 2. To b_b , add painted backgrounds for all columns $c \in [C^0, C^1)$ and column-separating gaps $c \in [C^0, C^{1}-1)$ by $\col@bg@paintcolumns$ defining their regions $R^c_{\{c,g\}}(i)$ by letting common top edge position $y_0 = \col@bg@columntop = H_{i-1} + h_{i-1}$ and common height $y_1 y_0 = \col@bg@columnheight = H'_i$, if $H'_i > 0$. Also add painted background for the *i*-th spanning text by $\col@bg@paintbox$ as we did for under-painting but this time the region is $R_s(i)$.
- 3. Let \Ctempdimb = $H_i + h_i$ for the next element $span(H_{i+1}, h_{i+1})$.

Then if $H'_{n+1} > 0$, we add the last rule segment of H'_{n+1} tall to b_r , and add painted backgrounds for columns and column-separating gaps as done in the step 2 above but letting $y_1 - y_0 =$ $H'_{n+1} + d$ to let the common bottom edge of the their regions reach the bottom of text area for non-last pages.

```
473 \def\pcol@buildcolseprule#1#2#3#4{%
474
     \Ctempdima#1\relax \dimenC#4\relax
     \let\pcol@bg@from#2\relax \let\pcol@bg@to#3\relax
475
     \setbox\pcol@tempboxa\vbox{}\setbox\@tempboxa\vbox{}%
476
     \let\@elt\pcol@buildcselt@S \pcol@sptextlist
477
478
     \@tempdimb\z@ \let\@elt\pcol@buildcselt \pcol@sptextlist
479
     \let\@elt\relax \advance\@tempdima-\@tempdimb
480
     \ifdim\@tempdima>\z@
481
       \setbox\pcol@tempboxa\vbox{\unvbox\pcol@tempboxa
         \hrule\@height\@tempdima\@width\columnseprule}%
482
       \setbox\@tempboxa\vbox{\unvbox\@tempboxa
483
         \let\@elt\relax
484
         \edef\pcol@bg@columntop{\number\@tempdimb sp}%
485
486
         \edef\pcol@bg@columnheight{%
487
           \@elt{\number\@tempdima sp}\@elt{\number\dimen@ sp}}%
488
         \pcol@bg@paintcolumns}%
489
     \fi}
   \def\pcol@buildcselt@S#1#2{%
490
491
     \setbox\@tempboxa\vbox{\unvbox\@tempboxa
492
       \let\@elt\relax
       \def\pcol@bg@spanningtop{\@elt{#1sp}}%
493
       \advance\@tempdima-#1sp\relax \advance\@tempdima-#2sp\relax
494
495
       \advance\dimen@\@tempdima
       \edef\pcol@bg@spanningheight{\@elt{#2sp}%
496
         \ifdim\@tempdima>\z@\else \@elt{\number\dimen@ sp}\fi}%
497
498
       \pcol@bg@paintbox{S}}}
499
   \def\pcol@buildcselt#1#2{%
500
     \@tempdimc#1sp \advance\@tempdimc-\@tempdimb
501
     \setbox\pcol@tempboxa\vbox{\unvbox\pcol@tempboxa
       \ifdim\@tempdimc>\z@ \hrule\@height\@tempdimc\@width\columnseprule \fi
502
```

```
503
       \vskip#2sp}%
     \setbox\@tempboxa\vbox{\unvbox\@tempboxa
504
       \let\@elt\relax
505
       \edef\pcol@bg@columntop{\number\@tempdimb sp}%
506
507
       \edef\pcol@bg@columnheight{\@elt{\number\@tempdimc sp}}%
       \ifdim\@tempdimc>\z@ \pcol@bg@paintcolumns \fi
508
       \def\pcol@bg@spanningtop{\@elt{#1sp}}%
509
       \advance\@tempdima-#1sp\relax \advance\@tempdima-#2sp\relax
510
       \advance\dimen@\@tempdima
511
       \edef\pcol@bg@spanningheight{\@elt{#2sp}%
512
         \ifdim\@tempdima>\z@\else \@elt{\number\dimen@ sp}\fi}%
513
       \pcol@bg@paintbox{s}}%
514
     \@tempdimb#1sp \advance\@tempdimb#2sp\relax}
515
516
```

\pcol@hfil The macro \pcol@hfil⟨c⟩ is used in \pcol@ioutputelt, \pcol@imakeflushedpage and \pcol@iflushfloats to separate column c+1 and c or c and c+1 according as the columns are swapped or not in the page the caller macros are building. If \columnseprule = r > 0, the macro puts the followings; a horizontal space of $g_c/2 = \text{pcol@columnsep} \cdot c/2$ followed by a skip -r/2 to nullify the width of the rule; the rule in \pcol@tempboxa which \pcol@ buildcolseprule built, with color \pcol@colseprulecolor $\cdot c$ or \pcol@colseprulecolor according as the former is defined or not, i.e., \colseprulecolor[mode]{color}[c] is declared or not; and $g_c/2$ again but preceded by -r/2. On the other hand if r = 0, we simply put a space of g_c . Note that the skips of $g_c/2$ and g_c are accompanied by 1 fil infinite stretch to avoid underfull when $\sum_{c=C^0}^{C^1-2} (w_c + g_c) + w_{C^1-1} < W_T$ where $(C^0, C^1) = \{(0, C_L), (C_L, C)\}$, due to arithmetic errors in calculations of w_c and g_c^{155} .

```
517 def pcol@hfil#1{{%}}
     \@tempdima\csname pcol@columnsep#1\endcsname\relax
518
519
     \ifdim\columnseprule>\z@
       \hskip.5\@tempdima\@plus1fil\relax
520
       \hskip-.5\columnseprule
521
       \@ifundefined{pcol@colseprulecolor#1}%
522
         {\pcol@colseprulecolor}{\@nameuse{pcol@colseprulecolor#1}}%
523
       \copy\pcol@tempboxa \hskip-.5\columnseprule
524
       \hskip.5\@tempdima\@plus1fil\relax
525
     \else \hskip\@tempdima\@plus1fil\relax
526
527
     fi}}
```

\pcol@outputpage The macro \@outputpage, being our own version of LATEX's one kept in \pcol@@outputpage, \@outputpage ships out a page p or parallel-page pair in p. The reason why we redefine this macro is that we need a few special operations for parallel-paging and background painting outside of paracol environments. Therefore, the macro is not only used in our own macros \pcol@outputelt, \pcol@output@start, \pcol@output@flush, \pcol@output@clear, \pcol@flushfloats and \pcol@output@end, but also in LATEX's \@opcol and \@doclearpage¹⁵⁶ invoked from our own or LATEX's \output routine.

528

First we calculate $H'_M = \text{topmargin} + \text{headheight} + \text{headsep}$ to place the origin of background painting at the top edge of text area in what IATEX assumes as a page, i.e., shifted 1 inch down from the real page. Then if \ifpcol@output = true to mean this macro is used

 $^{^{155}}$ It is assured the sum of w_c and g_c cannot exceed W_T even with arithmetic errors and thus overfull never occurs.

¹⁵⁶And possibly in \@outputdblcol if double-column typesetting is done outside paracol.

in a paracol environment, we build the painted backgrounds of left and right parallel-pages in \pcol@tempboxa = b_l and \@tempboxa = b_r by putting a vertical skip of H'_M , and invoking \pcol@bg@paintpage with the setting (\pcol@bg@from, \pcol@bg@to) = (C_b^0, C_b^1) be $(0, C_L)$ and (C_L, C) respectively. Note that \pcol@bg@paintpage paints backgrounds of regions $R_a^{[c]}$ for all $a \in \{T, B, L, R, C, S, t, b, l, r\}$ and $c \in [C_b^0, C_b^1)$, and for b_r we temporarily increment page(p) by one if non-paired parallel-paging is in effect.

Otherwise, i.e., if $\ifpcol@output = false$ indicating outside use, we build the painted backgrounds in b_l and b_r similarly but with the following differences; background painting is done if $\ifpcol@havelastpage = true$ to mean the page to be shipped has the last page of closed paracol as its part and $\set@color \neq \relax$ to mean some coloring package is loaded; page background painting is done by $\col@bg@@paintpage$ because $\col@bg@paintpage$ is not available outside paracol environments; the background of post-environment stuff is painted by $\col@bg@@paintbox$ for the region $R_{\{P,p\}} = [(0, W_T)(H_B, H_T)]$ where $H_B =$ $\col@bg@preposttop \in {\col@bg@preposttop@left, \col@bg@preposttop@right} hav$ $ing the bottom edge of the last paracol environment (having right parallel-page for <math>b_r$). In addition, we examine if $\col@rightpage \neq \perp$ to mean the right parallel-page was built by $\col@output@end$ when the last paracol environment was closed and, if so, make the box $\textheight tall adding \vfil to its bottom.$

Then regardless of ifpcol@output, we do the followings; let the height and depth of b_l and b_r be 0 because they cannot occupy any real spaces in the ship-out image; temporarily let ifpcol@swapcolumn = false if page(p) is odd, $C_L = C$ to mean parallel-paging is not in effect¹⁵⁷, parallel-paging is done in non-paired mode¹⁵⁸, or we are outside paracol environments and the page does not have anything produced in environments. That is, we let ifpcol@swapcolumn = true if the page has something produced by a paracol environment, column-swapping and parallel-paging are specified for the (last) environment¹⁵⁹, and the page number is even. Note that a page may have two or more (last pages of) paracol environments whose parallel-paging style can be inconsistent including the case some of them are not parallel-paged. If this inconsistency happens the page is shipped out following the style of the last environment. Also note that even if the last environment is not parallel-paged, the right parallel-page kept in pcol@rightpage is assuredly shipped out.

Then if column-swapping is in effect, we ship out the right parallel-page at first by $\col@outputpage@r and then the left one by <math>\col@outputpage@l to swap the left and right. Otherwise, the ship-out order is normal and thus the invocation order is <math>\col@outputpage@l to swap the left and right. Otherwise, the ship-out order is normal and thus the invocation order is <math>\col@outputpage@l to swap the left and right. Otherwise, the ship-out order is normal and thus the invocation order is <math>\col@outputpage@l to swap the left and right. Otherwise, the ship-out order is normal and thus the invocation order is <math>\col@outputpage@l to swap the left and right. Otherwise, the ship-out order is normal and thus the invocation order is <math>\col@outputpage@l to swap the left and \col@outputpage@r as its argument is <math>page(p) + 1$ if it is the second one, i.e., not swapped, while the argument in other cases and of $\col@outputpage@l are always page(p)$. Then finally, we $\globally let \ifpcol@havelastpage = false because so far the next page does not have paracol's last page especially when we are outside it, let <math>\col@bg@preposttop@right have 0$ because, if we are outside, the next pre-environment stuff should start from the top of a page, and let $\mathcal{M} = \col@mparbottom@out be \mathcal{M}_0 = \col@mparbottom@zero because so far we have no marginal notes given in paracol environments¹⁶⁰.$

529 \let\pcol@Coutputpage\Coutputpage

¹⁵⁷Since the assignments of C_L and C in \pcol@zparacol are \global and they are not modified anywhere else, examining their equality outside paracol environments is safe and meaningful.

 $^{^{158}}$ We need this examination because \ifpcol@swapcolumn = false for non-paired parallel-paging is made locally by \pcol@zparacol.

 $^{^{159}}$ Column-swapping may be enabled *after* the last **paracol** environment was closed but we consider the enabling is effective for the page having the environment.

 $^{^{160}}$ This assignment in a paracol environment is meaningless because \mathcal{M} is meaningless too, but not harmful.

```
530 \def\@outputpage{\begingroup
     \@tempdima\topmargin \advance\@tempdima\headheight \advance\@tempdima\headsep
531
     \ifpcol@output
532
       \setbox\pcol@tempboxa\vtop{\vskip\@tempdima \global\pcol@bg@paintedfalse
533
        \let\pcol@bg@from\z@ \let\pcol@bg@to\pcol@ncolleft
534
        \pcol@bg@paintpage}%
535
       \ifpcol@bg@painted \@tempswatrue \else \@tempswafalse \fi
536
       \setbox\@tempboxa\vtop{\vskip\@tempdima \global\pcol@bg@paintedfalse
537
         \ifpcol@paired\else \advance\c@page\@ne \fi
538
         \let\pcol@bg@from\pcol@ncolleft \let\pcol@bg@to\pcol@ncol
539
         \pcol@bg@paintpage}%
540
541
     \else
       \def\reserved@a{\vskip\@tempdima \global\pcol@bg@paintedfalse
542
         \ifpcol@havelastpage \ifx\set@color\relax\else
543
           \pcol@bg@@paintpage \pcol@bg@@paintbox{Pp}%
544
         \fi\fi}%
545
       \setbox\pcol@tempboxa\vbox{%
546
         \let\pcol@bg@preposttop\pcol@bg@preposttop@left
547
         \let\pcol@bg@from\z@ \let\pcol@bg@to\pcol@ncolleft \reserved@a}%
548
549
       \ifpcol@bg@painted \@tempswatrue \else \@tempswafalse \fi
       \setbox\@tempboxa\vbox{\ifpcol@paired\else \advance\c@page\@ne \fi
550
         \let\pcol@bg@preposttop\pcol@bg@preposttop@right
551
         \let\pcol@bg@from\pcol@ncolleft \let\pcol@bg@to\pcol@ncol
552
         reserved@a}%
553
       \ifvoid\pcol@rightpage\else
554
         \pcol@Logstart{\@outputpage{rightset}}%
555
         \setbox\pcol@rightpage\vbox to\textheight{\unvbox\pcol@rightpage \vfil}%
556
         \pcol@Logend{\@outputpage{rightset}}%
557
       \fi
558
559
     \fi
     \ht\pcol@tempboxa\z@ \dp\pcol@tempboxa\z@
560
     \ht\@tempboxa\z@ \dp\@tempboxa\z@
561
     \ifodd\c@page
562
                                                     \pcol@swapcolumnfalse \fi
     \ifnum\pcol@ncolleft<\pcol@ncol\else
                                                     \pcol@swapcolumnfalse \fi
563
     \ifpcol@output\else \ifpcol@havelastpage\else \pcol@swapcolumnfalse \fi\fi
564
     \@tempcnta\c@page
565
     \ifpcol@paired\else \advance\@tempcnta\@ne
                                                     \pcol@swapcolumnfalse \fi
566
567
     \ifpcol@swapcolumn \pcol@outputpage@r\c@page \pcol@outputpage@l\@tempcnta
568
     \else
                         \pcol@outputpage@l\c@page \pcol@outputpage@r\@tempcnta
569
     \fi
     \global\pcol@havelastpagefalse \gdef\pcol@bg@preposttop@left{0pt}%
570
571
     \global\let\pcol@bg@preposttop@right\pcol@bg@preposttop@left
572
     \global\let\pcol@mparbottom@out\pcol@mparbottom@zero
     \endgroup}
573
574
```

 $\colloutputpage@1$ The macro $\colloutputpage@1(page)$, used solely in our own version of \colloutputpage , at $\pcolloutputpage dr$ first lets $\populate page \phase \$ \pcol@outputpage@ev \@outputpage. That is, even when this macro is invoked after \pcol@outputpage@r due to swapped parallel-paging, this assignment cancels the increment of \copage done in IATFX's \Coutputpage or in other word \pcolCCoutputpage because in this case parallel-pages are paired. Then we make \Othemargin \let-equal to \evensidemargin if two-side typesetting is in effect and \copage is even, or to \oddsidemargin otherwise for the reference in \pcolo outputpage@ev as shown shortly.

Next, if background painting took place in \@outputpage, we let \everyvbox have the macro invocation \pcol@outputpage@ev $\langle b_l \rangle$ to be expanded to the following sequence so that they are the leading materials in the \vbox to be \shipout; examination if the document is processed by a Japanese LATEX named pLATEX and then, if so, a control sequence \yoko to put materials naturally; the painted background b_l shifted right by \@themargin; \nointerlineskip to inhibit \baselineskip insertion after b_l ; emptying \everyvbox to ensure nothing will be inserted into internal \vboxes; and the assignment of \yoko to \let it be \relax if necessary. This trick with \everyvbox is necessary¹⁶¹ because b_l should be put before \pcol@Outputpage puts the page header, or the header would be overlaid by regions, e.g., $R_{\{t,T\}}$ in natural cases.

The tricky elements to handle \yoko in the sequence is necessary for pIATEX whose \@outputpage has \yoko as the first element of the \vbox to be \shipout, because \yoko must be the first element of a box but our \everyvbox to put background would make it non-first. That is by the tricky elements, the \vbox should have \yoko as the first element from \everyvbox and then that put by pIATEX's \@outputpage is nullified by \let\yoko\relax in the \everyvbox to be shipped out. On the other hand in ordinary IATEX, \yoko does not appear in the \vbox or is modified. The examination of the use of pIATEX is also trickily done by comparing the expansion results of \meaning\yoko and \string\yoko. Since the former results in the tokens "\yoko" which \string\yoko gives us iff \yoko is a primitive of underlying TEX being pTEX if so, the comparison should give us equality iff pIATEX is in use¹⁶².

Then we invoke \pcol@Coutputpage being (p)LATEX's original version of \Coutputpage to ship out \Coutputbox finally.

The macro $\colorightpage@r\langle page \rangle$ performs similar operations but it does them only when $\colorightpage \neq \bot$ to mean we are in an paracol environment with parallel-paging or outside it but in the page in which it resides. Other differences are as follows; $\langle page \rangle$ can be page(p) + 1 for non-paired right parallel-pages; \colorightpage prior to the invocation of \colorightpage ; and b_r is given to $\colorightpage@ev$ as its argument.

575 \def\pcol@outputpage@l#1{%

```
\pcol@Logstart{\@outputpage{left}}%
576
     \global\c@page#1\relax
577
     \let\@themargin\oddsidemargin
578
     \if@twoside\ifodd\c@page\else \let\@themargin\evensidemargin \fi\fi
579
     \if@tempswa \everyvbox{\pcol@outputpage@ev\pcol@tempboxa}\fi
580
581
     \pcol@Coutputpage
     \pcol@Logend{\@outputpage{left}}}
582
583
   \def\pcol@outputpage@r#1{%
584
     \begingroup
585
     \ifvoid\pcol@rightpage\else
586
       \global\c@page#1\relax
       \let\@outputbox\pcol@rightpage
587
       \pcol@Logstart{\@outputpage{right}}%
588
       \let\@themargin\oddsidemargin
589
       \if@twoside\ifodd\c@page\else \let\@themargin\evensidemargin \fi\fi
590
       \ifpcol@bg@painted \everyvbox{\pcol@outputpage@ev\@tempboxa}\fi
591
592
       \pcol@@outputpage
593
       \pcol@Logend{\@outputpage{right}}%
594
     \fi
```

 $^{^{161} \}mathrm{Unless}$ we rewrite **\Coutputpage**.

 $^{^{162}}$ Unless some other T_EX has a primitive named \yoko. This examination is more strict than that with \pfmtname for \ifpcol@bfbottom.

```
595 \endgroup}
596 \def\pcol@outputpage@ev#1{%
597 \edef\reserved@a\meaning\yoko}\edef\reserved@b{\string\yoko}%
598 \ifx\reserved@a\reserved@b \yoko\fi
599 \moveright\@themargin\box#1\nointerlineskip \everyvbox{}%
600 \ifx\reserved@a\reserved@b \let\yoko\relax \fi}
601
```

9 Starting New Column-Page

\pcol@startcolumn The macro \pcol@startcolumn $\langle f \rangle$ is invoked from \pcol@output with f = 1 and \pcol@ freshpage with f = 0 to start a new column-page. This macro has two additional functions to LATEX's \@startcolumn, one for page-wise footnotes and the other for coloring.

First, if the page p in which the new column-page resides has page-wise footnotes in $\pi^f(p) = \col@footins$ because the column is not the leading one, we temporarily shrink \@colht and \@colroom by the space required to put $\pi^f(p)$ by \pcol@shrinkcolbyfn during the trial of deferred float placement, remembering the existence of the footnotes by letting \@tempdimb = $-\skip\pcol@footins$ which should be 0 otherwise. This shrinkage is essentially required when $p < p_t$ because $\pi^f(p)$ has been fixed to be a part of p and thus deferred floats cannot push footnotes down to succeeding pages. In the case of $p = p_t$, the shrinkage is also desirable to avoid unnecessary pushing down of footnotes which TEX has decided to be in p.

Then after trying put deferred floats in the column-page by $\langle \texttt{Ctryfcolumn} \text{ and } \mathsf{pcol} \texttt{Ctrynextcolumn}$ as done in LATEX's $\langle \texttt{Qstartcolumn}, \texttt{we} \rangle \texttt{insert} \pi^f(p)$, if it is has some footnotes, by letting $\mathsf{footins}$ have it by $\mathsf{pcol} \texttt{Qgetcurrfoot}$ so that TEX will be aware of the footnotes when it examines the page break of the column-page. That is, if $p < p_t$ the $\mathsf{insertion}$ is to keep the vertical space for $\pi^f(p)$ in the building process of the column-page in p because any page-wise footnotes cannot be added to p any more, and thus $\pi^f(p)$ is preserved until the page p is shipped out. On the other hand if $p = p_t$, page-wise footnotes in p can grow further and thus $\mathsf{inserted}$ footnotes will be captured again by $\mathsf{pcol} \texttt{Qoutput} \texttt{Qswitch}$ or $\mathsf{pcol} \texttt{Q}$ startpage. Therefore, if $p = p_t$, we release $\pi^f(p)$ to $\mathsf{Qfreelist}$.

Then if $p = p_t$, we also \insert deferred footnotes in Φ until their total height reaches \@colht by \pcol@deferredfootins if f = 1 to mean this macro is invoked from \pcol@ output¹⁶³. Note that the deferred footnote \insertion in the case of f = 0 will be done afterward when \pcol@freshpage does \pcol@restartcolumn at its tail. Also note that \pcol@ deferredfootins examines if \@tempdimb = 0 to mean $\pi^f(p) = \bot$ and thus \skip\footins should be taken into account in its extraction of the footnotes from Φ .

Then after restoring \colht and canceling the temporary shrinkage of \colroom , we invoke \colcavecolorstack to save column-page's color context into Γ_s so that coloring \specials to reestablish Γ_s will be put at its top if it has something when we leave it.

```
602 %% Starting New Column Page
603
604 \def\pcol@startcolumn#1{%
605 \@tempdima\@colht \@tempdimb\z@
606 \ifvoid\pcol@footins\else
607 \pcol@shrinkcolbyfn\@colht\pcol@footins\@tempdimb
608 \fi
609 \global\@colroom\@colht
610 \@tryfcolumn\@deferlist
```

¹⁶³The \insertion of $\pi^{f}(p)$ also requires f = 1 but this examination is redundant because $\pi^{f}(p) = \bot$ definitely if f = 0.

```
\if@fcolmade\else
611
       \pcol@trynextcolumn
612
       \ifpcol@scfnote \ifnum#1>\z@
613
         \ifvoid\pcol@footins\else
614
            \edef\pcol@currfoot{\pcol@footins}%
615
616
            \pcol@getcurrfoot\copy
            \pcol@Log\pcol@startcolumn{insert}\footins
617
            \insert\footins{\unvbox\footins}%
618
            \ifnum\pcol@page=\pcol@toppage
619
620
              \pcol@Fb
621
              \@cons\@freelist\pcol@footins
              \pcol@Fe{startcolumn(pagefn)}%
622
            \fi
623
         \fi
624
          \ifnum\pcol@page=\pcol@toppage
625
            \pcol@deferredfootins\pcol@startcolumn \fi
626
627
       \fi\fi
     \fi
628
     \advance\@tempdima-\@colht
629
     \global\advance\@colroom\@tempdima
630
631
     \global\advance\@colht\@tempdima
     \pcol@savecolorstack}
632
```

633 \def\pcol@trynextcolumn{\begingroup

- 634 \let\reserved@b\@deferlist
- 635 \global\let\@deferlist\@empty
- 636 \let\@elt\@scolelt
- 637 \reserved@b
- 638 \end{group}

```
639
```

10 Background Painting

 $\label{eq:product} $$ \ C_b, C_b^1, C_b^1$ are made let-equal to $$ \ C_b, C_b^1$ are made let-equal to $$ \ C_b, C_b^1$ or $$ (C_L, C$) by \col@buildcolseprule and \coutputpage for background painting of columns and column-separating gaps, and referred to by column scanning loops in $$ \ col@bg@paint@ii and \col@bg@columnleft. The control sequence \col@bg@to is also referred to by \col@bg@paint@ii scans c \in [C_b^0, C_b^1-1$ rather than $$ [C_b^0, C_b^1$]. Since this decrement is done whenever a painting macro is used regardless some setting of C_b^1, \col@bg@to has default setting with C to avoid unbound reference at the decrement. Note that since this decrement is done in a $$ wbox and an appropriate setting must have been done if C_b^1 is referred in $$ col@bg@paint@ii, this decrement and default setting are safe. $$$

640 %% Background Painting 641

642 \let\pcol@bg@to\pcol@ncol

\pcol@bg@paintpage The macros \pcol@bg@@paintpage, \pcol@bg@@paintcolumns and \pcol@bg@@paintbox{A} \pcol@bg@@paintpage are made \let-equal to their interface counterparts \pcol@bg@paintpage, \pcol@bg@paint \pcol@bg@paintcolumns columns and \pcol@bg@paintbox by \pcol@zparacol if some coloring package has been \pcol@bg@@paintcolumns loaded. Otherwise, these interface macros are \let-equal to \relax for first two and \@gobble \pcol@bg@paintbox for the last, so that macros in \output routine freely use them unaware of coloring capability. \pcol@bg@@paintbox One exception is in \@outputpage which uses \pcol@bg@@paintpage and \pcol@bg@@paintbox explicitly when it is outside **paracol** environments, examining the availability of coloring.

> The macro \pcol@bg@paintpage and \pcol@bg@@paintpage are used in \@outputpage to paint backgrounds of regions $R_a^{[c]}$ for all $a \in \{T, B, L, R, G, C, t, b, l, r\}$ and $c \in [C_b^0, C_b^1)$ for a = C while $c \in [C_b^0, C_b^1 - 1)$ for a = G. Therefore, the macro invokes \pcol@bg@paint@i with two \pcol@bg@paint@ii{ A_b }{ A_g }{ A_c }, letting A_b = TBLR, A_g = G and A_c = C in the first invocation and then $A_b = \texttt{tblr}$ and $A_g = A_c = \emptyset$ in the second.

> The macro $\pcol@bg@paintcolumns$ is used in $\pcol@buildcolseprule$ and $\pcol@$ buildcselt to paint backgrounds of regions $R_a^c(i)$ for $c \in [C_b^0, C_b^1 - 1)$ and $R_c^c(i)$ for $c \in [C_b^0, C_b^1)$. Therefore, the macro invokes $\col@bg@paint@i with \col@bg@paint@ii giving it <math>A_b = \emptyset$, $A_g = g$ and $A_c = c$.

> The macro $\cal{pcol@bg@paintbox}{A}$ is used in the following macros with A shown in the parentheses to paint the backgrounds of regions $R_{\{a_1,a_2\}}$ where $(a_1,a_2) \in \{(S,s), (F,f), (N,n), ($ (P, p).

```
\pcol@outputelt (Ff), \pcol@ioutputelt (Nn, Ff), \pcol@buildcselt (Ss),
\pcol@output@start (Pp), \pcol@output@clear (Ff),
\pcol@makeflushedpage (Ff), \pcol@imakeflushedpage (Nn),
\pcol@output@end (Nn).
```

The macro \Coutputpage also uses the function but \pcolObg@Opaintbox explicitly with A = Pp. Therefore \pcol@bg@paintbox invokes \pcol@bg@paint@i with \pcol@bg@paint@ ii giving it $A_b = A$ and $A_g = A_c = \emptyset$.

```
643 \def\pcol@bg@@paintpage{%
```

```
644
     \pcol@bg@paint@i{%
```

```
\pcol@bg@paint@ii{TBLR}{G}{C}\pcol@bg@paint@ii{tblr}{}}}
645
648
```

\pcol@bg@paint@i The macro \pcol@bg@paint@i{body} is used in \pcol@bg@@paintpage, \pcol@bg@@paint columns and \pcol@bg@@paintbox to paint backgrounds by a sequence of \pcol@bg@paint@ii specified in $\langle body \rangle$. The painted background is built in \Ctempboxa being a \vtop having a null \vskip as its first element so that everything put in the box is below its reference point at its top. Then, before invoking $\col@bg@paint@ii</code> in <math>\langle body \rangle$, we do the followings; $\col@bally$ let $\ifpcol@bg@painted = false$ to indicate so far any painted background are produced; make \pcol@bg@leftmargin \let-equal to \pcol@lrmargin to use this \dimen register locally with the more appropriate alias; negate $\pagerim locally$ to calculate H_T easily; decrement C_b^1 by one locally for the column scanning loop for $c \in [C_b^0, C_b^1 - 1)$ in \pcol@bg@paint@ii; and **\offinterlineskip** to inhibit inter-line **\baselineskip** insertion in the box. Then after the invocation of the sequence of $\colorby colorby colorby colorby and closing the box, we let$ the height, depth and width of the box be 0 so that it does not occupy any real space in the outer box in which the box is put. Finally, if $\ightarrow \label{eq:pointed} = true$ meaning that some painted backgrounds are built in the box, we put the box into the outer box surrounding it by \nointerlineskip to inhibit inter-line \baselineskip insertion before and after it. 649 \def\pcol@bg@paint@i#1{%

- 650 \setbox\@tempboxa\vtop{\vskip\z@
- 651 \global\pcol@bg@paintedfalse
- 652 \let\pcol@bg@leftmargin\pcol@lrmargin
- 653 \pagerim-\pagerim \advance\pcol@bg@to\m@ne
- 654 \offinterlineskip #1}%
- 655 \ht\@tempboxa\z@ \dp\@tempboxa\z@ \wd\@tempboxa\z@
- 656 \ifpcol@bg@painted \nointerlineskip \box\@tempboxa \nointerlineskip \fi}

First we invoke $\colorsep{0.1}$ with $\ifpcolorsep{0.1}$ we invoke $\colorsep{0.1}$ with $\ifpcolorsep{0.1}$ with $\colorsep{0.1}$ and $\ifpcolorsep{0.1}$ we invoke $\colorsep{0.1}$ and $\colorsep{0.1}$ we invoke $\colorsep{0.1}$ for all $a \in A_b$ and c = -1 to paint the background of R_a . Second, we invoke $\colorsep{0.1}$ for all $a \in A_b$ and c = -1 to paint the background of R_a . Second, we invoke $\colorsep{0.1}$ background and the $\ifpcolorsep{0.1}$ background of $\colorsep{0.1}$ background of $\colorsep{0.1}$ background of $\colorsep{0.1}$ background of $\colorsep{0.1}$ background background of $\colorsep{0.1}$ background background of $\colorsep{0.1}$ background bac

```
657 \def\pcol@bg@paint@ii#1#2#3{%
```

- $658 \verb| \col@bg@swappage\ifpcol@bg@swap\fi$
- 659 \@tfor\reserved@b:=#1\do{\pcol@bg@paintregion\reserved@b\m@ne}%
- 660 \pcol@bg@swappage\ifpcol@swapcolumn\fi
- 661 \@tfor\reserved@b:=#2#3\do{%
- 662 \pcol@currcol\pcol@bg@from \@whilenum\pcol@currcol<\pcol@bg@to\do{%
- 663 \pcol@bg@paintregion\reserved@b\pcol@currcol
- 664 \advance\pcol@currcol\@ne}}%
- 665 \@tfor\reserved@b:=#3\do{\pcol@bg@paintregion\reserved@b\pcol@currcol}}

\pcol@bg@swappage The macro \pcol@bg@swappage $\langle if \rangle$ \fi is used solely in \pcol@bg@paint@ii but twice with $\langle if \rangle = \ifpcol@bg@swap$ and then with $\langle if \rangle = \ifpcol@swapcolumn$, to let \pcol@bg@ leftmargin and \ifpcol@bg@swap have values for mirroring according to the truth values of $\langle if \rangle$ and \iffctwoside and the parity of page(p) of the page p for which background painting is taking place. That is, they are let have the values as follows.

$$W = \begin{cases} \texttt{\basis} page(p) \mod 2 = 1 \ \lor \texttt{\basis} \texttt{\basis$$

 $= \begin{cases} (W, \ false) & page(p) \bmod 2 = 1 \lor \langle if \rangle = false \\ (W_P - (W + W_T + 2in), \ true) & page(p) \bmod 2 = \land \langle if \rangle = true \end{cases}$

Note that $W_P - (W + W_T + 2 \text{ in})$ means the right margin width minus 1 in with given left margin width W, and thus $W_M = \text{pcol@bg@leftmargin} + 1$ in gives us the right margin width we need in mirrored background painting.

```
666 \def\pcol@bg@swappage#1#2{%
```

- 667 \pcol@bg@leftmargin\oddsidemargin \pcol@bg@@swapfalse
- 668 \ifodd\c@page\else
- 669 \if@twoside \pcol@bg@leftmargin\evensidemargin \fi
- 670 **#1%** \ifpcol@{bg@swap,swapcolumn}
- 671 \pcol@bg@@swaptrue
- 672 \advance\pcol@bg@leftmargin\textwidth \advance\pcol@bg@leftmargin2in
- 673 \advance\pcol@bg@leftmargin-\paperwidth

```
674
       \pcol@bg@leftmargin-\pcol@bg@leftmargin
```

```
675
        #2% \fi
```

```
676
      \fi}
```

```
677
```

 $\col@bg@paintregion$ The macro $\col@bg@paintregion(a)(c)$ is used only in $\col@bg@paint@ii{A_b}{A_q}{A_c}$ $\colored pcolored paintregion@i but as many times as <math>|A_b| + |A_g|(C_b^1 - C_b^0 - 1) + |A_c|(C_b^1 - C_b^0)$ to paint background region $R_a^{[c]}$ specified by \pcol@bg@@.a with color $B_a^c = \pcol@bg@color@.a.@.c$ or, if it is undefined, $B_a = \col@bg@color@\cdot a.$

If R_a^c or R_a is defined, the painted background is built in \@tempboxa with \vtop having null vertical skip at its top and by $\col@bg@paintregion@i{F_x}{F_y}{F_b}$ where the arguments are defined in the body of the macro \pcol@bg@@.a and thus we need triple \expandafter to give them to the macro. Prior to the invocation of the macro, we let reserved@a = a' have $a \cdot \mathbf{Q} \cdot c$ if B_a^c is defined for $a \in \{G, C, g, c\}$, or a otherwise definitely for $a \notin \{G, C, g, c\}$.

Then \pcol@bg@paintregion@i calculates $x_0 = \langle @tempdima, y_0 = \langle @tempdimb, x_1 = \langle @tempdimc and y_1 = \langle dimen@ of the region <math>R_a^{[c]}$ by $\col@bg@calculate\langle z \rangle \langle z_0 \rangle \{F\}$ giving it $(z, z_0, F) \in \{(x_0, 0, F_x), (y_0, 0, F_y), (x_1, x_0, F_w), (y_1, y_0, F_h)\}$, where (x_0, y_0) and (x_1, y_1) is the left-top and right-bottom corner of the painting region in the text-area coordinate, i.e., left-right and top-down coordinate whose origin is at the left-top corner of the leftmost column. Next we modify $\{x, y\}_{\{0,1\}}$ for extension by \pcol@bg@addext $\langle z \rangle \{s\} \{d\}$ with $(z, s, d) \in \{(x_0, -, 1), (y_0, -, t), (x_1, \emptyset, r), (y_1, \emptyset, b)\}.$

Now we have $[(x_0, y_0)(x_1, y_1)]$ and thus, if not mirrored, we place $R_a^{[c]}$ at (x_0, y_0) by a vertical skip of y_0 and shifting a **\box** for the region right by x_0 by **\moveright**, and paint the box putting a vrule of $(x_1 - x_0)$ wide and $(y_1 - y_0)$ tall, letting vcurrent@color nition of \set@color. On the other hand if mirroring is to be done, the region should be $[(W_T - x_1, y_0)(W_T - x_0, y_1)]$ and thus the shift amount for \moveright of the \hbox is $(W_T - x_1)$.

Then after \pcol@bg@paintregion@i finishes its work, \pcol@bg@paintregion lets the switch $\ \ e = true$ because we painted $R_a^{[c]}$, lets the height, depth and width of \mathbb{Q} tempboxa be 0 to make it a phantom, and then put it into the outside box opened by $\colorbig@paint@i.$ On the other hand, if neither B_r^c nor B_r defined to mean the background painting of the region is not specified, we do nothing.

```
678 \def\pcol@bg@paintregion#1#2{%
     \@ifundefined{pcol@bg@color@#1@\number#2}%
679
       \label{eq:logithtargen} {\def\reserved@a{\#1}}{\def\reserved@a{\#1@\number#2}}\
680
     \@ifundefined{pcol@bg@color@\reserved@a}\relax
681
682
       {\setbox\@tempboxa\vtop{\vskip\z@
683
           \expandafter\expandafter\expandafter
             \pcol@bg@paintregion@i\csname pcol@bg@@#1\endcsname}%
684
685
        \global\pcol@bg@paintedtrue
        \ht\@tempboxa\z@ \dp\@tempboxa\z@ \wd\@tempboxa\z@ \box\@tempboxa}}
686
   \def\pcol@bg@paintregion@i#1#2#3#4{%
687
     \pcol@bg@calculate\@tempdima\z@{#1}%
688
     \pcol@bg@calculate\@tempdimb\z@{#2}%
689
     \pcol@bg@calculate\@tempdimc\@tempdima{#3}%
690
     \pcol@bg@calculate\dimen@\@tempdimb{#4}%
691
     \col@bg@addext\@tempdima{-}{1}\pcol@bg@addext\@tempdimc{}{r}\%
692
     \pcol@bg@addext\@tempdimb{-}{t}\pcol@bg@addext\dimen@{}{b}%
693
     \vskip\@tempdimb
694
695
     \ifpcol@bg@@swap
       \advance\@tempdima-\@tempdimc \@tempdima-\@tempdima
696
```

```
\advance\@tempdimc-\textwidth \@tempdimc-\@tempdimc
697
       \moveright\@tempdimc\hbox{%
698
         \advance\dimen@-\@tempdimb
699
         \edef\current@color{\@nameuse{pcol@bg@color@\reserved@a}}\pcol@set@color
700
         \vrule\@width\@tempdima\@height\dimen@}%
701
702
     \else
       \moveright\@tempdima\hbox{%
703
         \advance\@tempdimc-\@tempdima \advance\dimen@-\@tempdimb
704
         \edef\current@color{\@nameuse{pcol@bg@color@\reserved@a}}\pcol@set@color
705
         \vrule\@width\@tempdimc\@height\dimen@}%
706
     fi
707
708
```

\pcol@bg@dimen

 $\colored bg@calculate$ The macro $\colored bg@calculate\langle z \rangle \langle z_0 \rangle \langle F \rangle$ is used in $\colored bg@paintregion@i$ and \col $\colorsection bg@addext$ to accumulate dimensional values specified in F into a \dimen register z with initial $\colorsymbol{pcolorgative}$ value z_0 . The specification F is a sequence of \colorsymbol{lef} to add f to z, $\colorsymbol{pcolorgative}$ $\colorseparate{product} by F^-$ from z, or macros expanded to either of them.

The macro makes $\colorsymbol{pcolorsymbol{$ $z = z_0$, and then does what is specified in F. Therefore, $\operatorname{lelt}(f)$ appearing directly or indirectly in F does $\alpha \sqrt{f}$ for the accumulation. On the other hand, $\rho \sqrt{f}$ for subtraction, does F^- , and then remake $\ensuremath{\colsephi}$ advance. Note that f may be expanded to a negative amount having '-' its beginning to results in $\operatorname{Qelt}(f)$ expanded to $\langle advance \langle z \rangle - \langle f' \rangle$ with some positive amount f', but this double negation is legitimate in TFX and is equivalent to $\alpha \sqrt{z} \langle f' \rangle$. The macro $\rho collog @negative is used in the$ following macros.

\pcol@bg@ext@inf@l, \pcol@bg@ext@inf@r, \pcol@bg@ext@inf@t, \pcol@bg@@t, \pcol@bg@@b, \pcol@bg@@l, \pcol@bg@@r, \pcol@bg@@p.

```
709 \def\pcol@bg@calculate#1#2#3{\let\pcol@bg@dimen#1\relax
710
     \let\@elt\pcol@bg@advance \pcol@bg@dimen#2\relax #3}
711 \def\pcol@bg@negative#1{\let\@elt\pcol@bg@nadvance #1\relax
     \let\@elt\pcol@bg@advance}
712
713 \def\pcol@bg@advance#1{\advance\pcol@bg@dimen#1\relax}
714 \def\pcol@bg@nadvance#1{\advance\pcol@bg@dimen-#1\relax}
715
```

 $\colorsection density of the macro \colorsection density of the macro \colorsection density of the last the macro \colorsection density of the last the macro \colorsection density of the last the las$ $\colorsymbol{pcolObgOextOinfOl times with } (z, s, d) \in \{(x_0, -, 1), (y_0, -, t), (x_1, \emptyset, r), (y_1, \emptyset, b)\}, to perform extension on a$ \pcol@bg@ext@inf@r \dimen register z.

First the macro gets $e = \col@bg@ext@.d.@.a' \in e_a^{|c|}(\{x, y\}^{\{+, -\}})$ where $a' = \col@bg@ext@.d.@.a' \in e_a^{|c|}(\{x, y\}^{\{+, -\}})$ \pcol@bg@ext@inf@t $\colored bg@ext@inf@b \in \{a \cdot @ \cdot c, a\}$. Then if e < 9000 pt being a finite extension, we let $z \leftarrow z \pm e$ according to s, i.e. + if $s = \emptyset$ while - if s = -. Otherwise, i.e., e > 9000 pt for a infinite extension, let e' be the value shown below by invoking \pcol@bg@ext@inf@.d

$$e' = \begin{cases} -(W_M - W_R) & d = 1\\ W_P - (W_M - W_R) & d = r\\ -(H_M - H_R) & d = t\\ H_P - (H_M - H_R) & d = b \end{cases}$$

where $W_M - W_R$ is specified by \pcol@bg@pageleft and $H_M - H_R$ by \pcol@bg@pagetop. Then we let $z = e' \pm (e - 10000 \text{ pt})$ according to s again, i.e., move z inside by (10000 pt - e)from e'.

```
716 \def\pcol@bg@addext#1#2#3{%
```

```
\dimen@ii\@nameuse{pcol@bg@ext@#3@\reserved@a}\relax
717
     \ifdim\dimen@ii<9000\p@\relax \advance#1#2\dimen@ii
718
     \else
719
       \pcol@bg@calculate#1\z@{\@nameuse{pcol@bg@ext@inf@#3}}%
720
       \advance\dimen@ii-\@M\p@ \advance#1#2\dimen@ii
721
722
     \fi}
723 \def\pcol@bg@ext@inf@l{\pcol@bg@negative\pcol@bg@pageleft}
724 \def\pcol@bg@ext@inf@r{\pcol@bg@negative\pcol@bg@pageleft
725
     \pcol@bg@paperwidth}
726 \def\pcol@bg@ext@inf@t{\pcol@bg@negative\pcol@bg@pagetop}
727 \def\pcol@bg@ext@inf@b{\pcol@bg@negative\pcol@bg@pagetop
     \pcol@bg@paperheight}
728
729
```

 $\col@bg@paperwidth$ The following macros specify the whole or a part of $F \in \{F_x, F_y, F_w, F_h\}$ being the body of $\col@bg@paperheight$ $\col@bg@c.a$ for background painting regions $R_a^{[c]}$.

\pcol@bg@paperheight
 \pcol@bg@pageleft
 \pcol@bg@textheight
 \pcol@bg@columnleft
 \pcol@bg@columnright
 \pcol@bg@columnwidth
 \pcol@bg@columnsep

 $\label{eq:product} $$ \ W_P - 2W_R = paperwidth - 2pagerim (t,T,b,B,r,R) $$ \ Coll g g paperheight = $H_P - 2H_R = paperheight - 2pagerim (b,B) $$ \ Coll g g pageleft = $W_M - W_R = (\ Coll g g leftmargin + 1 in) - pagerim $$$ $$ \ Coll g g leftmargin + 1 in) - pagerim $$$ \ Coll g g leftmargin + 1 in $$ $$ \ Coll g leftmargin + 1 in $$ $$ \ Coll g leftmargin + 1 in $$ $$ \ Coll g leftmargin + 1 in $$ $$ \ Coll g leftmargin + 1 in $$ $$ \ Coll g leftmargin + 1 in $$ $$ \ Coll g leftmargin + 1 in $$ $$ \ Coll g leftmargin + 1 in $$ \ C$

$$(t, T, b, B, l, L, r, R)$$

 $\label{eq:product} $$ \ = H_M - W_R$$$ = (\topmargin + \headheight + \headsep + 1 in) - \grim (t, T, b, B)$$ \collected by the equation of the three that the three the three the text the tight + \topmaxdepth $$$ \collected by the text height = H_T = \topmaxdepth $$$

$$\label{eq:pcol_bg_columnwidth} w_c = \col_columnwidth c \quad (c,C)$$

 $\verb|pcol@bg@columnsep=g_c=\verb|pcol@columnsep|c (g,G)|$

Note that \pagerim in F means -\pagerim because its sign is reversed by \pcol@bg@paint@ i. The macros are used in \pcol@bg@@.a whose region identifier a is shown in parentheses above, but besides them \pcol@bg@paperwidth is also used in \pcol@bg@ext@inf@r, \pcol@ bg@paperheight in \pcol@bg@ext@inf@b, \pcol@bg@pageleft in \pcol@bg@ext@inf@l and \pcol@bg@ext@inf@r, and \pcol@bg@pagetop in \pcol@bg@ext@inf@t and \pcol@bg@ext@ inf@b. Also note that \pcol@bg@textheight is used in \pcol@output@clear while it is temporarily redefined in \pcol@output@start and \pcol@output@end.

```
730 \def\pcol@bg@paperwidth{\@elt\paperwidth \@elt{2\pagerim}}
```

```
731 \def\pcol@bg@paperheight{\@elt\paperheight \@elt{2\pagerim}}
```

732 \def\pcol@bg@pageleft{\@elt{1in}\@elt\pcol@bg@leftmargin \@elt\pagerim}

733 \def\pcol@bg@pagetop{\@elt{1in}\@elt\topmargin \@elt\headheight \@elt\headsep

734 \@elt\pagerim}

```
735 \def\pcol@bg@textheight{\@elt\textheight \@elt\@maxdepth}
```

^{736 \}def\pcol@bg@columnleft{%

- 737 \@tempcnta\pcol@bg@from \@whilenum\@tempcnta<\pcol@currcol\do{%
- 739 \@elt{\@nameuse{pcol@columnsep\number\@tempcnta}}%
- 740 \advance\@tempcnta\@ne}}
- 741 \def\pcol@bg@columnright{\pcol@bg@columnleft \pcol@bg@columnwidth}
- 742 \def\pcol@bg@columnwidth{\@elt{\@nameuse{pcol@columnwidth\number\pcol@currcol}}}

```
743 \def\pcol@bg@columnsep{\@elt{\@nameuse{pcol@columnsep\number\pcol@currcol}}}
```

 $\col@bg@preposttop</code> Besides the macros shown above, <math>\col@bg@@.a$ uses the following macros defined by macros $\col@bg@preposttop@left$ using $\col@bg@paintpage$, $\col@bg@paintcolumns$ or $\col@bg@paintbox$.

- \pcol@bg@preposttop being \pcol@bg@preposttop@left or \pcol@bg@preposttop@right for a ∈ {p, P} by \@outputpage and \pcol@output@end, the latter of which may define only the left one if the closing environment is not parallel-paged. That is, both of left and right macros are usually equivalent, but the right one can be smaller than the left if we have two or more (last pages of) paracol environments in a page and the closing environment is not parallel-paged while some others are. In such case, \@outputpage or \pcol@output@start, another macro referring to them, must paint the region below \pcol@bg@preposttop@right in the right page as a part of pre-environment stuff or post-environment stuff by \letting \pcol@bg@preposttop@ be \pcol@bg@preposttop@ left and \pcol@bg@preposttop@right for the left and right parallel-pages respectively. Both macros have common initial value 0.
- \pcol@bg@columntop and \pcol@bg@columnheight for $a \in \{c, g\}$ by \pcol@buildcol seprule and \pcol@buildcselt.
- \pcol@bg@spanningtop and \pcol@bg@spanningheight for $a \in \{s,S\}$ by \pcol@ buildcselt.
- \pcol@bg@floatheight for $a \in \{f, F\}$ by \pcol@outputelt, \pcol@ioutputelt, \pcol@ioutputelt, \pcol@output@clear and \pcol@makeflushedpage
- $\col@bg@footnoteheight for a \in \{n, N\}$ by $\col@ioutputelt$, $\col@imakeflushed page and <math>\col@output@end$.

744 \def\pcol@bg@preposttop@left{0pt}
745 \let\pcol@bg@preposttop@right\pcol@bg@preposttop@left
746

\pcol@bg@preposttop \pcol@bg@preposttop@left \pcol@bg@columntop \pcol@bg@columnheight \pcol@bg@floatheight \pcol@bg@floatheight \pcol@bg@spanningtop \pcol@bg@spanningheight \pcol@bg@@c The macros \pcol@bg@@.a define arguments F_x , F_y , F_w and F_h to be passed to \pcol@ \pcol@bg@@C bg@paintregion@i in their bodies to calculate (x_0, y_0) and $(x_1 - x_0, y_1 - y_0)$ for regions $R_a^{[c]}$ \pcol@bg@@g as shown below in the form of $(x_0, y_0) + (x_1 - x_0, y_1 - y_0)$ (to have (x_1, y_1)), where $H^c =$ $\label{eq:local_$ $\plaue{prod} \plaue{prod} \pl$ $\pcol@bg@@S$ and $H^p = \pcol@bg@preposttop$ calculated by macros which invoke background painting $\poiled good macros, while s^n = \skip\footins.$ \pcol@bg@@T R_{c}^{c} : $(W_{c}, H^{c}) + (w_{c}, h^{c})$ \pcol@bg@@b R_C^c : $(W_c, 0) + (w_c, H_T)$ \pcol@bg@@B \pcol@bg@@l R_{q}^{c} : $((W_{c} + w_{c}), H^{c}) + (g_{c}, h^{c})$ \pcol@bg@@L R_G^c : $((W_c + w_c), 0) + (g_c, H_T)$ \pcol@bg@@r $R_{\{s,S\}}$: $(0, H^s) + (W_T, h^s)$ \pcol@bg@@R $R_{\{t,T\}}$: $(-(W_M - W_R), -(H_M - H_R)) + ((W_P - 2W_R), H_M - H_R)$ \pcol@bg@@f \pcol@bg@@F $R_{\{b,B\}}$: $(-(W_M - W_R), H_T) + ((W_P - 2W_R), (H_P - 2H_R) - ((H_M - H_R) + H_T))$ \pcol@bg@@n $R_{\{l,L\}}$: $(-(W_M - W_R), 0) + ((W_M - W_R), H_T)$ \pcol@bg@@N $R_{\{r,R\}}$: $(W_T, 0) + ((W_P - 2W_R) - ((W_M - W_R) + W_T), H_T)$ \pcol@bg@@p \pcol@bg@@P $R_{\{f,F\}}$: (0, 0) + (W_T , h^f) $R_{\{n,N\}}$: $(0, H_T - (h^n + s^n)) + (W_T, h^n + s^n)$ $R_{\{p,P\}}$: $(0, H^p) + (W_T, H_T - H^p)$ 747 \def\pcol@bg@@c{% {\pcol@bg@columnleft}% 748 749{\@elt\pcol@bg@columntop}% 750{\pcol@bg@columnwidth}% {\pcol@bg@columnheight}} 751752 \def\pcol@bg@@C{% {\pcol@bg@columnleft}% 753 754{}% {\pcol@bg@columnwidth}% 755{\pcol@bg@textheight}} 756 757 \def\pcol@bg@@g{% {\pcol@bg@columnright}% 758 759{\@elt\pcol@bg@columntop}% {\pcol@bg@columnsep}% 760{\pcol@bg@columnheight}} 761762 \def\pcol@bg@@G{% {\pcol@bg@columnright}% 763 764{}% {\pcol@bg@columnsep}% 765 {\pcol@bg@textheight}} 766 767 \def\pcol@bg@@s{% 768 {}% {\pcol@bg@spanningtop}% 769 770 {\@elt\textwidth}% {\pcol@bg@spanningheight}} 771 772 \def\pcol@bg@@t{% {\pcol@bg@negative\pcol@bg@pageleft}% 773 {\pcol@bg@negative\pcol@bg@pagetop}% 774 {\pcol@bg@paperwidth}% 775

```
{\pcol@bg@pagetop}}
776
777 \def\pcol@bg@@b{%
     {\pcol@bg@negative\pcol@bg@pageleft}%
778
     {\pcol@bg@textheight}%
779
     {\pcol@bg@paperwidth}%
780
     {\pcol@bg@paperheight
781
       \pcol@bg@negative{\pcol@bg@pagetop \pcol@bg@textheight}}}
782
   \def\pcol@bg@@l{%
783
     {\pcol@bg@negative\pcol@bg@pageleft}%
784
785
     {}%
     {\pcol@bg@pageleft}%
786
     {\pcol@bg@textheight}}
787
788 \def\pcol@bg@@r{%
     {\@elt\textwidth}%
789
790
     {}%
791
     {\pcol@bg@paperwidth
        \pcol@bg@negative{\pcol@bg@pageleft \@elt\textwidth}}%
792
     {\pcol@bg@textheight}}
793
794 \def\pcol@bg@@f{%
795
     {}%
     {}%
796
     {\@elt\textwidth}%
797
     {\pcol@bg@floatheight}}
798
799 \def\pcol@bg@@n{%
     {}%
800
801
     {\pcol@bg@textheight
       \pcol@bg@negative{\pcol@bg@footnoteheight \@elt{\skip\footins}}}%
802
     {\@elt\textwidth}%
803
     {\pcol@bg@footnoteheight \@elt{\skip\footins}}}
804
805 \def\pcol@bg@@p{%
806
    {}%
     {\@elt\pcol@bg@preposttop}%
807
808
     {\@elt\textwidth}%
     {\pcol@bg@textheight \pcol@bg@negative{\@elt\pcol@bg@preposttop}}}
809
810 \let\pcol@bg@@S\pcol@bg@@s
811 \let\pcol@bg@@T\pcol@bg@@t
812 \let\pcol@bg@@B\pcol@bg@@b
813 \let\pcol@bg@@L\pcol@bg@@l
814 \let\pcol@bg@@R\pcol@bg@@r
815 \let\pcol@bg@@F\pcol@bg@@f
816 \let\pcol@bg@@N\pcol@bg@@n
817 \let\pcol@bg@@P\pcol@bg@@p
818
```

11 Special Output Routines

11.1 Dispatcher

 $\label{eq:product} $$ \ f \in F = \{ \texttt{start}, \texttt{switch}, \texttt{flush}, \texttt{clear}, \texttt{end} \}$ has our own \colloop@switch \outputpenalty code less than -10000 to invoke the corresponding macro \collootput@.f. \colloop@flush The code macros are given to \colloinvokeoutput as its argument by \colloparacol \colloop@clear (f = \texttt{start}), \colloop@switchcol (f = \texttt{switch}), \colloop@clear (f$

```
switch), and \ (f = end) to set one of them into \ utputpenalty, so that the
other user \pcol@specialoutput examines which special function is invoked.
```

```
819 %% Special Output Routines: Dispatcher
820
821 \def\pcol@op@start{-10010}
822 \def\pcol@op@switch{-10011}
823 \det\col@op@flush{-10012}
824 \def\pcol@op@clear{-10013}
825 \def\pcol@op@end{-10014}
826
```

\pcol@specialoutput The macro \pcol@specialoutput is invoked solely in \pcol@output to invoke our own or ETFX 's special output routine. It examines if $P = \operatorname{outputpenalty} \in \{\operatorname{pcoloop} f \mid f \in F\}$ and then, if so, before invoking $\colloutput@f$, we rebuild $\loutput@loutput@f$. and the last vertical skip as done in IATFX's \@specialoutput. We also let \outputpenalty = -10000^{164} so that \vsize is correctly set to \@colroom in the second half of \pcol@output after this macro finishes.

> Otherwise, i.e., if $P \notin \{ \text{pcoloop0} \cdot f \mid f \in F \}$, we simply invokes LATEX's \@specialoutput^{165}. 827 \def\pcol@specialoutput{%

```
\ifnum\outputpenalty=\pcol@op@start\relax
828
       \let\reserved@a\pcol@output@start
829
     \else\ifnum\outputpenalty=\pcol@op@switch\relax
830
       \let\reserved@a\pcol@output@switch
831
832
     \else\ifnum\outputpenalty=\pcol@op@flush\relax
833
       \let\reserved@a\pcol@output@flush
     \else\ifnum\outputpenalty=\pcol@op@clear\relax
834
       \let\reserved@a\pcol@output@clear
835
     \else\ifnum\outputpenalty=\pcol@op@end\relax
836
       \let\reserved@a\pcol@output@end
837
     \else \let\reserved@a\@specialoutput
838
     \fi\fi\fi\fi\fi
839
840
     \ifnum\outputpenalty=-\@Miv\relax
841
       \ifvoid\footins\else \pcol@Log\dummy{dummy}\footins \fi
842
     \fi
     \ifx\reserved@a\@specialoutput\else
843
       \global\setbox\@holdpg\vbox{\unvbox\@holdpg \unvbox\@cclv
844
         \setbox\@tempboxa\lastbox \unskip}%
845
       \outputpenalty-\@M
846
     \fi
847
     \reserved@a}
848
849
```

Building Starting Page 11.2

\pcol@output@start The macro \pcol@output@start is invoked solely from \pcol@specialoutput to process the special **\output** request made in **\pcol@zparacol** and to build the *starting page* from which parallel columns start possibly with the stuff preceding \begin{paracol}, or pre-environment stuff in short. First, we turn $\ ifpcol@output = true$ so that $\ vert$ requests for page breaks are processed by our own macros such as $pcol@makecol</code> hereafter. Then we let <math>p = p_b =$

 $^{^{164}}$ It can be any value larger than -10004.

¹⁶⁵With footnote logging if **\outputpenalty** = -10004.

 $p_t = 0$ and $\Pi = \emptyset$ because we have nothing for $q < p_t = 0$. We also move **@deferlist** to **@dbldeferlist** and then let **@deferlist** be empty because all column-wise deferred floats become page-wise. In this float importation, as discussed in item-(4) of §1.8, we force all floats in the list have depth 0 to ensure no one has 1sp to conform our own and old-fashioned pagewise float placement mechanism¹⁶⁶. We then and let $\Phi = \bot$ because we don't have any deferred footnotes.

Next we calculate $H = H_r - (H_m + H_f + H_b)$ where $H_r = \colroom$; H_m is the heightplus-depth of the main vertical list in \colorootexilon ; H_f is the sum of $\skip\footins$, the heightplus-depth of \colrootexilon and \belowfootnotexkip , if \colrootexilon is not \perp or 0 otherwise; and $H_b = \textfloatsep$ if the pre-environment stuff has bottom floats or 0 otherwise. That is, H is the room for each of column-page in the starting page. Then we examine if $H < 1.5 \times \begin{bmatrix} begin{bmatrix} begi$

After that we invoke \pcol@startpage to let it produce $\pi(p_t)$ for the starting page $p_t = 0$ letting \pcol@currpage be empty so that the macro will not refer to it. The page $\pi(0)$ is usually empty but can have non-empty $\pi^i(0)$ with imported deferred floats which are now page-wise. Moreover, we can have two or more pages if deferred page-wise floats produce float pages. However, we can be unaware of these effects of floats because the resulting Π^+ with them is correct of course.

Then let $\topskip = \col@topskip$ being the value at $\begin{paracol}, and \ifpcol@firstpage = false, because we have the starting page without pre-environment stuff and thus the first item of each column will be at its top.$

```
850 %% Special Output Routines: Building First Page
851
852 \def\pcol@output@start{%
853
     \global\pcol@outputtrue
     \global\pcol@page\z@ \global\pcol@toppage\z@ \global\pcol@basepage\z@
854
855
     \global\let\pcol@pages\@empty
     \global\let\@dbldeferlist\@deferlist \global\let\@deferlist\@empty
856
     {\def\@elt##1{\global\dp##1\z@}\@dbldeferlist}%
857
     \setbox\z@\box\pcol@topfnotes
858
     \@tempdima\@colroom
859
     \advance\@tempdima-\ht\@holdpg \advance\@tempdima-\dp\@holdpg
860
     \ifvoid\footins\else
861
       \advance\@tempdima-\skip\footins
862
863
       \advance\@tempdima-\ht\footins \advance\@tempdima-\dp\footins
       \advance\@tempdima-\belowfootnoteskip
864
     \fi
865
     \ifx\@botlist\@empty\else \advance\@tempdima-\textfloatsep \fi
866
     \ifdim\@tempdima<1.5\baselineskip
867
       \setbox\@cclv\box\@holdpg \@makecol
868
       \pcol@outputfalse \@outputpage \pcol@outputtrue
869
       \global\let\pcol@currpage\@empty \pcol@startpage
870
       \global\topskip\pcol@topskip \global\pcol@firstpagefalse
871
```

 $^{^{166}\}mathrm{Though}$ having $\mathtt{1sp}$ is almost impossible.

¹⁶⁷ We can be unaware of our customization for synchronization in \collocombinefloats because \collocats because because because

Otherwise, i.e., if $H \ge 1.5 \times \text{baselineskip}$, we invoke \pcol@makenormalcol to make the pre-environment stuff as the spanning stuff of the starting page. The macro is different from \@makecol as follows; the height of resulting \@outputbox is natural rather than \textheight; merged footnotes is excluded if any; and the skip of \textfloatsep is added below the bottom floats also if any,

Then we let h be the height-plus-depth of Qoutputbox being the spanning stuff and shrink Qcolht by h. Next if $h > H_B = \texttt{pcol@bg@preposttop@cleft}$, pcol@bg@preposttop@left, being the bottom of the previous paracol environment (having right parallel-page) or 0 if the current page does not have it, to mean we have ordinary single-columned stuff in pre-environment stuff, we paint its background by pcol@bg@praintbox temporarily letting pcol@bg@textheight = h so that $y_0 = H_B$ and $y_1 = h$ for $R_{\{p,P\}}$. This background painting is not only for $\pi^b(0)$ which we acquire from from Qcreelist by Qnext and let have the spanning stuff, but also for pcol@tightpage if $C_L < C$ to mean parallel-paging for which we temporarily increment c@page by one if non-paired.

We also let $\pi^h(0)$ be the shrunk \@colht, and $\pi^t(0)$ be \topskip if h = 0 assuming that the page does not have any spanning stuff¹⁶⁸ to typeset column-pages from the top of the page, or otherwise be 0 together with \topskip to inhibit the ordinary \topskip insertion.

As for $\pi^m(0)$, we define it as follows, referring to $\mathcal{M} = \text{pcol@mparbottom@out} = \{M_L^l, M_L^r, M_R^l, M_R^r\}$, where M_X^x has exactly one element mpar(h, t) which may be the position of last marginal notes in the last paracol environment in the page we are working on, or $M_X^x = \{mpar(0,0)\}$ if such marginal note or the environment itself does not exist in the page. On the other hand, B = Qmparbottom may have non-zero for the bottom edge of the last marginal note in pre-environment stuff including the last paracol environment if any. Therefore, what we need to do is to let $M_L^x = \{mpar(0, B)\}$ to reflect the marginal node whose bottom is at B and which can be different from what M_L^x had, where x is the target margin in the pre-environment stuff determined by if@mparswitch, the parity of page(0) and if@reversemargin.

The replacement is done by $\col@do@mpbout$ which invokes $\col@do@mpbout@whole(m_L^l) \langle m_L^r \rangle \langle M_R^l \rangle \langle M_R^r \rangle$ where $m_L^x \in \{M_L^x, \col@do@mpbout@elem(M_L^x)\}$ whose choice is made according that $x \in \{l, r\}$ is the target margin (latter) or not (former). Therefore, prior to the invocation of $\col@do@mpbout@ubout@whole so that it \col@do@mpbout@elem \col@do@mpbout@elem to let it be expanded to <math>\col@dol@mparbottom@out with its four arguments, and \col@do@mpbout@elem to let it be expanded to <math>\col@dol@mparbottom@out \col@dol@mpbout@elem to feach M_{\{L,R\}}^{\{l,r\}}$ in the resulting \mathcal{M} with mpar(t-h,b-h) to have what we give to $\pi^m(0)$. This replacement transforms the coordinates for text area to that for columns, and makes it possible for the first marginal note in each margin in the paracol environment we now start to exploit the space for pre-environment stuff even if it is tall extraordinarily.

Then we let $\pi(0)$ have $\pi^i(0)$ and $\pi^m(0)$ shown above, and $\pi^p(0) = \backslash cOpage$, $\pi^f(0) = \bot$ and $\pi^s(0) = \emptyset$ by $\backslash pcolOdefcurrpage$, and let $\land ifpcolOfirstpage = true$ because $\pi^b(0)$ has pre-environment stuff.

872 \else

- 873 \pcol@makenormalcol
- 874 \@tempdima\ht\@outputbox \advance\@tempdima\dp\@outputbox
- 875 \global\advance\@colht-\@tempdima
- 876 \def\reserved@a{%
- 877 \ifdim\pcol@bg@preposttop=\@tempdima\else

¹⁶⁸Checking the emptiness by \pcol@ifempty does not work well for the very first page of a document because it has a \write as the very first item.

878	\edef\pcol@bg@textheight{\@elt{\number\@tempdima sp}}%
879	\pcol@bg@paintbox{Pp}%
880	\fi}
881	\ifnum\pcol@ncolleft<\pcol@ncol
882	\global\setbox\pcol@rightpage%
883	\ifpcol@paired\else \advance\c@page\@ne \fi
884	\let\pcol@bg@preposttop\pcol@bg@preposttop@right
885	\reserved@a \unvbox\pcol@rightpage}%
886	\fi
887	\pcol@Fb
888	\@next\@currbox\@freelist{\global\setbox\@currbox%
889	$\verb+let+pcol@bg@preposttop+pcol@bg@preposttop@left+$
890	\reserved@a \unvbox\@outputbox}}\pcol@ovf
891	\pcol@Fe{output@start(preenv)}%
892	\global\dimen\@currbox\@colht
893	\ifdim\@tempdima=\z@ \@tempskipa\topskip \else \@tempskipa\z@ \fi
894	\global\skip\@currbox\@tempskipa \global\topskip\@tempskipa
895	\def\pcol@do@mpbout@whole##1##2##3##4{%
896	\xdef\pcol@mparbottom@out{{##1}{##2}{##3}{##4}}}%
897	\def\pcol@do@mpbout@elem\@elt##1##2{\@elt{0}{\number\@mparbottom}}%
898	\pcol@do@mpbout
899	\pcol@bias@mpbout{-\@tempdima}%
900	<pre>\pcol@defcurrpage{\number\c@page}\@currbox\voidb@x{}{\pcol@mparbottom@out}%</pre>
901	\global\pcol@firstpagetrue
902	\fi

Then regardless of H, we do the followings for all columns $c \in [0, C)$ to build κ_c , after initializing \@colroom to be \@colht, and invoking \pcol@floatplacement to reinitialize the parameters of column-wise float placement.

First, if we have let $\mathsf{topskip} = 0$ with the pre-environment stuff, we let $\kappa_c(\beta^b)$ have an invisible \hrule whose height and depth are 0 as the very first vertical item of the column-page. When we visit the column c for the first time afterward, we will \unvbox the box to let T_FX's page builder have ± 0 and the invisible rule. Then the first vertical item of the column-page is added but it is recognized as non-first by TFX's page builder and thus it inserts **\baselineskip** referring to **\prevdepth** as the depth of the last item. The important issue is that the \prevdepth to be referred is assured having its value at \begin{paracol}, which is usually the depth of the last item of spanning stuff, by the following mechanism: (1) \pcol@ invokeoutput invoked in \pcol@zparacol saves \prevdepth in \pcol@prevdepth before the \output request for \pcol@output@start; (2) \pcol@prevdepth is saved in $\kappa_c(\delta)$ by \pcol@ setcurrcolnf invoked from \pcol@output@start as discussed afterward; (3) when the column c is visited for the first time, the special output routine $\colored coutput@start itself (c = 0)$ or \pcol@output@switch (c > 0) restores \pcol@prevdepth from $\kappa_c(\delta)$ by \pcol@getcurrcol; (4) $\pcol@invokeoutput$ which made the \output request for (3) lets \prevdepth have the value of \pcol@prevdepth after the request. Therefore, the baseline progress from the last line of the spanning stuff to the first line of each column-page should be very natural as we see in the third and fourth lines of $\S6$ of Part I.

Then we invoke $\col@setcurrcolnf$ to save the following values for $\kappa_c(e)$ $(e \neq \beta)$; $\kappa_c(\tau) = \col@setcurrcolnf$ to save the following values for $\kappa_c(e)$ $(e \neq \beta)$; $\kappa_c(\tau) = \col@setcurrcolnf$ to save the following values for $\kappa_c(\delta) = \col@setcurrcolnf$ as discussed above; $\kappa_c(\lambda_t) = \kappa_c(\lambda_m) = \kappa_c(\lambda_b) = \emptyset$ because $\col@makenormalcol and \col@combinefloats invoked from it emptied them; <math>\kappa_c(\lambda_d) = \emptyset$ as discussed above; $\kappa_c(\nu_t) = \col@colmmber$, $\kappa_c(\nu_b) = \col@colmmber$ and $\kappa_c(\nu_t) = \col@colmmber$ as initialized by $\col@colmmber$ invoked from $\col@colmmber$; $\kappa_c(\rho_t) = \colmmber$ as initialized by $\colmmetric{0}{0}$. and $\kappa_c(\rho_b) = \texttt{bottomfraction} \times \texttt{Qcolht}$ as initialized by Qfloatplacement; $\kappa_c(\sigma)$ is defined by ifQnobreak and ifQafterindent at the time of $\texttt{begin}\{\texttt{paracol}\}$; and $\kappa_c(\varepsilon) = \texttt{verypar}$ at the time of $\texttt{begin}\{\texttt{paracol}\}$. We also let $\kappa_c(\beta^p) = 0$ because p = 0 and $\kappa_c(\beta^r) = \texttt{Qcolroom}$ defined above. In addition, we let $S_c = \emptyset$ because we don't have any column-page having been completed.

We also examine if $\hat{\gamma}_0^c = \collecturcelector c$ is defined and, if so, acquire an \insert from $\fill freelist$ to let $\gamma_0^c = \collecturcelector c$ have the coloring \special for the color defined in $\hat{\gamma}_0^c$ by invoking $\collectlecterelector c$ being the original $\set@collecturcelector c$ with nullification of $\special c$.

```
\global\@colroom\@colht \pcol@floatplacement
903
     \pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do{%</pre>
904
905
       \pcol@Fb
       \@next\@currbox\@freelist{\global\setbox\@currbox\vbox{%
906
907
         \ifdim\topskip=\z0 \hrule\@height\z0\@width\z0 \fi}}\pcol@ovf
       \pcol@Fe{output@start(col)}%
908
       \pcol@setcurrcolnf
909
       \global\count\@currbox\z@
910
       \global\dimen\@currbox\@colroom
911
       \expandafter\gdef\csname pcol@shipped\number\pcol@currcol\endcsname{}%
912
913
       \pcol@ifccdefined
         {\@next\@currbox\@freelist{\global\setbox\@currbox\vbox{%
914
           \def\current@color{\pcol@ccuse{}}\let\aftergroup\@gobble
915
            \pcol@set@color}}\pcol@ovf}%
916
917
         {\def\@currbox{\voidb@x}}%
918
       \pcol@ccxdef{\@currbox}%
919
      \advance\pcol@currcol\@ne}%
```

Finally, we let c = pcol@currcol = 0 for the first column, and regain the parameters in κ_0 by pcol@getcurrcol. Then before putting $\kappa_0(\beta^b)$ to the main vertical list by unvbox returning $\kappa_0(\beta)$ to @freelist by @cons because it has become useless so far, we save the color context just with γ_0^c into Γ_s by pcol@savecolorstack because Γ is emptied by pcol@ zparacol. Then we insert footins through itself to the main vertical list if it is not \bot and thus has footnotes to be merged. This insertion is different from other footnote insertion because footins is not unvboxed but is put as a whole and is followed by penaltyinterlinepenalty, so that footnote with inappropriate glue discarding, which we will discuss in §18. We also add a penalty 10000 or interlinepenalty according to if@nobreak = true or not to allow the first column to start from a new page when its first item is taller than the room in the starting page.

```
\global\pcol@currcol\z@
920
921
     \pcol@getcurrcol
922
     \pcol@savecolorstack
923
     \pcol@Fb
     \@cons\@freelist\@currbox \unvbox\@currbox
924
     \pcol@Fe{output@start(col)}%
925
926
     \ifvoid\footins\else
       \pcol@Log\pcol@output@start{insert}\footins
927
       \insert\footins{\box\footins\penalty\interlinepenalty}%
928
929
     \fi
     \if@nobreak \nobreak \else \addpenalty\interlinepenalty \fi}
930
931
```

- \pcol@makenormalcol The macro \pcol@makenormalcol is invoked solely from \pcol@output@start to let \@output box have the pre-environment stuff as spanning stuff of the starting page. The operations this macro performs are very similar to those of \@makecol, which in fact is used in this macro itself, but has the following differences.
 - If \ifpcol@mgfnote = true, we exclude footnotes in \footins from \@outputbox, because they are merged with page-wise footnotes given in columns, by saving it into \@tempboxa during the building process and restoring it from the box register.
 - (2) If pre-environment stuff does not have bottom floats, we build \Coutputbox by ourselves without relying on \Cmakecol because the skips put into the bottom (or near it) by the macro is harmful to making pre-environment stuff and parallel columns naturally connected. Therefore, we move \Choldpg to \Coutputbox adding \footins to its tail if any by \pcolCcombinefootins, and then combine top floats if any by \pcolCcombinefloats¹⁶⁹. In addition, we clear \Cmidlist and returns its contents to \Cfreelist as \Cmakecol does.
 - (3) If pre-environment stuff has bottom floats, on the other hand, we use \@makecol to build pre-environment stuff in \@outputbox moving \@holdpg into \box255 prior to the invocation¹⁷⁰. Also before invocation in addition, we temporarily let \ifpcol@lastpage = true to let \@combinefloats = \pcol@combinefloats used in \@makecol put a vertical skip of \textfloatsep below the bottom floats so that the floats are well separated from the top of multi-column stuff in the starting page. We also nullify \@textbottom by making it \let-equal to \relax because it is unnecessary to put an infinitely stretchable skip at the bottom¹⁷¹, and let \vbadness = 10000 to avoid an inevitable underfull message because \@makecol lets \@outputbox as tall as \textheight.
 - (4) In both cases but especially that with bottom floats, resulting \Coutputbox is decapsulated by \unvbox to make its height *natural*.

Note that the special function for synchronized column-page in \clicklencembinefloats used directly or indirectly in this macro, on the other hand, is not active in the invocation because \clicklencembinelect

```
932 \def\pcol@makenormalcol{%
     \ifpcol@mgfnote \setbox\@tempboxa\box\footins \fi
933
934
     \begingroup
     \ifx\@botlist\@empty
935
       \ifvoid\footins \setbox\@outputbox\box\@holdpg
936
937
       \else
                        \pcol@combinefootins\@holdpg\footins
938
       \fi
       \pcol@Fb
939
       \let\@elt\relax \xdef\@freelist{\@freelist\@midlist}%
940
941
       \pcol@Fe{makenormalcol}%
```

¹⁶⁹Since we do not have bottom floats, the order of materials in the resulting \Coutputbox being top floats, main text and footnotes should be consistent with other pages with any IAT_EX including $pIAT_EX$.

 $^{^{170}}$ Therefore the order of footnotes and bottom floats is consistent with other pages and columns, i.e., footnote-first in the native LATEX while float-first in pLATEX, for example.

¹⁷¹Even if unharmful.

 $^{^{172}}$ We could put them at the bottom by keeping them somewhere and insert them in \pcol@outputcolumns, but it will cause another problem that the numbers of the figures and footnotes are smaller than those in column-pages which are above them.

```
942
       \global\let\@midlist\@empty
       \pcol@combinefloats
943
944
     \else
       \pcol@lastpagetrue
945
       \setbox\@cclv\box\@holdpg \let\@textbottom\relax \vbadness\@M
946
       \@makecol
947
948
     \fi
     \global\setbox\@outputbox\vbox{\unvbox\@outputbox}%
949
     \endgroup
950
     \ifpcol@mgfnote \setbox\footins\box\@tempboxa \fi}
951
952
```

11.3 Column-Switching

First, we examine if the column-switching is to close a spanning text, i.e., ifpcol@sptext = true and c = 0, and if so we do the following; let h_p be the height of pcol@prespan having pre-spanning-text stuff if it is not \bot , or 0 if \bot to mean we have had a page break in the spanning text; add h_p to @colroom which we temporarily shrank when the spanning text starts; add an element span(H, h) to the tail of $\pi^s(p_t) = pcol@sptextlist$ by pcol@getcurrpage and pcol@defcurrpage, where H is h_p plus the total height of top floats measured by pcol@ addflhd, and h is the height-plus-depth of @holdpg having (a part of) spanning text, represented in the form of integers and thus expanded with number; shift @holdpg left by pcol@ shiftspanning if the column-0 is not the leftmost due to column-swapping; and then put prespanning-text stuff and (maybe shifted) @holdpg into @holdpg itself so as to let @holdpg have everything in the column-page 0 as usual.

Note that it can be $\col@prespan = \bot$ if spanning text had a page break (or multiple ones) in it as shown above. This empty pre-spanning-text stuff, however, does not always means that we have no top floats because the page break in the spanning text can produce a column-page with top floats which are deferred from the previous page(s), or though unlikely the spanning text itself has float environments. Therefore, the measurement of the total height of top floats are always necessary. Also note that we perform these operations at the first column-switching for column-scaning from c = 0 with $\ifpcol@sptext = true$, i.e., prior to the synchronization itself which takes place afterword, as explained shortly.

Then regardless of the operations above, we acquire an \insert from \@freelist by \@next for $\kappa_c(\beta)$ to store the current column-page in (maybe modified) \@holdpg by \pcol@clearcst@ unvbox to add uncoloring \specials to rewind the color stack Γ^c at the bottom and possibly coloring ones to establish that saved in Γ_s at the top as the color context for the column-page when it has the first item.

Then if $\texttt{footins} \neq \bot$, we perform one of the followings.

- If page-wise footnote typesetting is in effect and $p = p_t$, we save \footins into $\pi^f(p)$ by the sequence of \pcol@getcurrpinfo to get $\pi(p)$, \pcol@savefootins to move it in $\pi^f(p)$, and \pcol@defcurrpage to update $\pi(p)$ with $\pi^f(p)$.
- If page-wise footnote typesetting is in effect but $p < p_t$, we simply discard the contents of **\footins** by making it \bot , because **\footins** should have $\pi^f(p)$ which has been already fixed.
• If column-wise footnote typesetting is in effect, by $\col@savefootins we save \footins into \pcol@currfoot, which should be <math>\perp$ in other cases, so that it will be saved into $\kappa_c(\tau)$ by $\pcol@setcurrcol afterward.$

Then if c = 0, we invoke \pcol@setpageno to reflect the jump of \c@page made in the building process of the column-page to $\pi(q)$ for all $q \in [p, p_t]$. After that, we save c's columncontext into κ_c by \pcol@setcurrcol and let $\kappa_c(\beta^p) = p$ and $\kappa_c(\beta^r) = \Colroom$. 953 %% Special Output Routines: Column-Switching 954955 \def\pcol@output@switch{% 956 \ifpcol@sptext\ifnum\pcol@currcol=\z@ \ifvoid\pcol@prespan \dimen@\z@ \else \dimen@\ht\pcol@prespan \fi 957 958 \global\advance\@colroom\dimen@ 959 \pcol@addflhd\@toplist\pcol@textfloatsep \pcol@getcurrpinfo\@tempcnta\@tempdima\@tempskipa 960 \@tempdimb\ht\@holdpg \advance\@tempdimb\dp\@holdpg 961 \@cons\pcol@sptextlist{{\number\dimen@}{\number\@tempdimb}}% 962 963 \pcol@defcurrpage{\number\@tempcnta}\pcol@spanning\pcol@footins 964 {\pcol@sptextlist}{\pcol@mparbottom}% \pcol@shiftspanning\@holdpg 965 966 \setbox\@holdpg\vbox{\unvbox\pcol@prespan \unvbox\@holdpg}% 967 \fi\fi \pcol@Fb 968 969 \@next\@currbox\@freelist{\global\setbox\@currbox\vbox{ 970 \pcol@clearcst@unvbox\@holdpg}}\pcol@ovf \pcol@Fe{output@switch}% 971 972 \def\pcol@currfoot{\voidb@x}% 973 \ifvoid\footins\else 974 \ifpcol@scfnote 975 \ifnum\pcol@page=\pcol@toppage 976 \pcol@getcurrpinfo\@tempcnta\@tempdima\@tempskipa 977 \pcol@Log\pcol@output@switch{save}\footins \pcol@Fb 978 979 \pcol@savefootins\pcol@footins \pcol@Fe{output@switch(pagefn)}% 980 \pcol@defcurrpage{\number\@tempcnta}\pcol@spanning\pcol@footins 981 {\pcol@sptextlist}{\pcol@mparbottom}% 982 \else 983 984 \pcol@Log\pcol@output@switch{discard}\footins 985 \setbox\@tempboxa\box\footins 986 \fi 987 \else \pcol@Log\pcol@output@switch{save}\footins 988 \pcol@Fb 989 990 \pcol@savefootins\pcol@currfoot \pcol@Fe{output@switch(colfn)}% 991 \fi 992\fi 993 \ifnum\pcol@currcol=\z@ \pcol@setpageno \fi 994\pcol@setcurrcol 995 996 \global\count\@currbox\pcol@page 997 \global\dimen\@currbox\@colroom

Next, we examine if ifpcol@sptext = true and c = 0 again, and if so we broadcast if@nobreak and if@afterindent, or in other words $\kappa_c(\sigma)$, and tokens in $everypar = \kappa_c(\varepsilon)$.

to pretend all columns follow the spanning text. That is, for each column e, we restore its column-context from κ_e by \pcol@getcurrcol, let \if@nobreak and \if@afterindent have the values for $c \ (\in \{0, C-1\})$ and \everypar = $\kappa_c(\varepsilon)$, and then save the context to κ_e by \pcol@setcurrcol so that $\kappa_e(\sigma) = \kappa_c(\sigma)$ and $\kappa_e(\varepsilon) = \kappa_c(\varepsilon)$. After that, we \globally turn \ifpcol@sptext = false to give it the default state.

Note that this broadcast is essential when the spanning text has sectioning commands to have consistent settings of the page break inhibition, the skip above the another sectioning command following them, and the indentation of the first paragraph, for all columns. On the other hand, broadcasting of \everypar is natural even when it does not have sectioning commands because all columns may be considered following the spanning text. Also note that, as mentioned in the explanation of the first examination at the beginning of this macro, we perform these operations at the first column-switching for column-scanning from c = 0 with \ifpcol@sptext = true prior to the synchronization following the spanning text. This means, if \if@nobreak = true, \penalty = 10000 is inserted at the top and bottom end of the space for spanning text in the columns such that $c \neq 0$, the former by this column-scan and the latter by the column-switching to c made after the synchronization. Therefore, if our synchronization mechanism and TEX's page builder once agreed both end can be in a page, both end will not chosen as page break points¹⁷³.

```
998
      \let\reserved@a\@nobreakfalse \let\reserved@b\@afterindentfalse
999
      \ifpcol@sptext\ifnum\pcol@currcol=\z@
1000
        \if@nobreak \let\reserved@a\@nobreaktrue \fi
        \if@afterindent \let\reserved@b\@afterindenttrue \fi
1001
        \@temptokena\everypar
1002
        \pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do{%</pre>
1003
          \pcol@getcurrcol \reserved@a \reserved@b \everypar\@temptokena
1004
          \pcol@setcurrcol
1005
1006
         \advance\pcol@currcol\@ne}%
1007
        \global\pcol@sptextfalse
1008
      \fi\fi
```

Finally we invoke $\col@sync$ for the synchronization if $\ifpcol@sync or \ifpcol@clear$ is true, and then $\col@restartcolumn$ to restart the current column-page d if $\ifpcol@clear = false$ to mean ordinary (but possibly synchronized) column-switching or $\ifpcol@clear = true$ but $\ifpcol@sync = true$ too to mean pre-flushing column height check, before finishing \output routine letting $\ifpcol@sync = false$ for next column-switching.

```
1009 \@tempswafalse \ifpcol@sync \@tempswatrue \fi \ifpcol@clear \@tempswatrue \fi
1010 \if@tempswa \pcol@sync \fi
1011 \@tempswatrue
1012 \ifpcol@clear \ifpcol@sync\else \@tempswafalse \fi\fi
1013 \if@tempswa \pcol@restartcolumn \fi
1014 \global\pcol@syncfalse}
1015
```

 $\col@shiftspanning$ The macro $\col@shiftspanning(b)$ is used in $\col@makecol and \col@output@switch to let box register b have itself but shifted left by <math>W_T - w_0 = \textwidth - \columnwidth$ so that the left edge of its contents spanning text is aligned to the left edge of the leftmost column being different from column-0 due to column-swapping, i.e., if $\iftpcol@swapcolumn = true$

 $^{^{173}}$ As for c = 0, its top end of spanning text is a feasible break point to make the penalty insertion asymmetric. Therefore, we need to reinvestigate if the condition of the broadcast is really appropriate, and, if inappropriate, have to go back to the old implementation in which \ifpcol@sync is included in the condition. Otherwise, if proved appropriate, we will have to consider to make the penalty insertion symmetric by adding \nobreak at the top of spanning text in c = 0.

and \c@page mod 2 = 0. Note that \c@page is *not* obtained from $\pi^p(p)$ by the invokers but have the value when the \output request is made to let invokers work, and thus have the correct value even when a jump occurs prior to the request.

```
1016 \def\pcol@shiftspanning#1{%
1017 \ifpcol@swapcolumn\ifodd\c@page\else
1018 \setbox#1\vbox{\@tempdima\textwidth \advance\@tempdima-\columnwidth
1019 \moveleft\@tempdima\box#1}
1020 \fi\fi}
1021
```

\pcol@restartcolumn The macro \pcol@restartcolumn is invoked from \pcol@output@switch or \pcol@freshpage to restart the current column-page $d = \pcol@nextcol which becomes c = \pcol@currcol by$ $the very first assignment in this macro. Then we restore the column-context in <math>\kappa_c$ by \pcol@ getcurrcol and let $p = \kappa_c(\beta^p)$ and \@colroom = $\kappa_c(\beta^r)$ before returning $\kappa_c(\beta)$ to \@freelist by \@cons because it has become useless so far. We also restore the page context of p by \pcol@ getcurrpage.

```
1022 \def\pcol@restartcolumn{%
```

- 1023 \global\pcol@currcol\pcol@nextcol
- 1024 \pcol@getcurrcol
- 1025 \global\pcol@page\count\@currbox
- 1026 \global\@colroom\dimen\@currbox
- 1027 \pcol@Fb

```
1028 \@cons\@freelist\@currbox
```

1029 \pcol@Fe{restartcolumn(col)}%

```
1030 \pcol@getcurrpage
```

Then we perform footnote \insertion as follows.

- (1) If footnote typesetting is page-wise and $p = p_t$, we do the followings.
 - (a) Put the contents of $\kappa_c(\beta^b)$ by \pcol@putbackmvl to make the color context in .dvi consistent with the current .tex's one, and to save pre-spanning-text stuff into \pcol@prespan if we are opening a spanning text.
 - (b) Put \penalty = 10000 by \nobreak if \if@nobreak = true or \interlinepenalty by \addpenalty¹⁷⁴ otherwise, as the page break penalty at the returning point. Note that adding the \penalty will be nullified by T_EX if $\kappa_c(\beta^b)$ has nothing and thus, if the column-page is still empty when we leave from it, its emptiness without any items is assured. Also note that the penalty insertion here *looks* essential to keep T_EX's page builder from confusing with page-wise footnotes which it has not seen in a column-page¹⁷⁵.
 - (c) If $\pi^f(p) \neq \bot$, let \pcol@currfoot and then \footins have the footnotes in it by an \edef and \pcol@getcurrfoot, return the \insert for them to \@freelist, invoke \pcol@shrinkcolbyfn to shrink \@colht temporarily by their total height and to remember the existence of them with \@tempdimb = -\skip\footins, and then \insert the footnotes so that it contributes to the building process of the column-page to be restarted. Otherwise, i.e. if $\pi^f(p) = \bot$, \@colht is unchanged and \@tempdimb = 0.

¹⁷⁴As done in \@specialoutput but \penalty\interlinepenalty should be sufficient.

 $^{^{175}\}mathrm{At}$ least a test with tall page-wise footnotes gave us a confusing result.

builder from holding too large number of footnotes unprocessed causing confused ordering on presenting them to **\output** routine.

- (2) If footnote typesetting is page-wise but $p < p_t$, we do the followings.
 - (a) If $\pi^f(p) \neq \bot$, get it into \footins as done in (1c) but giving \copy to \pcol@ getcurrfoot because $\pi^f(p)$ has been fixed and thus will be kept until it is shipped out, and then \insert it.
 - (b) Put $\kappa_c(\beta^b)$ and the penalty as done in (1a) and (1b).

The order of footnotes, main vertical list and then penalty is essential to ensure that the column-page in $p < p_t$ has room for footnotes whose residence in p has already been fixed.

- (3) If footnote typesetting is column-wise, we do the followings.
 - (a) Put $\kappa_c(\beta^b)$ as done in (1a).
 - (b) If $\kappa_c(ft) \neq \bot$, get it by \pcol@getcurrfoot returning the \insert to \@freelist, and then \insert it.
 - (c) Put a penalty as done in (1b).

The order of main vertical list, footnotes and then penalty is appropriate for column-wise footnotes because they definitely have space in the column-page and T_EX will break the page below the insertion, possibly just below thanks to the penalty, to keep the footnotes and references to them in a page.

```
1031
      \ifpcol@scfnote
        \edef\pcol@currfoot{\pcol@footins}%
1032
        \ifnum\pcol@page=\pcol@toppage
1033
          \@tempdima\@colht \@tempdimb\z@
1034
          \pcol@putbackmvl
1035
          \if@nobreak \nobreak \else \addpenalty\interlinepenalty \fi
1036
1037
          \ifvoid\pcol@footins\else
1038
            \pcol@Fb
            \pcol@getcurrfoot\box \@cons\@freelist\pcol@currfoot
1039
            \pcol@Fe{restartcolumn(pagefn)}%
1040
1041
            \pcol@Log\pcol@restartcolumn{insert}\footins
1042
            \pcol@shrinkcolbyfn\@colht\footins\@tempdimb
            \insert\footins{\unvbox\footins}%
1043
          \fi
1044
          \pcol@deferredfootins\pcol@restartcolumn
1045
1046
          \@colht\@tempdima
1047
        \else
1048
          \ifvoid\pcol@footins\else
            \pcol@getcurrfoot\copy
1049
            \pcol@Log\pcol@restartcolumn{insdmy}\footins
1050
1051
            \insert\footins{\unvbox\footins}%
1052
          \fi
          \pcol@putbackmvl
1053
          \if@nobreak \nobreak \else \addpenalty\interlinepenalty \fi
1054
        \fi
1055
      \else
1056
        \pcol@putbackmvl
1057
1058
        \ifvoid\pcol@currfoot\else
```

```
1059
          \pcol@Fb
          \pcol@getcurrfoot\box \@cons\@freelist\pcol@currfoot
1060
          \pcol@Fe{restartcolumn(colfn)}%
1061
          \pcol@Log\pcol@restartcolumn{insert}\footins
1062
1063
          \insert\footins{\unvbox\footins}%
1064
        \fi
        \if@nobreak \nobreak \else \addpenalty\interlinepenalty \fi
1065
1066
      \fi}
1067
```

\pcol@getcurrcol The macro \pcol@getcurrcol is invoked from the following macros to restore the typesetting \pcol@igetcurrcol parameters of the column $c = \pcol@currcol from \kappa_c$, and to let \columnwidth have $w_c = \pcol@igetcurrcol \pcol@columnwidth <math>c^{176}$.

\pcol@output@switch	\pcol@restartcolumn
\pcol@measurecolumn	\pcol@synccolumn
$\pcol@imakeflushedpage$	$\pcol@iflushfloats$
\pcol@output@end	
	\pcol@output@switch \pcol@measurecolumn \pcol@imakeflushedpage \pcol@output@end

Since we represent κ_c as;

$$\{\kappa_c(\beta)\}\{\kappa_c(\tau)\}\{\kappa_c(\delta)\}\{\kappa_c(\lambda_t)\}\{\kappa_c(\lambda_m)\}\{\kappa_c(\lambda_b)\}\{\kappa_c(\lambda_d)\}\{\kappa_c(\xi)\}\} \\ \{\{\kappa_c(\eta)\}\{\kappa_c(\nu_t)\}\{\kappa_c(\rho_t)\}\{\kappa_c(\nu_b)\}\{\kappa_c(\rho_b)\}\{\kappa_c(\nu_c)\}\{\kappa_c(\sigma)\}\{\kappa_c(\varepsilon)\}\}$$

in the body of $\col@col.c$, we restore first eight by $\col@igetcurrcol</code> giving everything above as its arguments by the expansion of$

\csname pcol@col\number\pcol@currcol\endcsname

and then of the resulting control sequence. Then this macro gives its ninth argument to \pcol@ iigetcurrcol which restores the last eight. We also do

$\verb|global|columnwidth|pcol@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@columnwidth|col@co$

by a pair of **\expandafter** for the first two control sequences.

Note that the restore operations are global, except for $\kappa_c(\beta)$ and $\kappa_d(\tau)$ because they are referred to only in output, including if@nobreak for which @nobreaktrue and @nobreakfalse are defined global by ET_EX . Also note that $\dimen-type$ parameters are saved in the form of integers and thus restoring them needs to specify the unit sp.

```
1068 \def\pcol@getcurrcol{%
      \expandafter\expandafter\pcol@igetcurrcol
1069
        \csname pcol@col\number\pcol@currcol\endcsname
1070
1071
      \expandafter\global\expandafter\columnwidth
1072
        \csname pcol@columnwidth\number\pcol@currcol\endcsname}
1073 \def\pcol@igetcurrcol#1#2#3#4#5#6#7#8#9{%
      \def\@currbox{#1}\def\pcol@currfoot{#2}\global\pcol@prevdepth#3sp\relax
1074
      \gdef\@toplist{#4}\gdef\@midlist{#5}\gdef\@botlist{#6}\gdef\@deferlist{#7}%
1075
      \global\pcol@textfloatsep#8sp\pcol@iigetcurrcol#9}
1076
1077 \def\pcol@iigetcurrcol#1#2#3#4#5#6#7#8{%
      \global\@textfloatsheight#1sp\relax
1078
      \global\@topnum#2\relax \global\@toproom#3sp\relax
1079
      \global\@botnum#4\relax \global\@botroom#5sp\relax
1080
```

¹⁷⁶\hsize and \linewidth are let have w_c and $w_c - \mu$ respectively in \pcol@invokeoutput.

```
\global\@colnum#6\relax
1081
      \global\@afterindentfalse \@nobreaktrue
1082
      \ifcase#7
1083
        \@nobreakfalse \or
1084
1085
        \global\@afterindenttrue \else
1086
        \relax
1087
      \fi
      \global\everypar{#8}}
1088
```

\pcol@getcurrfoot The macro \pcol@getcurrfoot(com) is invoked from \pcol@startcolumn (\copy, $\pi^f(p)$), \pcol@restartcolumn (\copy/\box, $\pi^f(p)/\kappa_c(\tau)$), \pcol@flushcolumn (\box, $\kappa_c(\tau)$) and \pcol@imakeflushedpage (\box, $\kappa_c(\tau)$) to put everything in \pcol@currfoot, having the second element in the parens following macro names, into **\footins** using $\langle com \rangle$ shown as the first element in parens for the box component. That is, if the source $\pi^f(p)$ or $\kappa_c(\tau^b)$ is void, we let \box.\footins be so. Otherwise, we move \box, \count, \dimen and \skip of the source into those of \footins^{177} .

```
1089 \def\pcol@getcurrfoot#1{%
      \ifvoid\pcol@currfoot \global\setbox\footins\box\voidb@x
1090
1091
      \else
1092
        \global\setbox\footins#1\pcol@currfoot
1093
        \global\count\footins\count\pcol@currfoot
1094
        \global\dimen\footins\dimen\pcol@currfoot
1095
        \global\skip\footins\skip\pcol@currfoot
1096
      \fi}
```

\pcol@setcurrcol The macro \pcol@setcurrcol is invoked from \pcol@output@switch, \pcol@measurecolumn \pcol@setcurrcolnf and \pcol@synccolumn to save column-context of $c = \pcol@currcol in \kappa_c$. It is also used in \pcol@setcurrcolnf invoked from \pcol@output@start, \pcol@flushcolumn, \pcol@ imakeflushedpage, \pcol@iflushfloats and \pcol@freshpage for the saving when the column-page is known to have no footnotes.

> The macro \pcol@setcurrcol at first calculates the combined code for \if@nobreak and \if@afterindent, and then saves parameters into κ_c by \xdef to have the sequence shown in the description of \pcol@getcurrcol. Note that \dimen-type parameters are saved by expansions with \number and thus as decimal integers.

> The macro $\colored et as \colored et as \colored$ invoke \pcol@setcurrcol for saving.

1097 \def\pcol@setcurrcol{{\let\@elt\relax

```
\@tempcnta\if@nobreak\if@afterindent\@ne\else\tw@\fi\else\z@\fi
1098
```

- 1099 \expandafter\xdef\csname pcol@col\number\pcol@currcol\endcsname{%
- 1100 {\@currbox}{\pcol@currfoot}{\number\pcol@prevdepth}%

```
{\@toplist}{\@midlist}{\@botlist}{\@deferlist}{\number\pcol@textfloatsep}%
1101
```

- {{\number\@textfloatsheight}% 1102
- 1103 {\number\@topnum}{\number\@botnum}{\number\@botnum}{
- 1104 {\number\@colnum}{\number\@tempcnta}{\the\everypar}}}
- 1105 \def\pcol@setcurrcolnf{\def\pcol@currfoot{\voidb@x}\pcol@setcurrcol}
- 1106

\pcol@putbackmvl The macro \pcol@putbackmvl, solely used in \pcol@restartcolumn, has two functions; color stack restoration and pre-spanning-text stuff preservation. It examines the emptiness of the

 $^{^{177}}$ Moving \count, \dimen and \skip is redundant almost always because it is very unlikely that these footnote parameters are modified dynamically. Moreover, dynamic modification of them is hardly consistent with repetitive self-\insertion of \footins in \pcol@restartcolumn and \@reinserts of LATEX. However, we dare to move them in order to, for example, allow each column has its own footnote parameters.

column-page of the column c to be restarted in $\kappa_c(\beta) = \langle \texttt{Currbox}$. If so, the color stack Γ^c is saved into $\Gamma_s = \col@colorstack@saved by \col@savecolorstack as the opening color$ context of the column-page, and $\column column-page$, and $\column column col$

Otherwise, Γ_s is let \perp because the opening color context has already been put when we left from the column-page. Then if $\ true$ to mean a spanning text is to start, we save $\kappa_c(\beta)$ into \pcol@prespan adding the coloring \specials to restore color context from Γ^c by \pcol@restorecolorstack¹⁷⁸. We also shrink $\kappa_c(\beta^r) = \colroom$ by the height of the pre-spanning-text stuff so that spanning text will be captured by \pcol@makecol if it is broken into two (or more) pages, and put a invisible \hrule to the main vertical list letting topskip = 0 to suppress topskip insertion prior to the spanning text but instead to make the text led by \baselineskip (or \lineskip) according to the \prevdepth being the depth of the tallest column and the height of the first **\hbox** in the spanning text. Otherwise, i.e., if ifpcol@sptextstart = false, we simply put back $\kappa_c(\beta)$ into the main vertical list and then the coloring \specials by \pcol@restorecolorstack.

Note that \ifpcol@sptextstart is temporarily made false by this macro if the \pcol@ output@switch invoking \pcol@restartcolumn did not make synchronized column-switching, i.e., if $\iften constraints = true$ to mean the page is flushed before the synchronization, or $\figure{lines} for column-scanning prior to the synchronization.$

```
1107 \def\pcol@putbackmvl{%
1108
      \ifpcol@flush \pcol@sptextstartfalse \fi
1109
      \ifpcol@sync\else \pcol@sptextstartfalse \fi
      \pcol@ifempty\@currbox
1110
       {\pcol@savecolorstack
1111
        \ifpcol@sptextstart \global\setbox\pcol@prespan\box\voidb@x \fi}%
1112
       {\global\setbox\pcol@colorstack@saved\box\voidb@x
1113
        \ifpcol@sptextstart
1114
1115
          \global\setbox\pcol@prespan\vbox{%
1116
            \unvbox\@currbox \pcol@restorecolorstack}%
1117
          \global\advance\@colroom-\ht\pcol@prespan
1118
          \global\topskip\z@ \hrule\@height\z@\@width\z@
1119
        \else
1120
          \unvbox\@currbox \pcol@restorecolorstack
1121
        fi}
1122
```

11.4**Color Management**

 $\colored colored col$ \pcol@ifempty unvbox and \pcol@measurecolumn to examine if $\langle box \rangle$ is empty, and to perform $\langle then \rangle$ if so or $\langle else \rangle$ otherwise. Since T_FX does not provide any convenient way for the examination unfortunately, we perform a series of tricky operations to put the followings into \@tempboxa; a penalty of \pcol@magicpenalty = 12345 whose existence in the $\langle box \rangle$ is (almost) impossible; contents of $\langle box \rangle$ put by $\langle unvcopy \rangle$; and then a $\langle global \rangle \langle definition of \langle glempa to let it have$ the decimal representation of *lastpenalty*. Since *lastpenalty* has $\langle pen \rangle$ if the last item is $\left| \operatorname{penalty} \langle pen \rangle \right|$, or 0 otherwise, $\left| \operatorname{cgtempa} = \left| \operatorname{pcol} \operatorname{magicpenalty} \right|$ is empty.

> 1123 %% Special Output Routines: Color Management 1124

 $^{^{178}}$ If \pcol@prespan is connected to (the first part of) the spanning text, the reestablishment of the color stack here correctly places coloring \specials in .dvi. On the other hand, if the spanning text is stowed away to the next page as a whole, the reestablishment here is essential for the correct paring of the pushes and pops, the latter of which are at the bottom of the column-page whose tail is \pcol@prespan.

```
1125 \def\pcol@magicpenalty{12345}
1126 \def\pcol@ifempty#1#2#3{%
      \setbox\@tempboxa\vbox{\penalty\pcol@magicpenalty
1127
        \unvcopy#1\xdef\@gtempa{\number\lastpenalty}}%
1128
1129
      \ifnum\@gtempa=\pcol@magicpenalty\relax \def\reserved@a{#2}%
                                                 \def\reserved@a{#3}%
1130
      \else
1131
      \fi
      \reserved@a}
1132
1133
```

 $\collectercst@unvbox$ The macro $\collectercst@unvbox(box)$, invoked from $\collectercst@unvbox]$ and $\collectercst@unvbox]$ $\colored colored col$ column-page from which we are now leaving, if $\pcol@ifempty$ judges that (box) is not empty. Above the $\langle box \rangle$, we put coloring **\specials** to establish the color stack of .dvi saved in $\Gamma_s = \$ bcol@colorstack@saved by \pcol@restorecst as the opening color context of the column-page. The stack Γ_s , however, can be \perp if $\langle box \rangle$ already has the **\specials**, i.e., when we visit the column-page it had already had some items. Below (box), on the other hand, we put uncoloring \specials by \pcol@clearcolorstack to rewind Γ_r^c to clear the color context of the column-page in .dvi temporarily so that afterward it is made consistent with that in .tex.

> The macro \pcol@clearcolorstack, solely invoked from \pcol@clearcst@unvbox shown above¹⁷⁹, scans $\Gamma_r^c = (\gamma_0^c, \Gamma_r)$ by \pcol@scancst giving $\Gamma_r = \text{\pcol@colorins}$ to it as its argument. Since we gives Γ_r to the macro, this scan includes removals of all γ_i^- and $\gamma_{i,m}^-$, all γ_i having matching γ_i^- , all $\gamma_{i,m}$ having matching $\gamma_{i,m}^-$, and all elements to update γ_0^c , from Γ_r to let \pcol@colorins have Γ . Prior to this invocation, we \define \reserved@a $\langle \gamma_i \rangle$ and $\reserved@b\langle \gamma_0^c \rangle$ to let them have $\reset@color$ so that uncoloring \special will be put into the main vertical list for each $\gamma_i \in \Gamma$ and γ_0^c before update if any, regardless of coloring \special they have. That is, we invoke \reset@color as many times as the appearance of $\gamma_i \in \Gamma$ and once if $\gamma_0^c \neq \bot$ before the invocation, ignoring the color information in each element and the order of elements, expecting \reset@color just pops printer's color stack to rewind it as we intend.

> Note that in some printer .definition could \define \reset@color to let printer's text color be \current@color to make the stack rewinding resulting in the sequence of coloring operations with \current@color at the invocation of \output. This meaningless operations might cause a problem when a colored column-page of c_1 is physically followed by another column-page of the succeeding column c_2 without any coloring, because the column-page of c_2 will be colored with $\current@color</code> at the page break in <math>c_1$. If this problem is serious, we could initialize γ_0^c with \current@color at \begin{paracol} for all c such that $\hat{\gamma}_0^c$ is undefined, in order to make sure that any column-page has at least one coloring **\special** with γ_0^c at its beginning so that, for example, coloring operations at the tail of the column-page of c_1 is overridden by that of the default color of c_2 placed at the head of its column-page.

```
1134 \def\pcol@clearcst@unvbox#1{%
      \pcol@ifempty#1\relax
1135
       {\pcol@restorecst\pcol@colorstack@saved \unvbox#1\pcol@clearcolorstack}}
1136
1137 \def\pcol@clearcolorstack{%
      \def\reserved@a##1{\reset@color}\def\reserved@b##1{\reset@color}%
1138
      \pcol@scancst\pcol@colorins}
1139
1140
```

¹⁷⁹But we have this macro to avoid the complication in \defining \reserved@a and \reserved@b with an argument if we did it in the argument of \pcol@ifempty in \pcol@clearcst@unvbox.

1141 \def\pcol@restorecolorstack{\pcol@restorecst\pcol@colorins}
1142 \def\pcol@restorecst{%
1143 \def\reserved@a##1{\unvbox##1}\def\reserved@b##1{\unvcopy##1}%
1144 \pcol@scancst}
1145

 \colorscancst The macro $\colorscancst(box)$ is invoked from \colorscancstcancst and \colorscancst \pcol@iscancst restorecst. In the former invocation, we have $\langle box \rangle = \Gamma_r = \text{pcol@colorins}$ to rewind $\Gamma_r = (\gamma_0^c, \Gamma_r)$ with \reserved@a $\langle \gamma_i \rangle$ and \reserved@b $\langle \gamma_0^c \rangle$ having \reset@color. In the latter one, we have $\langle box \rangle \in \{ \Gamma = \col@colorins, \Gamma_s = \col@colorstack@saved \}$ to reestablish $\Gamma^c = (\gamma_0^c, \Gamma) \text{ or } \Gamma_s \text{ with } \text{reserved@a} \langle \gamma_i \rangle \text{ to apply } \text{unvbox to } \gamma_i \text{ and } \text{reserved@b} \langle \gamma_0^c \rangle \text{ to apply}$ \unvcopy to γ_0^c . Therefore, if $\langle box \rangle = \col@colorins$, we at first put (un)coloring \special for γ_0^c , unless it is \perp , to the main vertical list applying **\reserved@b** to it. This means the **\special** for γ_0^c is put first prior to those for elements in Γ_r or Γ consistently in reestablishing but not in rewinding. However as we discussed in the description of \pcol@clearcolorstack, the order of rewinding does not affect the result for almost all printers because only the number of pop operations is significant for them¹⁸⁰. Then if $(box) \neq \bot$ we invoke \pcol@iscancst to examine the contents of (box) from its bottom to top. Prior to the invocation, we do the following; let $\det pboxa$ have an empty $\forall box$ as its initial value of reformed $\langle box \rangle$; let pcol@tempboxa have an empty \vbox as its initial value of the sequence of \specials to be put into the main vertical list; let $n_{\text{pop}} = \texttt{Qtempcntb} = 0$; let M = reservedQb = () as its initial value of the list of identifiers of math-mode pops; if@tempswa = true to mean the first vboxto update γ_0^c found in the scan (i.e., the bottommost one) is effective.

In the macro \colorscancest , we repeatedly examine the last \colorscancest in (box) taken by $\lastbox into \gamma = \colorscancest$ until γ becomes \perp , and perform one of the following for γ .

- (1) If $height(\gamma) = 0$ and $width(\gamma) = 0$ to mean $\gamma = \gamma_i^-$, increment n_{pop} .
- (2) If $height(\gamma) = 0$ and $width(\gamma) = m > 0$ to mean $\gamma = \gamma_{i,m}^{-}$, let M = (m, M).
- (3) If $height(\gamma) \neq 0$, $depth(\gamma) = 0$ and $width(\gamma) = 0$ to mean $\gamma = \gamma_i$, decrement n_{pop} if $n_{pop} > 0$, or otherwise add γ to the head of \Ctempboxa and apply \reserved@a $\langle \gamma \rangle$ to add its result to the head of \pcol@tempboxa.
- (4) If height(γ) ≠ 0, depth(γ) = 0 and width(γ) = m > 0 to mean γ = γ_{i,m}, do nothing if m ∈ M, or otherwise add γ to the head of \@tempboxa and apply \reserved@a⟨γ⟩ to add its result to the head of \pcol@tempboxa.
- (5) If $height(\gamma) \neq 0$, $depth(\gamma) \neq 0$ to mean γ has a \special with which γ_0^c is updated. If \if@tempswa = true to mean γ is the first (bottommost) occurrence, γ_0^c is updated acquiring an \insert from \@freelist if it was \bot . In this case of \bot , we have to put an uncoloring \special by \reset@color, because \pcol@scancst did not do it but

 $^{^{180}}$ And even for the minority because multiple updates of printer's color with one particular color are independent of the order of them.

\columncolor or \normalcolumncolor pushed the corresponding color \special. Then we let if@tempswa = false.

Otherwise, i.e., if if@tempswa = false for second or succeeding occurrences, we do nothing because updates by them are overridden by the first one.

Note that the cases other than (3) and (4) happen only in rewinding, and thus in reestablishing we only have (3) and (4) with $n_{\text{pop}} = 0$ and M = () always so that every γ is kept into new $\langle box \rangle$ and a coloring \special for it will be put into the main vertical list.

Then we go back to $\collectric} to let (box) = \collectric} to the main vertical list.$

```
1146 \def\pcol@scancst#1{%
      \@tempcnta#1\relax
1147
      \ifnum\@tempcnta=\pcol@colorins
1148
        \ifvoid\pcol@ccuse{@box}\else
1149
          \reserved@b{\pcol@ccuse{@box}}\fi
1150
1151
      \fi
      \ifvoid\@tempcnta\else
1152
        \setbox\@tempboxa\vbox{}\setbox\pcol@tempboxa\vbox{}\@tempcntb\z@
1153
        \def\reserved@b{}\let\@elt\relax \@tempswatrue \pcol@iscancst
1154
1155
        \global\setbox\@tempcnta\box\@tempboxa \unvbox\pcol@tempboxa
1156
      fi
1157 \def\pcol@iscancst{%
      \setbox\@tempcnta\vbox{%
1158
        \unvbox\@tempcnta \global\setbox\pcol@tempboxb\lastbox}%
1159
      \ifvoid\pcol@tempboxb \let\reserved@c\relax
1160
1161
      \else
        \let\reserved@c\pcol@iscancst
1162
        \ifdim\ht\pcol@tempboxb=\z@
1163
          \ifdim\wd\pcol@tempboxb=\z@ \advance\@tempcntb\@ne
1164
1165
          \else \edef\reserved@b{\@elt{\number\wd\pcol@tempboxb}\reserved@b}%
1166
          \fi
        \else\ifdim\dp\pcol@tempboxb=\z@
1167
          \ifdim\wd\pcol@tempboxb=\z@
1168
            \ifnum\@tempcntb>\z@ \advance\@tempcntb\m@ne
1169
            \else
1170
              \setbox\@tempboxa\vbox{\copy\pcol@tempboxb \unvbox\@tempboxa}%
1171
1172
              \setbox\pcol@tempboxa\vbox{%
                \reserved@a\pcol@tempboxb \unvbox\pcol@tempboxa}%
1173
            \fi
1174
          \else
1175
            \count@\wd\pcol@tempboxb \chardef\reserved@d\z@
1176
            \def\@elt##1{\ifnum##1=\count@ \chardef\reserved@d\@ne \fi}%
1177
            \reserved@b \let\@elt\relax
1178
            ifnum/reserved@d=z@
1179
              \setbox\@tempboxa\vbox{\copy\pcol@tempboxb \unvbox\@tempboxa}%
1180
              \setbox\pcol@tempboxa\vbox{%
1181
                \reserved@a\pcol@tempboxb \unvbox\pcol@tempboxa}%
1182
            \fi
1183
          \fi
1184
        \else\if@tempswa
1185
1186
          \ifvoid\pcol@ccuse{@box}%
            \@next\@currbox\@freelist{\global\setbox\@currbox\vbox{}}\pcol@ovf
1187
            \pcol@ccxdef{\@currbox}\reset@color
1188
```

```
1189
          \fi
           \global\setbox\pcol@ccuse{@box}\vbox{\unvbox\pcol@tempboxb}%
1190
          \@tempswafalse
1191
        \fi\fi\fi
1192
      \fi
1193
      \reserved@c}
1194
1195
```

\pcol@savecolorstack The macro \pcol@savecolorstack is used in \pcol@startcolumn, \pcol@output@start and $\color context$ in Γ^c of a current column-page c known to be or found empty into $\Gamma_s = \collecolorstack@saved$. If both of $\gamma_0^c =$ $\colored column color@box \cdot c$ and $\Gamma = \colored colorins$ are \bot , Γ_s is let be \bot . Otherwise, Γ_s is let be a \vbox having a \vbox for γ_0^c at the top if it is not \perp and then the contents of Γ if it is not \perp .

```
1196 \def\pcol@savecolorstack{%
      \ifvoid\pcol@colorins \@tempswafalse \else \@tempswatrue \fi
1197
      \ifvoid\pcol@ccuse{@box}%
1198
        \setbox\@tempboxa\box\voidb@x
1199
1200
      \else
1201
        \setbox\@tempboxa\vbox{\unvcopy\pcol@ccuse{@box}}%
1202
        \ht\@tempboxa1sp \dp\@tempboxa\z@ \wd\@tempboxa\z@
1203
        \@tempswatrue
1204
      \fi
1205
      \if@tempswa
1206
        \global\setbox\pcol@colorstack@saved\vbox{%
1207
          \ifvoid\@tempboxa\else \box\@tempboxa \fi
          \ifvoid\pcol@colorins\else \unvcopy\pcol@colorins \fi}
1208
      \else \global\setbox\pcol@colorstack@saved\box\voidb@x
1209
1210
      \fi}
1211
```

pcol@ccuse The macro pcol@ccuse(pfx) is to expand a macro $pcol@columncolor (pfx) \cdot c$ for the current \pcol@ifccdefined column c. It is used in \pcol@output@start and \pcol@scancst@shadow with $\langle pfx \rangle =$ ' to \pcol@ccxdef have $\hat{\gamma}_0^c$, and in \pcol@scancst, \pcol@iscancst, \pcol@savecolorstack, \pcol@output@ end and \pcol@icolumncolor with $\langle pfx \rangle = @box to have \gamma_0^c$.

> The macro pcol@ifccdefined(then)(else) is used in pcol@output@start and pcol@scancst@shadow to examine whether $\hat{\gamma}_0^c = \text{pcol@columncolor} \cdot c$ is defined and to do $\langle then \rangle$ if so or $\langle else \rangle$ otherwise.

> The macro $\colectdef(body)$ $\$ (body) for the current column c. It is used in \pcol@output@start, \pcol@iscancst and \pcol@icolumncolor with $\langle body \rangle = \langle @currbox when an \insert for \gamma_0^c is acquired, and in$ \pcol@output@end with $\langle body \rangle =$ \voidb@x after releasing γ_0^c to \@freelist.

1212 \def\pcol@ccuse#1{\@nameuse{pcol@columncolor#1\number\pcol@currcol}} 1213 \def\pcol@ifccdefined#1#2{% \expandafter\ifx\csname pcol@columncolor\number\pcol@currcol\endcsname\relax 1214 $#2 \in 1 \$ 12151216 \def\pcol@ccxdef#1{% 1217 \expandafter\xdef \csname pcol@columncolor@box\number\pcol@currcol\endcsname{#1}} 1218 1219

11.5 Footnote Handling

```
\colorsavefootins The macro \colorsavefootins \langle cs \rangle, invoked from \colorsavecol for page-wise footnotes and
                                                          from \pcol@output@switch for both column-wise and page-wise footnotes, saves \footins to
                                                          an \insert register obtained by \@next from \@freelist, and \defines \langle cs \rangle being \pcol@
                                                          currfoot or \pcol@footins so that it has the register as its body and the register is then
                                                          saved into \pi^{f}(p) or \kappa_{c}(\tau). We save not only \box component of \footins but also \count,
                                                          \dimen and \skip<sup>181</sup>.
                                                          1220 %% Special Output Routines: Footnote Handling
                                                          1221
                                                          1222 \def\pcol@savefootins#1{%
                                                          1223
                                                                          \@next#1\@freelist{%
                                                          1224
                                                                                 \global\setbox#1\box\footins
                                                                                 \global\count#1\count\footins
                                                          1225
                                                                                 \global\dimen#1\dimen\footins
                                                          1226
                                                                                 \global\skip#1\skip\footins}{\def#1{\voidb@x}\pcol@ovf}}
                                                          1227
                                                          1228
\col@shrinkcolbyfn The macro \col@shrinkcolbyfn\langle height\rangle\langle ins\rangle\langle skip\rangle, invoked from \col@makecol, \col@akecol, \col@
                                                          ioutputelt, \pcol@startcolumn, \pcol@restartcolumn, \pcol@flushcolumn and \pcol@
```

makeflushedpage, shrinks $\langle height \rangle \in \{ \langle @colht, \langle @tempdima \rangle temporarily so that a column or$ $the set of all columns resides in a page with page-wise footnotes in the \insert <math>\langle ins \rangle$. The shrinkage is calculated by adding the sum of the height plus depth of all footnotes, i.e., that of $\langle ins \rangle$, and the natural component of $\langle skip \langle ins \rangle$, i.e., the vertical space inserted between the columns and the footnotes. Note that the stretch and shrink components of $\langle skip \langle ins \rangle$ cannot be incorporated into the calculation but their contribution to each column-page is taken care of by the following macro $\langle pcol@unvbox@cclv if required$. Also note that the inverse of $\langle skip \langle ins \rangle$ is kept in $\langle skip \rangle$ if it is not $\langle ncl@unvbox@cclv if required$. Also note that the inverse $\langle ins \rangle \neq \bot$ when this macro is invoked from $\langle pcol@startcolumn and <math>\rangle pcol@restartcolumn$ with $\langle skip \rangle = \langle @tempdimb.$

```
1229 \def\pcol@shrinkcolbyfn#1#2#3{%
1230 \ifx#3\relax\else #3-\skip#2\relax \fi
1231 \advance#1-\ht#2\advance#1-\dp#2\advance#1-\skip#2\relax}
```

\pcol@unvbox@cclv The macro \pcol@unvbox@cclv(*ins*), invoked from \pcol@makecol and \pcol@flushcolumn when they work on a column-page with page-wise footnotes, adds the stretch and shrink components of \skip(*ins*) at the end of \box255, where (*ins*) is non-void $\pi^{f}(p)$ having page-wise footnotes. Before the addition, the macro goes back to the baseline of \box255¹⁸² to nullify the baseline progress mechanism so as to make it sure the exact amount of the vertical skip is added. Then it adds the stretch and shrink by at first adding the skip itself and then the negative amount of its natural component.

```
1232 \def\pcol@unvbox@cclv#1{%
1233 \@tempdima\dp\@cclv \unvbox\@cclv
1234 \vskip \ifdim\@tempdima>\@maxdepth -\@maxdepth \else -\@tempdima \fi
1235 \vskip\skip#1\@tempdima\skip#1\vskip-\@tempdima}
1236
```

¹⁸¹Knowing these three components are virtually constants.

 $^{^{182}}$ The comparison of the depth of **\box255** and **\Gmaxdepth** and taking the latter if it is smaller is really just-in-case.

 $^{^{183}}$ The argument $\langle macro \rangle$ has the invoker itself shown in debug messages.

In order to avoid that \footins has footnotes across three or more pages to make confusion in the order of footnotes kept inside of T_EX, we cap the total height of footnotes by h =\@colht if it has already shrunk by non-deferred footnotes in the page we are working on indicated by \@tempdimb < 0, or $h = \@colht - \skip\footins$ if the page does not have nondeferred footnotes indicated by \@tempdimb = 0. That is, we extract leading elements of Φ by \vsplit until their total height reaches h and, if some elements are obtained in \@tempboxa, \insert them through \footins. As for the remaining elements if any, we add a leading \penalty\interlinepenalty which should have been removed by \vsplit.

Note that we temporarily let $splitmaxdepth = \mbox{maxdepth}, \splittopskip = 0$ and $\split so that the depth of the split first half is <math>\mbox{maxdepth}$ at deepest, the second half does not have any skip at its top, and T_EX will not complain of (almost) inevitable underfull. Also note that the successful extraction of the leading elements is examined by checking $\topscale{topscale}$ and thus we need to $\topscale{topscale}$ in itself because \split makes the height *h* regardless of its contents.

```
1237 \def\pcol@deferredfootins#1{%
      \ifdim\@tempdimb=\z@ \@tempdimb\@colht \advance\@tempdimb-\skip\footins
1238
      \else \@tempdimb\@colht
1239
1240
      \fi
      \ifvoid\pcol@topfnotes\else \ifdim\@tempdimb>\z@
1241
        \begingroup
1242
          \splitmaxdepth\@maxdepth \splittopskip\z@ \vbadness\@M
1243
          \setbox\@tempboxa\vsplit\pcol@topfnotes to\@tempdimb
1244
1245
          \ifvoid\pcol@topfnotes\else
             \global\setbox\pcol@topfnotes\vbox{\penalty\interlinepenalty
1246
               \unvbox\pcol@topfnotes}%
1247
          \fi
1248
1249
          \setbox\@tempboxa\vbox{\unvbox\@tempboxa}%
1250
          \ifdim\ht\@tempboxa>\z@
1251
            \pcol@Log#1{add}\@tempboxa
            \insert\footins{\unvbox\@tempboxa}%
1252
1253
          \fi
        \endgroup
1254
1255
      fi fi
1256
```

 $\label{eq:local_$

The null vertical skip is put for page-wise footnotes, for which the macro \pcol@putfootins is invoked from \pcol@ioutputelt and \pcol@makeflushedpage. Since we shrink the height of column-pages by the height-plus-depth of page-wise footnotes, the natural height of the box in which column-pages and page-wise footnotes are combined would be less than \textheight

¹⁸⁴And thus having the arguments $\langle b \rangle$ and $\langle f \rangle$ is unnecessary, but we keep this implementation to avoid unnecessary recoding from a development version.

 $^{^{185}}$ We avoid null space insertion to minimize the difference from older versions in traced output.

due to the depth of the last footnote line if we simply made the footnotes the last items of the box. Though this shortage at most \maxdepth is expected to be covered by the stretch factor of \skip\footins without too large badness causing an underfull message¹⁸⁶, someday we could face an underfull with some unusual settings of \maxdimen, \skip\footins and/or \vbadness. Therefore, we put a null vertical skip so that the real bottom of the footnotes, instead of the last baseline, is placed at the baseline of the box, to make the natural height of the box is **\textheight** exactly. Note that this shifting page-wise footnotes up will not make last baselines of footnotes among pages unaligned, because the last line have a strut.

```
1257 \def\pcol@combinefootins#1#2{%
      \setbox\@outputbox\vbox{%
1258
        \boxmaxdepth\@maxdepth
1259
        \unvbox#1\relax
1260
        \pcol@putfootins#2\unskip
1261
        \ifdim\belowfootnoteskip=\z@\else \vskip\belowfootnoteskip \fi}}
1262
1263 \def\pcol@putfootins#1{%
1264
      \vskip\skip#1\relax
1265
      \color@begingroup
        \normalcolor
1266
        \footnoterule
1267
        \unvbox#1\relax
1268
1269
      \color@endgroup \vskip\z@}
1270
```

Marginal Notes 11.6

\Caddmarginpar The macro \pcolCaddmarginpar is our own version of \Caddmarginpar, which \pcolC \pcol@addmarginpar zparacol makes \let-equal to \pcol@addmarginpar keeping its original definition in \pcol@ \pcol@caddmarginpar @addmarginpar. Therefore, in an paracol environment, the \output request made by IATFX's $\mbox{marginpar}$ in the column c and page p is processed by \colladdmarginpar through our own \output routine being \pcol@output, \pcol@specialoutput and LATEX's \@specialoutput. What we do in this macro are as follows; determine the margin which a marginal note goes to; temporarily modify the parameter $m_w = \text{marginparwidth or } m_s = \text{marginparsep}$ according to the margin and the column; determine the position to place the marginal note consulting $\pi^m(p) = \text{pcol@mparbottom}$ obtained by pcol@getcurrpage: and update $\pi^m(p)$ according to the position.

> First, there are the following parameters to determine the margin, and thus the value of \if@firstcolumn referred to in LATEX's \@addmarginpar and meaning left if true or right if false.

- (1) The macros \pcol@mpthreshold@l and \pcol@mpthreshold@r defined by \marginpar threshold give us the threshold of the column number to let columns less than it go to the left margin while those equal to or greater than it to the right, according to the parallel-page the column belongs to. Therefore, we let $\iftenst column = true$ iff $c < \colombol{methreshold@l} \land c < C_L \text{ or } c < \colombol{methreshold@r} \land c \geq C_L, \text{ as the}$ fundamental setting.
- (2) If $\ ifpcol@swapmarginpar = true$ because the specifier 'm' is given to $\ twosided$ explicitly or implicitly, the decision in (1) is reversed if $page(p) \mod 2 = 0$, and then this decision is reversed again if $c \geq C_L$ and ifpcol@paired = false to mean c is in a

 $^{^{186}}$ With default settings of $\max = 5 \, \text{pt}$ and the stretch factor $4 \, \text{pt}$ of $\sinh \sqrt{160 \, \text{stip}}$ $100 \times (5/4)^3 \approx 195$ is significantly less than the default \vbadness = 1000.

non-paired right parallel-page. The second reversal is done because page(p) is common to both left and right parallel-pages and is for the left page in usual cases without page number jumps. Therefore, $(page(p) \mod 2)$ is for left parallel-pages and thus for right counterparts the decision should be made by $((page(p) + 1) \mod 2)$ and thus the result should be reversed.

(3) If \if@reversemargin is made *true* by LATEX's \reversemarginpar, the decision made by (1) and then possibly reversed by (2) is finally reversed.

Second, we calculate

$$D = \texttt{N@tempdima} = \sum_{d=C^0}^{swap(c)-1} (w_{swap(d)} + g_{swap'(d)})$$

where x' = swap(x) is given by $\pcol@swapcolumn<math>\langle x \rangle \langle x' \rangle \langle C^0 \rangle \langle C^1 \rangle$ to let $x' = C^1 - (x - C^0) - 1$ if $\ifpcol@swapcolumn = true and <math>page(p) \mod 2 = 0$ or x' = x otherwise, $swap'(x) = \pcol@colsepid \in \{swap(x) - 1, x\}$ according to swapped or not, $(C^0, C^1) \in \{(0, C_L), (C_L, C)\}$ according to $c < C_L$ or not, and w_x and g_x are the width of x-th column and gap given by $\pcol@columnwidth x$ and $\pcol@columnsep x$ respectively. That is, D is the distance from the left edge of the column c to that of leftmost column in the (parallel-) page in which c resides. Then if $\if@firstcolumn = true$ to let the marginal note go to the left margin, we add Dto $m_w = \marginparwidth$ so that λT_EX 's $\marginpar being \pcol@caddmarginpar$ aligns the left edge of the marginal note at the point apart from the column's left edge by $(D + m_w) + m_s$ rather than $m_w + m_s$, or in other words $m_w + m_s$ apart from the left edge of the leftmost column. On the other hand if $\if@firstcolumn = false$, we add $W_T - (D + w_c)$ where W_T is \textwidth , being the distance from the right edge of the column c to that of the rightmost column, to $m_s = \marginparsep$ so that $\pcol@caddmarginpar$ aligns the left edge of the marginal note at the point apart from the column c to that of the rightmost column, to $m_s = \marginparsep$ so that $\pcol@caddmarginpar$ aligns the left edge of the marginal note at the point apart from the column's right edge by $W_T - (D + w_c) + m_s$ rather than m_s , or in other words m_s apart from the rightmost column.

Third, we let $\col@marbox$ be the first element of $\courrlist obtained by <math>\courrlist$ for the right marginal note if $\if@firstcolumn = false$, or \courrbox for the left marginal note otherwise. Then we let $t = \@dempdima$ be the distance from the top edge of the column to that of the marginal note, namely $\@dempdima$ be the height of $\col@marbox$ plus $\dimen\@currbox$ being downward shift amount optionally given by \marginnote . We also let $h = \@dempdimb$ be the height-plus-depth of the box $\col@marbox$ plus \marginparpush , or in other words the vertical space the marginal note requires. Then we give t and h to $\col@getmparbottom$ to let $\marginal text in \col@marbox, and to let <math>\col@marbox$ have the new list to be replaced with $M_{\{L,R\}}^{\{l,r\}}$ in $\pi^m(p)$.

Forth, we update $\pi^m(p)$ with the new list in \pcol@mpblist by a process similar to \pcol@ setpageno but with \pcol@setmpbelt to scan the list of pages Π^+ .

Fifth, we shift down \pcol@marbox by \dimen\@currbox and, if the shift amount is greater than the height of the box and thus the height of shifting result is zero, decrement \@mparbottom by the amount to deceive LATEX's \@addmarginpar into believing \@mparbottom is above the real one by the amount. In other words, by the decrement we let \@addmarginpar see the top edge of the shifted marginal note in the box, rather than that of the box itself, for the placement with \@mparbottom.

Finally, we invoke LATEX's original \@addmarginpar being \pcol@@addmarginpar to put the marginal note according to \if@firstcolumn, temporarily modified \marginparsep and \marginparwidth, and \@mparbottom. Note that since \pcol@zparacol lets \if@twocolumn $= true, \clicklinet true, \c$

```
1271 %% Special Output Routines: Marginal Notes
1272
1273 \def\pcol@addmarginpar{%
      \pcol@getcurrpage \@firstcolumntrue
1274
      \ifnum\pcol@currcol<\pcol@ncolleft
1275
        \let\reserved@a\z@ \let\reserved@b\pcol@ncolleft
1276
        \ifnum\pcol@mpthreshold@l>\pcol@currcol\else \@firstcolumnfalse \fi
1277
1278
      \else
1279
        \let\reserved@a\pcol@ncolleft \let\reserved@b\pcol@ncol
1280
        \ifnum\pcol@mpthreshold@r>\pcol@currcol\else \@firstcolumnfalse \fi
1281
      \fi
1282
      \ifpcol@swapmarginpar
1283
        \ifodd\c@page\else
          \if@firstcolumn \@firstcolumnfalse \else \@firstcolumntrue \fi
1284
1285
        \fi
        \ifpcol@paired\else \ifnum\pcol@currcol<\pcol@ncolleft\else
1286
          \if@firstcolumn \@firstcolumnfalse \else \@firstcolumntrue \fi
1287
1288
        \fi\fi
1289
     \fi
1290
      \if@reversemargin
        \if@firstcolumn \@firstcolumnfalse \else \@firstcolumntrue \fi
1291
1292
      \fi
      \pcol@swapcolumn\pcol@currcol\count@\reserved@a\reserved@b
1293
1294
      \@tempdima\z@
1295
      \@tempcnta\reserved@a \@whilenum\@tempcnta<\count@\do{%
        \pcol@swapcolumn\@tempcnta\@tempcntb\reserved@a\reserved@b
1296
        \advance\@tempdima\csname pcol@columnwidth\number\@tempcntb\endcsname\relax
1297
        \advance\@tempdima\csname pcol@columnsep\pcol@colsepid\endcsname\relax
1298
       \advance\@tempcnta\@ne}%
1299
      \if@firstcolumn \advance\marginparwidth\@tempdima
1300
1301
      \else
        \advance\marginparsep\textwidth \advance\marginparsep-\@tempdima
1302
1303
        \advance\marginparsep-\columnwidth
1304
      \fi
      \expandafter\@xnext\@currlist\@@\pcol@marbox\@gtempa
1305
      \if@firstcolumn\let\pcol@marbox\@currbox \fi
1306
      \@tempdima\@pageht \advance\@tempdima-\ht\pcol@marbox
1307
1308
      \advance\@tempdima\dimen\@currbox
      \@tempdimb\ht\pcol@marbox \advance\@tempdimb\dp\pcol@marbox
1309
      \advance\@tempdimb\marginparpush
1310
1311
      \pcol@getmparbottom\@tempdima\@tempdimb
1312
      \begingroup
1313
        \@tempcnta\pcol@page \advance\@tempcnta-\pcol@basepage
1314
        \edef\reserved@a{\pcol@pages\pcol@currpage}%
        \global\let\pcol@pages\@empty \global\let\pcol@currpage\@empty
1315
        \let\@elt\pcol@setmpbelt \reserved@a
1316
      \endgroup
1317
      \ifdim\dimen\@currbox=\z@\else
1318
        \ifdim\dimen\@currbox>\ht\pcol@marbox
1319
1320
           \advance\@mparbottom-\dimen\pcol@marbox
```

```
\fi
1321
        \setbox\pcol@marbox\hbox{\lower\dimen\@currbox\box\pcol@marbox}%
1322
      \fi
1323
      \pcol@@addmarginpar}
1324
1325
```

\pcol@getmparbottom@i \@mparbottom point the bottom of the marginal note below which a new marginal note m, pcol@getmpbelt whose natural top is at t and occupancy height is h, in the current column c and the page p is placed, or 0 if the side margin has had no marginal notes yet. It is also \defines M' =\pcol@mpblist having mpar(t', t'+h) for the new marginal note m placed at t' in it and being replaced with one of $M_{\{L,R\}}^{\{l,r\}}$ in $\pi^m(p)$ by \pcol@setmpbelt.

First we examine if $\pi^m(p) = \text{pcol@mparbottom}$ is empty and if so we simply let B = 0and M' = (mpar(t, t+h)) because there are no marginal notes in the page p at all. Otherwise we obtain $M \in \{M_X^x \mid X \in \{L, R\}, x \in \{l, r\}\}$ in \reserved@a according to the side margin to which the new marginal note m goes to, i.e., according to \if@firstcolumn and $c < C_L$ or not, by $\collegetmparbottom@i giving it the body of <math>\pi^m(p)$ by $\collegetmparbottom@i giving it the body of \pi^m(p)$ by by $\collegetmparbottom@i giving it the body of \pi^m($ \pcol@getmpbelt to each $mpar(t_i, b_i) \in M$ to have $t_k = \min\{t_i \mid t_i \ge t, t_i - \max(t, b_{i-1}) \ge h\}$ and let $B = b_{k-1}$ and

$$M' = (mpar(t_1, b_1), \dots, mpar(t_{k-1}, b_{k-1}), mpar(max(t, B), max(t, B) + h))$$
$$mpar(t_k, b_k), \dots, mpar(t_n, b_n))$$

where n = |M|, assuming $b_0 = 0$. That is, we try to find the first available gap between marginal notes below t to accommodate the marginal note m of h tall. Then if such t_k is not found because $t > t_n$ to mean m appears below the last marginal note as in natural cases, or $t_i - \max(t, b_{i-1}) < h$ for all t_i s.t. $t_i > t$ to mean there are no available gaps, we let $B = t_n$ and M' = (M, mpar(max(t, B), max(t, B) + h)) to place m at the bottom.

```
1326 \def\pcol@getmparbottom#1#2{%
1327
      \global\@mparbottom\z@
1328
      \ifx\pcol@mparbottom\@empty
1329
        \begingroup
          \@tempdimc#2\relax \advance\@tempdimc#1\relax \let\@elt\relax
1330
          \xdef\pcol@mpblist{\@elt{\number#1}{\number\@tempdimc}}%
1331
1332
        \endgroup
1333
      \else
        \expandafter\pcol@getmparbottom@i\pcol@mparbottom
1334
1335
        \begingroup
          \@tempdima#1\relax \@tempdimb#2\relax \@tempswafalse
1336
          \let\@elt\pcol@getmpbelt \global\let\pcol@mpblist\@empty \reserved@a
1337
          \if@tempswa\else
1338
            \ifdim\@tempdima<\@mparbottom \@tempdima\@mparbottom \fi
1339
            \advance\@tempdimb\@tempdima
1340
            \@cons\pcol@mpblist{{\number\@tempdima}{\number\@tempdimb}}%
1341
          \fi
1342
        \endgroup
1343
1344
      \fi}
1345 \def\pcol@getmparbottom@i#1#2#3#4{%
      \ifnum\pcol@currcol<\pcol@ncolleft
1346
        \if@firstcolumn \def\reserved@a{#1}\else\def\reserved@a{#2}\fi
1347
```

 $^{^{187}\}mathrm{Thus}$ giving t and h as arguments is not necessary but we dare to do it.

```
\else
                                                              1348
                                                                                    \if@firstcolumn \def\reserved@a{#3}\else\def\reserved@a{#4}\fi
                                                              1349
                                                                               \fi}
                                                              1350
                                                              1351 \def\pcol@getmpbelt#1#2{%
                                                                               \ifdim#1sp<\@tempdima
                                                              1352
                                                                                     \global\@mparbottom#2sp\relax \@cons\pcol@mpblist{{#1}{#2}}%
                                                              1353
                                                                                    \ifdim\@tempdima<#2sp\relax \@tempdima#2sp\relax \fi
                                                              1354
                                                              1355
                                                                               \else
                                                                                    \@tempdimc\@tempdima \advance\@tempdimc\@tempdimb
                                                              1356
                                                              1357
                                                                                     \ifdim#1sp<\@tempdimc
                                                                                          \@tempdima#2sp\relax \global\@mparbottom#2sp\relax
                                                              1358
                                                                                          \cons\pcol@mpblist{{#1}{#2}}%
                                                              1359
                                                                                     \else
                                                              1360
                                                                                           \@cons\pcol@mpblist{{\number\@tempdima}{\number\@tempdimc}\@elt{#1}{#2}}%
                                                              1361
                                                              1362
                                                                                           \@tempswatrue
                                                                                          \def\pcol@getmpbelt##1##2{\@cons\pcol@mpblist{{##1}{##2}}}
                                                              1363
                                                              1364
                                                                                    \fi
                                                                               \fi}
                                                              1365
                                                              1366
                 \pcol@setmpbelt The macro \pcol@setmpbelt{\pi^p(q)}\langle \pi^i(q) \rangle \langle \pi^f(q) \rangle \{\pi^s(q)\} \{\pi^m(q)\} is used solely in \pcol@
           \pcol@setmpbelt@i addmarginpar and is applied to \Pi^+ to update an element M \in \{M_X^x \mid X \in \{L, R\}, x \in l, r\} in
                                                              \pi^m(p) with M' =  pcol@mpblist given by \pcol@getmparbottom. The structure of the macro
                                                              is similar to \pcol@setpnoelt to update \pi^p(q) s.t. q \ge p, but in this macro the target of the
                                                              update is only p. Then for q = p, we invoke \pcol@setmpbelt@i giving it the body of \pi^m(p)
                                                              being \{M_L^l\}\{M_L^r\}\{M_R^r\}, or \langle\emptyset\rangle\langle\emptyset\rangle\langle\emptyset\rangle\langle\emptyset\rangle if \pi^m(p) = \emptyset, to obtain what \pi^m(p) should have
                                                              in \pi_{new}^m(p) = \text{reserved}@a in which M_X^x is replaced with M', where X = L or X = R if c < C_L
                                                              or not respectively, and x = l or x = r if \if@firstcolumn = true or not respectively, and
                                                              then update \pi^m(p) by \col@defcurrpage{\pi^p(p)}\langle \pi^i(p)\rangle\langle \pi^f(p)\rangle{\pi^s(p)}\langle \pi^{m}(p)\rangle{\pi^m(q)}.
                                                              1367 \def\pcol@setmpbelt#1#2#3#4#5{%
                                                                               {\let\@elt\relax \xdef\pcol@pages{\pcol@currpage}}%
                                                              1368
                                                              1369
                                                                               \ifnum\@tempcnta=\z@
                                                              1370
                                                                                    \def\reserved@a{#5}%
                                                                                    \ifx\reserved@a\@empty \pcol@setmpbelt@i{}{}\else \pcol@setmpbelt@i#5\fi
                                                              1371
                                                                                    \col@defcurrpage{#1}{#2}{#3}{#4}{\reserved@a}%
                                                              1372
                                                                               \else \gdef\pcol@currpage{\@elt{#1}#2#3{#4}{#5}}%
                                                              1373
                                                                               \fi
                                                              1374
                                                                               \advance\@tempcnta\m@ne}
                                                              1375
                                                              1376 \def\pcol@setmpbelt@i#1#2#3#4{%
                                                                               \ifnum\pcol@currcol<\pcol@ncolleft
                                                              1377
                                                                                     \if@firstcolumn \def\reserved@a{{\pcol@mpblist}{#2}{#3}{#4}}%
                                                              1378
                                                                                     \else
                                                                                                                                  \def\reserved@a{{#1}{\pcol@mpblist}{#3}{#4}}%
                                                              1379
                                                              1380
                                                                                    \fi
                                                              1381
                                                                               \else
                                                                                    \if@firstcolumn \def\reserved@a{{#1}{#2}{\pcol@mpblist}{#4}}%
                                                              1382
                                                                                    \else
                                                                                                                                  \label{eq:lasses} \label{eq:lasses} \\ \label{eq:lasses} \label{e
                                                              1383
                                                                                    \fi
                                                              1384
                                                              1385
                                                                               \fi}
                                                              1386
\verb|pcol@mparbottom@zero is used in \verb|@outputpage, \verb|pcol@getmparbottom@zero is used in \verb|@outputpage, \verb|pcol@getmparbottom@]|}
   \colomba problem default value of M = \colomba problem default value
```

```
198
```

mpar(0,0) for all elements $M \in \{M_X^x \mid X \in \{L,R\}, x = \{l,r\}\}$ to mean a page has no marginal

notes carrying over from the preceding paracol environments.

As for \mathcal{M} , besides the top level initialization to make it \mathcal{M}_0 , it is updated in \pcol@ output@end through macros \pcol@getmparbottom@last and \pcol@bias@mpbout to have the last element of each $M \in \{M_X^x \mid X \in \{L, R\}, x = \{l, r\}\}$ in $\pi^m(p_t)$ with transformation from coordinates of columns to that of text area, or directly with \mathcal{M}_0 if the last page will not have post-environment stuff. The resulting \mathcal{M} is at first used in \pcol@output@end itself through \pcol@do@mpbout to let \@mparbottom have the value b of mpar(t,b) in M_L^l or M_L^r according to the side margin which marginal notes in post-environment stuff goes to.

Then \mathcal{M} is passed to the next **paracol** environment if it resides in the page where the previous environment also resides, to be referred to by \pcol@output@start which also performs \pcol@do@mpbout and \pcol@bias@mpbout to let $\pi^m(0)$ have the lists according to \mathcal{M} and \Comparbottom which can be modified in post-environment stuff of the previous environment or in other word in pre-environment stuff of starting environment. By this setting of $\pi^m(0)$, marginal note placement in the starting page is aware of the marginal notes having been placed in previous environments and in pre-environment stuff and thus can correctly examines if a marginal note to be added in a margin collide the last one in the margin. On the other hand, if the post-environment stuff encounters a page break before a new environment starts, our own \Coutputpage should be invoked at the page break to let $\mathcal{M} = \mathcal{M}_0$ because the marginal notes in previous environments do not affect those in the new environment.

Note that \mathcal{M} is also referred to and updated by $\col@do@mpb@all@i and \col@do@$ mpb@all@ii because they are used in \pcol@bias@mpbout and \pcol@getmparbottom@last through \pcol@do@mpb@all.

```
1388 \global\let\pcol@mparbottom@out\pcol@mparbottom@zero
1389
```

\pcol@do@mpbout The macro \pcol@do@mpbout is used in \pcol@output@start and \pcol@output@end to \pcol@do@mpbout@i perform operations specified by \pcol@do@mpbout@whole and \pcol@do@mpbout@elem. The $\collectoremetabout@whole macro just invokes \collectoremetabout@i giving it all <math>M \in \{M_X^x \mid X \in \{L, R\}, x \in \{l, r\}\}$ by \pcol@do@mpbout@elem \expandafter.

> Then \pcol@do@mpbout@i determines the side margin $x \in \{l, r\}$ letting x = l iff $if@mparswitch = true, page(p) \mod 2 = 0$ and if@reversemargin = false, to invoke $\verb|pcol@do@mpbout@whole giving it all M but M^x_L whose sole element mpar(t, b) may be modified$ by $\col@do@mpbout@elem\@elt{t}{b}.$

> In \pcol@output@start, \pcol@do@mpbout@whole is to \xdefine \mathcal{M} with all M and \pcol@ do@mpbout@elem is expanded to mpar(0, B), where $B = \mbox{Qmparbottom}$, regardless of M_L^x so that it is replaced with (mpar(0, B)) in the modified \mathcal{M} keeping other elements unchanged. In \collecture{dend} , \col $\col@do@mpbout@elem lets B = b$ so that the bottom of the last marginal note in the side margin specified by x is passed to post-environment stuff through \@mparbottom.

1390 \def\pcol@do@mpbout{\expandafter\pcol@do@mpbout@i\pcol@mparbottom@out}

```
\def\pcol@do@mpbout@i#1#2#3#4{\@tempcnta\@ne
1391
```

```
\if@mparswitch \ifodd\c@page\else \@tempcnta\m@ne \fi\fi
1392
```

```
1393
      \if@reversemargin \@tempcnta-\@tempcnta \fi
```

```
\ifnum\@tempcnta<\z@
1394
```

```
\pcol@do@mpbout@whole{\pcol@do@mpbout@elem#1}{#2}{#3}{#4}%
1395
```

```
1396
       \else
```

```
\pcol@do@mpbout@whole{#1}{\pcol@do@mpbout@elem#2}{#3}{#4}%
1397
```

```
\fi}
1398
```

1399

$\colorige{tasgmpbout}$ The macro $\colorige{tasgmpbout}{y}$ is used in $\colorige{tasgmpbout}$ with -y being the heigh- $\colored bias@mpbout@i plus-depth of pre-environment stuff, in \pcol@output@end with y being that of spanning$

stuff in the last page, and in $\collectment particulat{y}$ with its argument y. The macro modifies mpar(t, b) in all $M \in \{M_X^x \mid X \in \{L, R\}, x \in \{l, r\}\}$ of \mathcal{M} so that they have mpar(t+y, b+y) for the transformation from text area coordinates to columns in the first and third, while for the reverse transformation in the second, by invoking \pcol@do@ mpbCall giving it \mathcal{M} and letting \reservedCa have \pcolCbiasCmpboutCi{y}. That is, $\clickline product (y) \clickline (y) \clickline$ t and b from mpar(t, b) in each M, and then it \defines \reserved@b with mpar(t+y, b+y) so that updated M has it.

1400 \def\pcol@bias@mpbout#1{\def\reserved@a{\pcol@bias@mpbout@i{#1}}% 1401 \pcol@do@mpb@all\pcol@mparbottom@out} 1402 \def\pcol@bias@mpbout@i#1\@elt#2#3\@nil{% 1403 \dimen@#2sp\relax \advance\dimen@#1\relax 1404 \dimen@ii#3sp\relax \advance\dimen@ii#1\relax 1405 \def\reserved@b{\@elt{\number\dimen@}{\number\dimen@ii}}} 1406

 $\coll{getmparbottom@last}$ The macro $\coll{getmparbottom@last}_y$ is used solely in $\coll{getmparbottom@last}$ to let $\mathcal{M}=$ mpar(y, y), and y is the negative counterpart of the height-plus-depth of the spanning stuff in the last page. Therefore, \mathcal{M} is let have the occupancy information of the last marginal note if any, or the top edge of text area otherwise, in each margin.

The macro at first examines if $\pi^m(p_t) = \emptyset$ and, if so, lets all elements in \mathcal{M} have (mpar(y, y)) by letting it \mathcal{M}_0 and then adding y to each t = b = 0 by \pcol@bias@ mpbout giving it y. Otherwise, i.e., if $\pi^m(p_t) \neq \emptyset$, it invokes \pcol@do@mpb@all giving it $\pi^m(p_t)$ and letting \reserved@a have \pcol@getmparbottom@last@i{y}. That is, $\cold{getmparbottom@last@i{y}mpar(t_1, b_1) \cdots mpar(t_n, b_n)\cold{getmparbottom@last@i{y}mpar(t_1, b_1) \cdots mpar(t_n, b_n)\cold{getmparbottom@last@i{y}mparbottom@last$ do@mpb@all@ii for each M_X^x to let \reserved@b have mpar(y, y) at first and then to let it have $mpar(t_i, b_i)$ for all $i \in [1, n]$. Therefore, **\reserved@b** should finally have $mpar(t_n, b_n)$ assuming $t_0 = b_0 = y$, and then becomes m_X^x .

```
1407 \def\pcol@getmparbottom@last#1{%
      \ifx\pcol@mparbottom\@empty
1408
1409
        \global\let\pcol@mparbottom@out\pcol@mparbottom@zero
1410
        \pcol@bias@mpbout{#1}%
1411
      \else
        \def\reserved@a{\pcol@getmparbottom@last@i{#1}}%
1412
        \pcol@do@mpb@all\pcol@mparbottom
1413
1414
      \fi}
1415 \def\pcol@getmparbottom@last@i#1#2\@nil{%
      \edef\reserved@b{\@elt{\number#1}{\number#1}}%
1416
      \def\@elt##1##2{\def\reserved@b{\@elt{##1}{##2}}}%
1417
      #2\let\@elt\relax}
1418
1419
```

```
\coll{eq:local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_l
    \pcol@do@mpb@all@i \pcol@getmparbottom@last with L = \pi^m(p_t), to process all four elements M_X^x in L ap-
\colored compbealles in plying \colored constrained to each of them and to let <math>\mathcal{M} have the result through \reserved@b.
                                                                                         The macro simply invokes \col@do@mpb@all@i giving it the body of L by \expandafter.
                                                                                        Then \col@do@mpb@all@i{M_L^{l}}{M_R^{r}} M_R^{r} initialize \mathcal{M} = \emptyset and then invokes \col@
                                                                                         do@mpb@all@ii four times giving it each M_X^x. Then \pcol@do@mpb@all@ii mpar(t_1, b_1) \cdots
```

 $mpar(t_n, b_n)$ \Quil invokes \reservedQa giving it all of $mpar(t_i, b_1)$ at once to process them and to have the result in \reservedQb being added to \mathcal{M} .

```
1421 \def\pcol@do@mpb@all@i#1#2#3#4{\begingroup \let\@elt\relax
     \gdef\pcol@mparbottom@out{}%
1422
     \pcol@do@mpb@all@ii#1\@nil\pcol@do@mpb@all@ii#2\@nil
1423
     \pcol@do@mpb@all@ii#3\@nil\pcol@do@mpb@all@ii#4\@nil
1424
1425
     \endgroup}
1426 \def\pcol@do@mpb@all@ii#1\@nil{%
1427
     \reserved@a#1\@nil
1428
     \xdef\pcol@mparbottom@out{\pcol@mparbottom@out{\reserved@b}}}
1429
```

11.7 Synchronization

\pcol@sync The macro \pcol@sync is invoked solely from \pcol@output@switch for explicit synchronization in the following three cases in which \ifpcol@sync \vee \ifpcol@clear = true commonly.

- $\ \$ or $\$ or or \ or $\$ or or \ or $\$ or or \ or $\$ or or \ or $\$ or $\$ or or \ or or \ or or \ or or \ or $\$ or or \ or \ or or \ or \ or \ or or \ o
- \ifpcol@sync ^ \ifpcol@clear to mean pre-flushing column height check.
- $\neg \perp fpcol@sync \land \perp fpcol@clear$ to mean page flushing.

In any cases¹⁸⁸, first we invoke \pcol@flushcolumn for all $c \in [0, C)$ to flush the current column-page of c into S_c if the column-page is not in p_t , i.e., $\kappa_c(\beta^p) < p_t$ and then, if we have deferred floats, to ship out following float pages up to $p_t - 1$ into S_c and to place them in p_t . This float placement in p_t is only for top and bottom floats in synchronized column-switching, while a float column may be made in other cases. Then we ship out all pages p such that $p < p_t$ by \pcol@outputcolumns giving argument 1. After that, we obtain the page context of p_t by \pcol@getcurrpinfo.

Next, we measure the vertical sizes of the contents in the current column-page of c which is now in p_t for all $c \in [0, C)$ by \pcol@measurecolumn as follows, where h(x) and d(x) are the height and depth of an object x respectively.

$$\begin{split} \sigma = & \texttt{floatsep} \qquad \sigma_t = \begin{cases} \kappa_c(\xi) & \kappa_c(\xi) < \infty \\ \texttt{textfloatsep} & \kappa_c(\xi) = \infty \end{cases} \quad \sigma_b = \texttt{textfloatsep} \\ f_c(t) &= (\kappa_c(\lambda_t) \neq ()) & f_c(m) = (\kappa_c(\beta) \neq \texttt{vbox}\{\}) \\ f_c(f) &= (\kappa_c(\tau) \neq \bot) & f_c(b) = f_c(b') = (\kappa_c(\lambda_b) \neq ()) \end{cases} \\ F_c(X) &= \exists x \in X : f_c(x) & f_b = \texttt{tipcol@bfbottom} \\ v_c(t) &= \texttt{tskip} \cdot \kappa_c(\beta) = \sum_{\phi \in \kappa_c(\lambda_t)} (h(\phi) + d(\phi)) + (|\kappa_c(\lambda_t)| - 1) \cdot \sigma + \sigma_t \\ v_c(m) &= h(\kappa_c(\sigma)) + d(\kappa_c(\beta)) \\ v_c(f) &= h(\kappa_c(\tau)) + d(\kappa_c(\tau)) \\ v_c(b) &= \sum_{\phi \in \kappa_c(\lambda_b)} (h(\phi) + d(\phi)) + (|\kappa_c(\lambda_b)| - 1) \cdot \sigma + \sigma_b \\ \phi \in \kappa_c(\lambda_b) \\ v_c(b') &= v_c(b) + \sigma_b \end{split}$$

¹⁸⁸In the last case of page flushing, invoking \pcol@flushcolumn is redundant because it is made $p = p_t$ by pre-flushing column height check always preceding the flushing, but the invocation is harmless.

$$\begin{split} \delta_c &= \begin{cases} \kappa_c(\delta) & f_c(m) \\ \infty & \neg f_c(m) \end{cases} \\ size_c(x) &= \begin{cases} v_c(x) & f_c(x) \\ 0 & \neg f_c(x) \end{cases} \\ SIZE_c(X) &= \begin{cases} \sum_{x \in X} size_c(x) & F_c(X) \\ -\infty & \neg F_c(X) \end{cases} \\ V_T &= \verb| @tempdima = \max_{0 \leq c < C} \{SIZE_c(\{t, m\})\} \end{cases} \\ V_B &= \verb| @tempdimb = \max_{0 \leq c < C} \{size_c(f) + size_c(b)\} \end{cases} \\ V_P &= \verb| @qageht = \max_{0 \leq c < C} \{SIZE_c(\{t, m, f, b\})\} \end{cases} \\ V'_P &= \verb| @pageht = \max_{0 \leq c < C} \{SIZE_c(\{t, m, f, b\})\} \end{cases} \\ D_T &= \verb| @tempdimc = \min\{\delta_c \mid SIZE_c\{t, m\} = V_T\} \\ d_c &= \begin{cases} 0 & f_c(b) \land (\neg f_c(f) \lor f_b) \\ d(\kappa_c(\delta)) & \neg f_c(b) \land \neg f_c(f) \end{cases} \\ D_P &= \verb| @qagedp = \min\{d_c \mid SIZE_c(\{t, m, f, b'\}) = V'_P\} \end{cases} \\ c_{\max} &= \verb| @tempcntb = \arg\max_{0 \leq c < C} \{SIZE_c(\{t, m, f, b'\}) = V'_P\} \end{cases} \end{split}$$

That is, V_T is the maximum of combined vertical size (height plus depth) of the top floats and the main vertical list, V_B is that of the footnotes and bottom floats, and V_P is that of all items. V'_P is similar to V_P but we add \textfloatsep to the size of bottom floats. Note that V_T , V_P and V'_P are $-\infty$ if any column-pages don't have corresponding items, while $V_B = 0$ if so. Also note that c_{\max} is the ordinal of the column whose size is V_P .

 D_T and D_P are the minimum δ_c and d_c respectively among those gives V_T and V'_P respectively, where δ_c is $\kappa_c(\delta)$ if $f_m = true$ or ∞ otherwise, and d_c is 0 if c has bottom float, or the depth of the last footnote if any and without any bottom float, or $\kappa_c(\delta)$ otherwise. The reason why D_T and D_P have minimums is that they are set into **\prevdepth** for the items just following the synchronization point, and thus a smaller value results in a larger interline skip and the special value $-1000 \, \text{pt}$ to inhibit the skip by, e.g., **\nointerlineskip**, is given the highest priority.

Note that V'_P and D_P are only for the last page and thus referred to by \pcol@output@end to close the environment, and the former is done by \pcol@makeflushedpage if it works on the page. The reason why we add \textfloatsep to V'_P is to make the last page well separated from the post-environment stuff if the tallest column, taking the addition into account, has bottom floats. Also note that we let \ifpcol@dfloats = false before scanning columns with \pcol@measurecolumn so that the switch becomes true after the scan iff a column has deferred floats (in the last page).

1430 %% Special Output Routines: Synchronization
1431
1432 \def\pcol@sync{%
1433 \pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do\pcol@flushcolumn
1434 \pcol@outputcolumns\@ne
1435 \prol@outputcolumns\@ne
1436 \prol@outputcolumns\@ne
1437 \prol@outputcolumns\@ne
1438 \prol@outputcolumns\@ne
1439 \prol@outputcolumns\@ne
143

```
1435 \pcol@getcurrpinfo{\global\c@page}{\global\@colht}{\global\topskip}%
```

```
1436 \@tempdima-\maxdimen \@tempdimb-\maxdimen \pcol@colht-\maxdimen
```

```
1437 \@pageht-\maxdimen \@tempdimc\maxdimen \@pagedp\maxdimen \@tempcntb\z@
```

```
1438 \pcol@dfloatsfalse
```

1439 \pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do\pcol@measurecolumn

As described above, any items can be empty, naturally for top floats, footnotes and bottom floats, but also including main vertical lists if the current column-pages were not in p_t before the invocation of \pcol@flushcolumn. Moreover, all main vertical lists can be empty if all leading column-pages just have started (by \newpage, for example). More weirdly, the case of all-empty main vertical lists can be accompanied with other non-empty items when columns have floats or footnotes which cannot be in $p_t - 1$ but are found their places in p_t .

Taking it into account that any items can be empty and the other item of page-wise footnotes, we have to determine whether the following two operations are taken; invocation of $\col@synccolumn$ for each column-page to set a synchronization point or to add an infinite stretch (and shrink) to its bottom; and the examination of the height of each columnpage, taking the synchronization point to be set into account, to tell the necessity of explicit page break with $\ifpcol@flush = true$. For the latter we calculate the examination target $V = \@tempdimb$ to be compared with $\pi^h(p_t)$, while for the former we determine the value of a switch $f = \if@tempswa$ so that we invoke $\pcol@synccolumn$ iff f = true and $V \ge 0$.

For synchronized column-switching with \ifpcol@clear = false, we let $f = (V_T \ge 0)$ to mean at least one column-page has a top float or non-empty main vertical list, i.e., $F_c(\{t, m\}) =$ true for some $c \in [0, C)$. That is if $V_T < 0$, since the next items added to all column-pages are placed at the top of the page¹⁸⁹, we don't need to set synchronization points in them. As for V, we let $V = \max(V_T, 0) + \max(V_B, 0) + v^f$ where v^f is the sum of height-plus-depth of $\pi^f(p_t)$ and $\skip \cdot \pi^f(p_t)$ if p_t has page-wise footnotes, or 0 otherwise¹⁹⁰. Note that it can be $V_P + v^f \le \pi^h(p_t) < V_T + V_B + v^f = V$ to mean setting the synchronization point at V_T below p_t 's top edge would push bottom stuff beyond its bottom edge and thus we need an explicit page break to place the point at the top of $p_t + 1$ (in usual cases).

For pre-flushing column height check or page flushing with ifpcol@clear = true on the other hand, we let $f = \neg col@sync to invoke \col@synccolumn only for page flushing and thus not for pre-flushing column height check. As for <math>V$, we let $V' = V'_P$ or $V' = V_P$ according as we working on last page or not, and then let $V = max(V', 0) + v^f$ or V = V' according as p_t has page-wise footnotes or not. That is, we have to invoke $col@synccolumn unless p_t$ is perfectly empty.

Then if $\fipcol@clear = false$ and $\max(V, V - D'_T + V_E) > \pi^h(p_t)$ where $D'_T = D_T$ if $0 \le D_T < \infty$ or 0 otherwise, or $\fipcol@clear = true$ and $V > \pi^h(p_t)^{191}$, we flush the page. That is, if the condition above holds, we let $\fipcol@flush = true$ and $d = \col@nextcol = c_{max}$ to tell $\col@switchcol or \col@flushclear$ to make an explicit page break in the column c_{max} from which we restart, and f = false to skip $\col@synccolumn$ to postpone the explicit synchronization. Note that the bias $V_E = \col@ensurevspace$ in synchronized column-switching is to avoid breaking a column-page just below the synchronization point due to too small space below the point, less than $\colwed{baselineskip}$ in default but can be other threshold explicitly defined by $\colwed{ensurevspace}$. That is, since $V - D_T + k\colwed{baselineskip}$ usually means the vertical position at which k-th baseline below the synchronization point is placed, the flushing condition with $V_E = k\colwed{baselineskip}$ ensures that the page is flushed iff the space below the point cannot accommodate k lines. Also note that necessary flushing with

¹⁸⁹In usual cases, but it can mean some of them have negative vertical sizes. Even though we can detect such a very unlikely special case, it is very tough to define the reasonable synchronization point above the top of p_t . Therefore, we assume the point is at the top of p_t and thus do nothing.

¹⁹⁰In the real implementation, $V = -\infty$ if $V_T = V_B = -\infty$ and no page-wise footnotes are presented, but this difference does not affect the decisions because $f \wedge (V \ge 0) = (V_T < 0) \wedge (V \ge 0) = false$ and $V \le \pi^f(p_t)$ with either V = 0 or $V = -\infty$.

 $^{^{191}}$ The examination is redundant in page flushing with \ifpcol@sync = false because it is assured that no overflow happens in any column-page by pre-flushing column height check and explicit page breaking, but is not harmful.

 $V > \pi^h(p)$ assuredly takes place even when D_T is unusually large and/or V_E is negative to make $-D_T + V_E < 0$.

Finally if $V \ge 0$ and f = true, we invoke \pcol@synccolumn for each column $c \in [0, C)$ to set a synchronization point in it or to add an infinite stretch (and shrink) at its bottom for flushing.

```
1440
      \@tempswatrue \global\pcol@flushfalse
1441
      \ifpcol@clear
        \ifpcol@lastpage \@tempdimb\pcol@colht \else \@tempdimb\@pageht \fi
1442
        \ifpcol@sync \@tempswafalse \fi
1443
1444
      \else
        \ifdim\@tempdima<\z@
                                    \@tempswafalse
1445
        \else\ifdim\@tempdimb<\z@ \@tempdimb\@tempdima</pre>
1446
        \else
                                    \advance\@tempdimb\@tempdima
1447
        \fi\fi
1448
1449
      \fi
      \ifpcol@scfnote\ifvoid\pcol@footins\else
1450
        \ifdim\@tempdimb<\z@ \@tempdimb\z@ \fi
1451
        \advance\@tempdimb\ht\pcol@footins \advance\@tempdimb\dp\pcol@footins
1452
        \advance\@tempdimb\skip\pcol@footins
1453
      \fi\fi
1454
      \dimen@\@tempdimb
1455
1456
      \ifpcol@clear\else \ifdim\dimen@<\z@\else
1457
        \ifdim\@tempdimc=\maxdimen\else \ifdim\@tempdimc<\z@\else
1458
          \advance\dimen@-\@tempdimc
1459
        \fi\fi
1460
        \advance\dimen@\pcol@@ensurevspace
        \ifdim\dimen@<\@tempdimb \dimen@\@tempdimb \fi
1461
      \fi\fi
1462
      \ifdim\dimen@>\@colht
1463
        \global\pcol@flushtrue \@tempswafalse \pcol@nextcol\@tempcntb
1464
      \fi
1465
      \ifdim\@tempdimb<\z@\else \if@tempswa
1466
        \pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do\pcol@synccolumn</pre>
1467
      fi fi
1468
1469
```

\pcol@flushcolumn The macro \pcol@flushcolumn is invoked for each column $c \in [0, C)$ from \pcol@sync to ship out the current column-page of c into S_c if it is not leading one, i.e., $p = \kappa_c(\beta^p) < p_t$. The macro also ships out float pages from p+1 up to p_t-1 if we have deferred floats to fill them and, if this float flushing still leaves deferred floats, puts some of them to the leading column-page being current now as its top and/or bottom floats.

First we obtain the column-context in κ_c by \pcol@getcurrcol and examines if $p = \kappa_c(\beta^p) < p_t$. If it does not hold to mean c has leading column-page, we do nothing.

Otherwise, we save $\ifpcol@lastpage into \ifpcol@lastpagesave turning the former switch$ *false* $because we are working on a non-leading column-page definitely in a non-last page. Then we put the contents of the current column-page <math>\kappa_c(\beta^b)$ adding \vfil at its tail into $\box255$ being the TEX's standard interface to carry the main vertical list for \ufleture . We also move everything in $\kappa_c(\tau)$ obtained by $\col@getcurrfoot$ into \footins and return $\kappa_c(\tau)$ to \ufleture is not void.

Then we obtain p's page context by $\pcol@getcurrpage</code> and, if it has page-wise footnotes in <math>\pi^f(p)$, we shrink \colht by the space required for the footnotes using $\pcol@shrinkcolbyfn$ and add the stretch/shrink components of $\skip \cdot \pi^f(p)$ at the bottom of $\box255$ by $\pcol@$

unvbox@cclv, as we did in \pcol@makecol. Otherwise we take a special care of the case that the height-plus-depth of $\kappa_c(\beta^b)$ is greater than $\pi^h(p)$ due to that its height is almost equal to $\pi^h(p)$ and thus its depth makes the hight-plus-depth exceeding $\pi^h(p)$. This excess is revealed by the \vfil we just have added making the height-plus-depth the height of \box255, and would cause overfull in \@makecol and \pcol@makecol because they need the height, i.e., not height-plus-depth, of \box255 not exceeding $\pi^h(p)$. Therefore if it happens, we we remove the \vfil and cap the height of \box255 by \@maxdepth to pretend as if the box is directly passed from TFX's page builder.

Next we examine if $\kappa_c(\rho_t)$ was made ∞ by \pcol@makefcolumn invoked from this macro itself when it processed the column-page in the previous pre-flushing column height check for environment closing, which found a page break should be done. That is, $\kappa_c(\rho_t) = \infty$ means the current column-page was once judged to be in the last page but pre-flushing column height check forced a page break to make it non-last, it should have all deferred floats now listed in $\kappa_c(\lambda_t)$ at \end{paracol}, but their total size is less than the threshold to make a usual float column for the last page. If so, since the page is not last now, we put all floats in $\kappa_c(\lambda_t)$ by \pcol@makefcolpage as the ship-out image in \@outputbox, ignoring the contents added to \box255 in the operations above because $\kappa_c(\beta^b)$ should be empty, and letting $\kappa_c(\rho_t) = 0$ to mean the floats have been processed¹⁹².

Otherwise, since the column-page can be put as usual, we invoke \pcol@@makecol¹⁹³ giving \@maxdepth to it to build the complete column-page in \@outputbox with depth capping and with the following setting¹⁹⁴.

Finally, regardless of $\kappa_c(\rho_t) = \infty$ or not, the resulting \Coutputbox becomes $s_c(p)$ and is added to the tail of S_c by \Cons.

1470	\def\pcol@flushcolumn{%
1471	\pcol@getcurrcol
1472	\ifnum\count\@currbox<\pcol@toppage
1473	\ifpcol@lastpage \pcol@lastpagesavetrue \else \pcol@lastpagesavefalse \fi
1474	\pcol@lastpagefalse
1475	\pcol@page\count\@currbox
1476	\setbox\@cclv\vbox{\unvbox\@currbox \vfil}%
1477	\ifvoid\pcol@currfoot\else
1478	\pcol@Fb
1479	\@cons\@freelist\pcol@currfoot
1480	\pcol@Fe{flushcolumn(colfn)}%
1481	\fi
1482	\pcol@getcurrfoot\box
1483	\pcol@getcurrpage
1484	\ifvoid\pcol@footins
1485	\ifdim\ht\@cclv>\@colht
1486	\setbox\@cclv\vbox{\boxmaxdepth\@maxdepth \unvbox\@cclv \unskip}%
1487	\fi
1488	\else
1489	\pcol@shrinkcolbyfn\@colht\pcol@footins\relax

 $^{^{192}\}kappa_c(\lambda_t)$ can have any values other than ∞ because definitely it will not be referred to in its inherent sense in the situation with no further float additions and no deferred floats.

 $^{^{193}}$ Neither \pcol@makecol because \box255 has \vfil at its tail and the column-page should be short enough, nor \@makecol because we need to ensure the depth of resulting \@outputbox is capped.

 $^{^{194}}$ LAT_EX's has another \insert named \@kludgeins for \enlargepage but paracol does not cares about it.

1490	\setbox\@cclv\vbox{\pcol@unvbox@cclv\pcol@footins}%
1491	\fi
1492	<pre>\pcol@Logstart{\pcol@flushcolumn(\number\c@page:\number\pcol@currcol)}</pre>
1493	\ifdim\@toproom=\maxdimen
1494	\setbox\@outputbox\pcol@makefcolpage \global\@toproom\z@
1495	\else
1496	\pcol@@makecol\@maxdepth
1497	\fi
1498	\pcol@Logend\pcol@flushcolumn
1499	\global\setbox\@currbox\box\@outputbox
1500	\expandafter\@cons\csname pcol@shipped\number\pcol@currcol\endcsname
1501	\@currbox

Then for each $q \in [p+1, p_t-1]$, we repeat the followings; get q's page context by \pcol@ getcurrpage; shrink \@colht by \pcol@shrinkcolbyfn if q has page-wise footnotes; try to make a float column in \@outputbox by \@makefcolumn giving it \@deferlist being $\kappa_c(\lambda_d)$ at initial but will be shrunk; if the float column is made, acquire an \insert by \@next to keep the contents of \@outputbox and to be added to the tail of S_c by \@cons.

1502	\advance\pcol@page\@ne
1503	\ifx\@deferlist\@empty\else
1504	\@whilenum\pcol@page<\pcol@toppage%
1505	\pcol@getcurrpage
1506	\ifvoid\pcol@footins\else
1507	\pcol@shrinkcolbyfn\@colht\pcol@footins\relax
1508	\fi
1509	\@makefcolumn\@deferlist
1510	\if@fcolmade
1511	\pcol@Fb
1512	\@next\@currbox\@freelist{\global\setbox\@currbox\box\@outputbox}%
1513	\pcol@ovf
1514	\pcol@Fe{flushcolumn(fcol)}%
1515	\expandafter\@cons
1516	\csname pcol@shipped\number\pcol@currcol\endcsname\@currbox
1517	\fi
1518	\advance\pcol@page\@ne}%
1519	\fi

Next, since we reach p_t and thus restore ifpcol@lastpage from <math>ifpcol@lastpagesave because the top page can be last. Then we acquire the current column-page of c which is now in p_t and thus empty, by $\ensuremath{\sc 0}$ the $\ensuremath{\sc 0}$ color $= \pi^h(p_t)$ by $\pcol@getcurrpinfo but shrinking them by <math>\pcol@shrinkcolbyfn if p_t$ has page-wise footnotes, and reinitialize the float placement parameters by $\pcol@floatplacement$. Then, if $\kappa_c(\lambda_d)$ still has some floats, we make a float column for some of them in the top page by $\pcol@makefcolumn if \ifpcol@clear = true meaning flushing, or try to move some of them to <math>\kappa_c(\lambda_t) = \@colroom is used in \pcol@makefcolumn as a working register, we let <math>\@colroom = \pi^h(p_t)$ again after its invocation. After that we save column-context including those given by $\pcol@stcurrcolnf$ because all footnotes are shipped out, and let $\kappa_c(\beta^p) = p_t$. We also let $\kappa_c(\beta^r) = \@colroom possibly modified by <math>\pcol@trynextcolumn but after canceling the shrinkage of <math>\@colht due to page-wise footnotes, i.e., \kappa_c(\beta^r) \leftarrow \kappa_c(\beta^r) + (H - H') \$ where H and H' are $\@colht before and after the shrinkage respectively.$

1520 \ifpcol@lastpagesave \pcol@lastpagetrue \fi

```
\pcol@Fb
1521
        \@next\@currbox\@freelist{\global\setbox\@currbox\vbox{}}\pcol@ovf
1522
        \pcol@Fe{flushcolumn(col)}%
1523
        \pcol@getcurrpinfo\@tempcnta{\global\@colht}\@tempskipa
1524
        \@pageht\@colht
1525
        \ifvoid\pcol@footins\else \pcol@shrinkcolbyfn\@colht\pcol@footins\relax \fi
1526
        \global\@colroom\@colht \pcol@floatplacement
1527
        \ifx\@deferlist\@empty\else
1528
          \ifpcol@clear
1529
            \pcol@makefcolumn \global\@colroom\@colht
1530
1531
          \else
            \pcol@trynextcolumn
1532
        \fi\fi
1533
        \pcol@setcurrcolnf
1534
        \global\count\@currbox\pcol@toppage
1535
        \advance\@pageht-\@colht \advance\@pageht\@colroom
1536
        \global\dimen\@currbox\@pageht
1537
      \fi %\ifnum\count\@currbox<\pcol@toppage
1538
1539
      \advance\pcol@currcol\@ne}
1540
```

First, we scan the copy of $\kappa_c(\lambda_d)$ applying \pcol@makefcolelt to each element to have the floats to be put in \@toplist, which is assuredly empty because the current column-page of c has already been shipped out to empty it, and those still deferred in $\kappa_c(\lambda_d)$. Prior to scan, we let $H_r = \pi^h(p_t)^{195} + \alpha$, as the space initially available for floats each of which being ϕ is assumed to consume $v(\phi) = h(\phi) + d(\phi) + \alpha$, and $H_t = \@colroom = -\alpha$ as the initial value of the accumulated size of $v(\phi)$ for all ϕ to be put, where $\alpha = \floatsep$ if \floatsep if $\floatspace = true$ as discussed afterward, or $\alpha = \@fpsep$ otherwise.

Then if the resulting $\langle \texttt{Qtoplist}$ is not empty¹⁹⁶, we examine if p_t is the last page ($\langle \texttt{ifpcolQ} | \texttt{lastpage} = true$) and $\kappa_c(\lambda_d)$ is empty to mean the last column-page have all deferred floats. This case is subtle because if we make the column-page a float column it can be sparse and unnecessarily throw the post-environment stuff to the next page. Therefore, we intend to pack floats to the page top as top floats and thus have let $\alpha = \langle \texttt{floatsep} \text{ in the building process of } \langle \texttt{Qtoplist} above^{197}$, but it may make a too tall column-page only having floats shrinking the post-environment stuff in the page. In addition, if other columns have float pages in the last page, packing the floats as top floats should give inconsistent appearance but we don't know whether the columns following c has float pages. Therefore, we performs this float packing if making the float page gives too sparse, more specifically if $H_t < \langle \texttt{floatpagefraction} \times \pi^h(p_t) = \langle \texttt{Qtpmin}, \texttt{but postpone the final decision until the column-page is eventually shipped out by <math>\mathsf{pcolQflushcolumn}$ or $\mathsf{pcolQmakeflushedpage}$. That is, if the all conditions above hold, we keep $\langle \texttt{Qtoplist}$ so that it is saved in $\kappa_c(\lambda_t)$ and let $\kappa_c(\rho_t) = \infty$ to indicate that the column has pending floats. Note that the floats are shipped out by $\mathsf{pcolQflushcolumn}$ if the page so that the floats are shipped out by $\mathsf{pcolQflushcolumn}$ if the page so tall column in p_t to

 $^{^{195}\}pi^h(p_t)$ referred in this macro may have been shrunk by page-wise footnotes in \pcol@flushcolumn.

¹⁹⁶It can happen if the first float is larger than $\pi^h(p_t)$.

 $^{^{197}}$ We dare to do it knowing the natural component of floatsep is a little bit (4pt) larger than that freeprime equation (4pt) and the possibility of having fewer floats than those given by $\mbox{@makefcolumn}$.

force a page break making p_t non-last. Also note that, in any cases, letting $\kappa_c(\rho_t) = \infty$ is safe because no longer we will have any float additions to the column-page.

Otherwise, i.e., if we are working on a non-last page to be flushed or a float column is to be made for the last page, we put all floats in \@toplist in a \vbox of $\pi^h(p_t)$ tall by \pcol@makefcolpage and then let $\kappa_c(\beta^b)$ be another \vbox having it. This encapsulation of the float column is necessary because $\kappa_c(\beta^b)$ can be put back to the main vertical list after the pre-flushing column height check to remove skips above and below the floats, namely \@fptop and \@fpbot, if the contents were not encapsulated.

```
1541 \def\pcol@makefcolumn{%
      \ifpcol@lastpage \@tempdimc\floatsep \else \@tempdimc\@fpsep \fi
1542
      \@tempdima\@colht \advance\@tempdima\@tempdimc \global\@colroom-\@tempdimc
1543
1544
      \begingroup
        \let\@elt\pcol@makefcolelt
1545
        \let\reserved@b\@deferlist
1546
1547
        \global\let\@deferlist\@empty
1548
        \reserved@b
      \endgroup
1549
      \ifx\@toplist\@empty\else
1550
        \@tempswatrue
1551
        \ifpcol@lastpage \ifx\@deferlist\@empty \ifdim\@colroom<\@fpmin
1552
1553
          \@tempswafalse \global\@toproom\maxdimen
1554
        \fi\fi\fi
        \if@tempswa \global\setbox\@currbox\vbox{\pcol@makefcolpage}\fi
1555
      \fi}
1556
```

\pcol@makefcolelt The macro \pcol@makefcolelt $\langle \phi \rangle$ is invoked solely from \pcol@makefcolumn to be applied to each float element ϕ in (the copy of) $\kappa_c(\lambda_d)$. We examine if $v(\phi) = h(\phi) + d(\phi) + \alpha \leq H_r$ to mean the float column being built has room large enough for the float ϕ . If so, we add ϕ to \@toplist by \@cons, and let $H_r \leftarrow H_r - v(\phi)$ and $H_t \leftarrow H_t + v(\phi)$. Otherwise, we add ϕ to $\kappa_c(\lambda_d)$ by \@cons to make it deferred again, and let $H_r = -\infty$ so that the examinations for any succeeding elements fail.

```
1557 \def\pcol@makefcolelt#1{%
1558 \@tempdimb\ht#1{}\advance\@tempdimb\dp#1{}\advance\@tempdimb\@tempdimc
1559 \ifdim\@tempdima \@cons\@deferlist#1\relax
1560 \@tempdima-\maxdimen
1561 \else \@cons\@toplist#1\relax
1562 \advance\@tempdima-\@tempdimb \global\advance\@colroom\@tempdimb
1563 \fi}
```

\pcol@makefcolpage The macro \pcol@makefcolpage is invoked from \pcol@flushcolumn, \pcol@makefcolumn and \pcol@imakeflushedpage to build a float column having floats in \@toplist, which is then returned to \@freelist and then emptied. The floats are put in a \vbox of \@colht tall with vertical skips of \@fptop, \@fpsep and \@fpbot above, between and below them respectively. The box is then let be $s_c(p)$ or $\kappa_c(\beta^b)$ explicitly or implicitly by the invokers, with an encapsulation in the case of \pcol@makefcolumn.

```
1564 \def\pcol@makefcolpage{\vbox to\@colht{%
1565 \vskip\@fptop \vskip-\@fpsep
1566 \def\@elt##1{\vskip\@fpsep\box##1}\@toplist \vskip\@fpbot}%
1567 \pcol@Fb
1568 \xdef\@freelist{\@freelist\@toplist}\global\let\@toplist\@empty
1569 \pcol@Fe{makefcolpage}%
1570 }
```

1571

- - 1572 \def\pcol@measurecolumn{%
 - 1573 \pcol@getcurrcol
 - 1574 \climits \@tempswafalse
 - 1575 \dimen@\z@ \pcol@addflhd\@toplist\pcol@textfloatsep
 - 1576 \global\skip\@currbox\dimen@
 - 1577 \advance\dimen@\ht\@currbox \advance\dimen@\dp\@currbox \dimen@ii\dimen@

Next we examine if the main vertical list $\kappa_c(\beta^b)$ is empty by $\col@ifempty$ and, if so, we let $\delta_c = \kappa_c(\delta) = \infty$ and save it (together with others) by $\col@setcurrcol</code> so that, if the column defines the <math>V_T$ finally by its top floats, D_T is let ∞ and the fact that the column has empty list is remembered. Otherwise, we let $\delta_c = \kappa_c(\delta)$ and $\if@tempswa = true$ to represent $F_c(\{t,m\}) = f_t \vee f_m$ because $f_m = true$. Then we invoke $\col@measureupdate$ to let $V_T = size_c(t) + size_c(m) = SIZE_c(\{t,m\})$ and $D_T = \delta_c$ if $F_c(\{t,m\}) = true$ and $V_T < SIZE_c(\{t,m\})$.

- 1578 \pcol@ifempty\@currbox
- 1579 {\global\pcol@prevdepth\maxdimen \pcol@setcurrcol}%
- 1580 {\@tempswatrue}%

Next we let $size_c(f) = 0$ if $\kappa_c(\tau^b)$ is void, or otherwise let $size_c(f) = h(\kappa_c(\tau^b)) + d(\kappa_c(\tau^b)) + \kappa_c(\tau^s)^{198}$ and if@tempswa = true because $f_c(f) = true$ and thus $F_c(\{t, m, f\}) = true$. After that, we calculate $size_c(f) + size_c(b)$ by pcol@addflhd giving it $\kappa_c(\lambda_b)$ and ∞ to mean textfloatsep should be used for the calculation as its argument also to have $if@tempswa = F_c(\{t, m, f, b\})$. Then we let $V_B = size_c(f) + size_c(b)$ if $V_B < size_c(f) + size_c(b)$, and let $V_P = size_c(t) + size_c(m) + size_c(f) + size_c(b) = SIZE_c(\{t, m, f, b\})$ and $c_{max} = c$ if $F_c(\{t, m, f, b\}) = true$ and $V_P < SIZE_c(\{t, m, f, b\})$.

1582 \ifvoid\pcol@currfoot \dimen@\z@

1583 \else

 $1584 \qquad \verb|dimen@ht|pcol@currfoot \advance\dimen@dp|pcol@currfoot||$

1585 \advance\dimen@\skip\pcol@currfoot

```
1586 \@tempswatrue
```

```
1587 \fi
```

```
1588 \pcol@addflhd\@botlist\maxdimen
```

```
1589 \ifdim\dimen@>\@tempdimb \@tempdimb\dimen@ \fi
```

1590 \advance\dimen@\dimen@ii

1593 \fi\fi

^{1591 \}if@tempswa \ifdim\dimen@>\@pageht

^{1592 \@}pageht\dimen@ \@tempcntb\pcol@currcol

 $^{^{198}\}mathrm{We}$ ignore the height and depth of **\footnoterule** because they are expected to be 0 and are so in the default setting.

Next, we let d_c be the depth of the lowest non-empty items among the main vertical list, footnotes and bottom floats. That is, we let $d_c \leftarrow \kappa_c(\delta)$ at first, and then, if $\ifpcol@bfbottom = true$, override it by $d_c \leftarrow d(\kappa_c(\tau^b))$ if there are footnotes, and finally override it by $d_c \leftarrow 0$ for the bottom floats if exist adding \textfloatsep to $SIZE_c(\{t, m, f, b\})$ to have $SIZE_c(\{t, m, f, b'\})$. This overriding order of $d(\kappa_c(\tau^b))$ and then 0 by bottom floats is reversed when $\ifpcol@bfbottom = false$ according to the implementation of \makecol . Then, we invoke $\pcol@measureupdate$ again to let $V'_P = SIZE_c(\{t, m, f, b'\})$ and $D_P = d_c$ if $F_c(\{t, m, f, b\}) = true$ and $V'_P < SIZE_c(\{t, m, f, b'\})$. It also lets $D_P = d_c$ if $F_c(\{t, m, f, b\}) = true$, $V'_P = SIZE_c(\{t, m, f, b'\})$ and $D_P > d_c$.

Finally, we let $\ ifpcol@dfloats = true \ if \\ \kappa_c(\lambda_d) \neq \emptyset$ to tell $\ col@makeflushedpage$ that the last page must be *full size* and $\ col@output@end$ to flush the deferred column-wise floats.

```
\dimen@ii\pcol@prevdepth
1594
1595
      \ifpcol@bfbottom
        \ifvoid\pcol@currfoot\else \dimen@ii\dp\pcol@currfoot \fi
1596
        \ifx\@botlist\@empty\else \dimen@ii\z@ \advance\dimen@\textfloatsep \fi
1597
1598
      \else
        \ifx\@botlist\@empty\else \dimen@ii\z@ \advance\dimen@\textfloatsep \fi
1599
1600
        \ifvoid\pcol@currfoot\else \dimen@ii\dp\pcol@currfoot \fi
1601
      \fi
      \pcol@measureupdate\pcol@colht\dimen@\@pagedp\dimen@ii
1602
      \ifx\@deferlist\@empty\else \pcol@dfloatstrue \fi
1603
      \advance\pcol@currcol\@ne}
1604
```

\pcol@addflhd The macro \pcol@addflhd $\langle list \rangle \langle tfs \rangle$ is invoked twice from \pcol@measurecolumn for a column \pcol@hdflelt c to measure $size_c(x)$ ($x \in \{t, b\}$) of top (x = t) or bottom (x = b) floats. The arguments and registers referred to in the macro have the following values according to x = t or x = b.

	x = t	x = b
$\langle list \rangle$	$\kappa_c(\lambda_t)$	$\kappa_c(\lambda_b)$
$\langle tfs \rangle$	\pcol@textfloatsep	\maxdimen
\if@tempswa	false	$F_c(\{t, m, f\})$
\dimen@	0	size(f)

The macro is also used in $\col@makecol and \col@output@switch for <math>x = t$ but with $\dimen@$ having the height of $\col@prespan$ for the measurement of the total height of prespanning-text stuff including top floats¹⁹⁹.

The macro at first examines if $\kappa_c(\lambda_x) = \langle list \rangle$ is empty and does nothing if so. Otherwise, \if@tempswa is turned *true* to have $f_c(t) = true$ for x = t or $F_c(\{t, m, f, b\}) = true$ for x = b. Then we scan all floats in $\langle list \rangle$ applying \pcol@hdflelt to each float ϕ to add $h(\phi) + d(\phi) + \langle lioatsep$ to \dimen@, from/to which we then subtract \floatsep and add σ_x because the last/first float is followed/preceded by the vertical skip of σ_x instead of \floatsep, to have $size_c(t)$ for x = t or $size_c(f) + size_c(b)$ for x = b being *returned* to \pcol@measurecolumn.

Note that σ_t is $\langle tfs \rangle = \col@textfloatsep$ if it is less than ∞ or \textfloatsep otherwise, while $\sigma_b = \textfloatsep$ always because $\langle tfs \rangle = \maxdimen$. Also note that σ_t can be biased by 10000 pt and thus larger than 5000 pt, if we have a MVL-float in top floats as discussed later. Another caution is that we ignore the contribution by \topfigrule nor \botfigrule because they should insert vertical items whose total height and depth are 0.

1605 \def\pcol@addflhd#1#2{%

1606 $\ifx#1\empty\else$

 $^{^{199}\}mathrm{In}$ these invocations, <code>\if@tempswa</code> is meaningless and not examined by the invokers.

```
1607
        \@tempswatrue
        \let\@elt\pcol@hdflelt
1608
        #1\advance\dimen@-\floatsep
1609
        \ifdim#2=\maxdimen \advance\dimen@\textfloatsep
1610
1611
        \else
          \advance\dimen@\pcol@textfloatsep
1612
          \ifdim\pcol@textfloatsep>5000\p@ \advance\dimen@-\@M\p@ \fi
1613
        \fi
1614
        \let\@elt\relax
1615
1616
      \fi}
1617 \def\pcol@hdflelt#1{\advance\dimen@\ht#1\advance\dimen@\dp#1%
      \advance\dimen@\floatsep}
1618
```

\pcol@measureupdate The macro \pcol@measureupdate $\langle V \rangle \langle v \rangle \langle D \rangle \langle d \rangle$ is invoked twice in \pcol@measurecolumn for c to update $V \in \{V_T, V_P'\}$ and $D = \{D_T, D_P\}$ as follows if \if@tempswa, being $F_c(\{t, m\})$ for $V = V_T$ or $F_c(\{t, m, f, b\})$ for $V = V_P'$, is true.

$$V \leftarrow \max(V, v)$$
 $D \leftarrow \begin{cases} \min(D, d) & V = v \\ D & V \neq v \end{cases}$

The arguments v and d have the followings according to V.

 $V = V_T : v = SIZE_c(\{t, m\}) \qquad d = \delta_c$ $V = V'_P : v = SIZE_c(\{t, m, f, b'\}) \qquad d = d_c$

```
1619 \def\pcol@measureupdate#1#2#3#4{\if@tempswa
1620 \ifdim#1<#2\relax#1#2\relax#3#4\relax
1621 \else\ifdim#1=#2\ifdim#3>#4\relax#3#4\fi\fi\fi}
1622
```

\pcol@synccolumn The macro \pcol@synccolumn is invoked for each column $c \in [0, C)$ from \pcol@sync to set a synchronization point at V_T from the top of the current column-page of c if \ifpcol@clear = false, or flush it otherwise. After obtaining c's column-context κ_c by \pcol@getcurrcol, we process one of the following three cases.

The first case is for flushing with $\ifpcol@clear = true$. In this case we simply add \vfil at the tail of the main vertical list in $\kappa_c(\beta^b)$ to make the whole column-page possibly with other items fit in a box of \colht tall and, if $\kappa_c(\xi) \neq \infty$ to mean the column to be flushed has a synchronization point, we also add an infinite shrink of 1/10000 fil so as to cancel a finite shrink just below the point, as done in $\coll@makecol^{200}$. We also let $\kappa_c(\delta) = 1000 \text{ pt}$ to mimic TEX's mechanism of \prevdepth with the empty main vertical list in the next column-page²⁰¹.

```
1623 \def\pcol@synccolumn{%
1624 \pcol@getcurrcol
1625 \ifpcol@clear
1626 \global\pcol@prevdepth\@m\p@
1627 \global\setbox\@currbox\vbox{\unvbox\@currbox
1628 \ifdim\pcol@textfloatsep=\maxdimen \vfil
1629 \else \vskip\z@\@plus1fil\@minus.0001fil
1630 \fi}%
```

²⁰⁰Just in case, because it looks impossible that the natural height of the column-page exceeds $\pi^h(p_t)$ with pre-flushing column height check. ²⁰¹The author is not sure if this setting is really necessary but, at least, it looks working well (though other

²⁰¹The author is not sure if this setting is really necessary but, at least, it looks working well (though other setting looks all right too).

The second and third cases are for synchronized column-switching. The second case is for $D_T = \infty$ to mean the synchronization point is set just below the top floats of a column whose main vertical list is empty because it is definitely $V_T \ge 0 > -\infty$. In this case, we should not put anything back to the main vertical list, because the column having defined the point will restart from the top of its column-page with \topskip and thus other columns should do so for the stuff following the point. Therefore, we put $\kappa_c(\beta^b)$ as the last top float, namely MVL-float because it is for the main vertical list, acquiring an \insert from \Offreelist by \Onext and assigning it to \pcolOfloat so that we pretend main vertical lists of all columns are empty.

The float has zero height and depth, and contains the followings if we have some real floats; a vertical skip of $-\floatsep$ to go back to the bottom of the last real float; \topfigrule and a skip of \textfloatsep to separate $\kappa_c(\beta^b)$ from the last real float; and $\kappa_c(\beta^b)$ followed by \ss to avoid overfull and underfull. Otherwise, i.e., we don't have any real floats, neither of the skips nor \topfigrule are put in the MVL-float because we let $\floatsep = \textfloatsep = 0$ and $\topfigrule = \relax$ temporarily in a group. Then we set the synchronization point by enlarging the space below the MVL-float so that the total size of all floats including \floatsep and \textfloatsep , which may be 0 as set in the process above, is equal to V_T . This enlarging is done by letting $\kappa_c(\xi) = V_T - (v_c(t) - \textfloatsep + \floatsep)$, the second term of which is the vertical size of the top float insertion process in $\pcol@cflt$ so that the top floats including the MVL-float consumes V_T as a whole²⁰².

Note that the process above involves floatsep and textfloatsep with some finite stretch and shrink, but these factors will not contribute the final result because they are canceled by vss in the MVL-float and by the small infinite stretch and shrink put by pcol@makecol</code> and $this macro for flushing. Also note that <math>\kappa_c(\xi)$ is then biased by 10000 pt so that pcol@cfltwill not put topfigrule because it has been already put as a part of the MVL-float or we don't have any real floats. We also let $\kappa_c(\delta) = 1000$ to mean the column-page's main vertical list is empty, so as to mimic T_FX 's mechanism of prevdepth with an empty list again.

Another attention we have to pay is that column-pages with $\kappa_c(\xi) = \infty$ does not have any synchronization points, and thus $\kappa_c(\xi) < \infty$ means a synchronization has already taken place in them. If this $\kappa_c(\xi) < \infty$ happens with $D_T = \infty^{203}$, we cannot update $\kappa_c(\xi)$ because \pcol@measurecolumn took care of its value on measuring $v_c(t)$. Therefore, we do nothing if $\kappa_c(\xi) < \infty$ but just let succeeding stuff be added to the main vertical list as in column-switching without synchronization.

1631	\else
1632	\@tempdimb\@tempdima
1633	\advance\@tempdimb-\skip\@currbox
1634	\ifdim\@tempdimc=\maxdimen
1635	\ifdim\pcol@textfloatsep=\maxdimen \begingroup
1636	\ifx\@toplist\@empty
1637	<pre>\textfloatsep\z@ \floatsep\z@ \let\topfigrule\relax</pre>
1638	\fi
1639	\pcol@Fb
1640	\@next\pcol@float\@freelist{\global\setbox\pcol@float\vbox to\z@{%
1641	<pre>\vskip-\floatsep \topfigrule \vskip\textfloatsep</pre>
1642	\unvbox\@currbox \vss}}\pcol@ovf
1643	\pcol@Fe{synccolumn(topfloat)}%
1644	\@cons\@toplist\pcol@float

²⁰²This enlarging cannot be done by making the float's height $V_T - v_c(t) - \text{loatsep}$ (or \textfloatsep) because the height can be negative.

²⁰³This can happen when a synchronization with $D_T = \infty$ is immediately followed by another synchronization or, more unlikely, by additions of items whose total amount is negative and then a synchronization.

1645	\advance\@tempdimb\textfloatsep \advance\@tempdimb-\floatsep
1646	\advance\@tempdimb\@M\p@
1647	\global\pcol@prevdepth\@m\p@
1648	\global\pcol@textfloatsep\@tempdimb
1649	\endgroup \fi

The third and last case is for $D_T < \infty$ and thus most usual. In this case, we enclose everything in $\kappa_c(\beta^b)$ in a \vbox whose height is $h_c^v = V_T - v_c(t)$ and let $\kappa_c(\beta^b)$ have it so that the item following the synchronization point start at V_T . An attention we have to pay is that it can be $h_c^v < \langle \text{topskip} \text{ to let TEX} \text{ insert a vertical skip of the difference between them when the$ box is returned to the main vertical list pushing down the synchronization point a little bit²⁰⁴. $Therefore, if so, we let <math>\kappa_c(\beta^b)$ have the followings; a $\langle \text{vbox of } \langle \text{topskip} \text{ tall having its old}$ contents at its top above which no vertical skip w^v_c going down to the synchronization point.

The encapsulation of the old contents $\kappa_c(\beta^b)$ in the box of h_c^v tall gives us the following two features desirable for synchronization. First, all vertical glues in the box are *frozen*, nullifying finite stretches in them because we insert an infinite stretch of 1/1000 fil at the bottom of $\kappa_c(\beta^b)$ to push up its old contents respecting other infinite stretches if any, as done by \raggedbottom, and also nullifying finite and infinite shrinks because $h_c^v \ge v_c(m)$ definitely. This freezing and nullification keeps synchronization points already in $\kappa_c(\beta^b)$ from being observed moving a little bit vertically. That is, if we have a glue just below a synchronization point and it were *visible* to TEX's page builder, the item below the glue could move up/down when the builder found a break point with some shrink/stretch. Though this moving up/down is inhibited by the small infinite stretch/shrink which the column-page will at its bottom finally, it is undesirable to make TEX misunderstanding that the glues are stretchable/shrinkable though they are not in reality.

Second, since the boxes in all column-page are zero deep due to the infinite stretch at their bottoms and these bottoms are aligned at the synchronization point, we have a clear view of the baseline progress after the synchronization regardless of their contents. That is, we let $\kappa_c(\delta) = D_T$ to broadcast D_T to all columns, so that the baselines of first items following the synchronization point are aligned **\baselineskip** below the bottom baseline of the column which defines D_T^{205} , if D_T plus the hight of each item is less than **\baselineskip**.

In addition, we let $\kappa_c(\xi) = \mathsf{textfloatsep}$ to indicate the column-page has the synchronization point we just have set, if it was ∞ to mean the point is the first one. By this setting, $\mathsf{pcol@makecol}$ and this macro itself will know that the column-page needs to have a small infinite shrink at its bottom to cancel finite ones below the synchronization point, while $\mathsf{pcol@}$ cflt acts as IAT_EX 's Qcflt because it should be $\kappa_c(\xi) \leq 5000\,\mathsf{pt}$ to mean the column-page does not have a MVL-float.

1650 \else

	1
1651	\global\pcol@prevdepth\@tempdimc
1652	\ifdim\pcol@textfloatsep=\maxdimen
1653	\global\pcol@textfloatsep\textfloatsep \f
1654	\global\setbox\@currbox%
1655	\ifdim\@tempdimb<\topskip

²⁰⁴This can happen not very unlikely especially with $v_c(t)$ a little bit less than V_T and $\kappa_c(\beta^b)$ being empty. ²⁰⁵Since D_T is given by one of the tallest columns whose depth is smallest among them, it is very likely that the bottom baseline of the column is lowest among all columns. However, another column can have the lowest one when its vertical size is a little bit shorter than V_T and its depth is small (e.g., 0). Though of course we can define D_T being V_T minus the height of the column having the largest height to make the first baseline below the synchronization point apart from the lowest one by **\baselineskip**, we dare to choose the definition of D_T because such lowest baseline often means that the column have some skip at its bottom to give us the impression that the space between the baselines of the tallest column and its first item is a little bit too large.

```
      1656
      \vbox to\topskip{\unvbox\@currbox \vskip\z@\@plus.0001fil}%

      1657
      \vskip-\topskip \vskip\@tempdimb

      1658
      \else

      1659
      \vbox to\@tempdimb{\unvbox\@currbox \vskip\z@\@plus.0001fil}%

      1660
      \fi

      1661
      \fi

      1662
      \fi
```

Finally, we let $\kappa_c(\nu_t) = 0$ to inhibit further addition of top floats because we have fixed the space for them²⁰⁶, and save it and other column-context members into κ_c by \pcol@setcurrcol.

1663 \global\@topnum\z@ \pcol@setcurrcol
1664 \advance\pcol@currcol\@ne}
1665

11.8 Page Flushing

\pcol@output@flush The macro \pcol@output@flush is invoked solely from \pcol@specialoutput to process the \output request made by \flushpage. We invoke \pcol@makeflushedpage giving it \@colht as the height of each column-page to have the ship-out image of the top page including its spanning stuff and page-wise footnotes in \@outputbox whose height is then set to be \textheight²⁰⁷, ensuring that its depth is capped by \boxmaxdepth = \@maxdepth. We also perform these height setting and depth capping on \pcol@rightpage if $C_L < C$ to mean parallel-paging. Then we invoke \@outputpage for shipping out, and then finally \pcol@ freshpage to have a new page to start new column-pages in it.

```
1666 %% Special Output Routines: Page Flushing
1667
1668 \def\pcol@output@flush{%
1669
      \pcol@makeflushedpage\@colht
1670
      \pcol@Logstart\pcol@output@flush
      \setbox\@outputbox\vbox to\textheight{\boxmaxdepth\@maxdepth
1671
        \unvbox\@outputbox}%
1672
      \ifnum\pcol@ncolleft<\pcol@ncol
1673
        \setbox\pcol@rightpage\vbox to\textheight{\boxmaxdepth\@maxdepth
1674
          \unvbox\pcol@rightpage}%
1675
1676
      \fi
      \pcol@Logend\pcol@output@flush
1677
1678
      \@outputpage
      \pcol@freshpage}
1679
1680
```

\pcol@output@clear The macro \pcol@output@clear is invoked solely from \pcol@specialoutput to process the \output request made by \clearpage. The first part up to \@outputpage and the last line of this macro are same as \pcol@output@flush to flush the top page and to have a newpage. In the remaining mid part, we invoke \pcol@flushfloats to ship out all deferred column-wise floats in all columns if any, and then do it for page-wise floats by the following invocations enclosed in a group; letting \pcol@rightpage = ⊥ for ordinary paging; \@dblfloatplacement to set up placement parameters followed by \f@depth = 0 to nullify the setting \f@depth = 1sp possibly done by it as discussed in the item-(2) of §1.8; \@makefcolumn with \@dbldeferlist to have a float page in \@outputbox if any; and a loop of background painting of \@outputbox

 $^{^{206} \}rm Allowing the addition is tremendously tough even when the column-page has sufficiently large space above the synchronization point.$

 $^{^{207}}$ Just in case because the height of source \@outputbox should be exactly \textheight though not specified so on its construction in \pcol@makeflushedpage.

and, if $C_L < C$, of empty \pcol@rightpage, and \@outputpage followed by \@makefcolumn repeated while we have a float page, i.e., $\iftedelta colmade = true$.

Note that the mid part is same as that found in \@doclearpage but we omit various adjuncts surrounding it as follows; examination of \if@twocolumn because we should have multiple columns; examination of \if@firstcolumn because we have to clear the page immediately even when we are not in the first column; concatenating \@dbltoplist with \@dbldeferlist and clearing it because the author believes \@dbltoplist must be empty on the invocation of this macro; and letting $\colht = \textheight because \pcol@flushfloats did it.$

```
1681 \def\pcol@output@clear{%
      \pcol@makeflushedpage\@colht
1682
      \pcol@Logstart\pcol@output@clear
1683
      \setbox\@outputbox\vbox to\textheight{\boxmaxdepth\@maxdepth
1684
1685
        \unvbox\@outputbox}%
      \ifnum\pcol@ncolleft<\pcol@ncol
1686
        \setbox\pcol@rightpage\vbox to\textheight{\boxmaxdepth\@maxdepth
1687
1688
          \unvbox\pcol@rightpage}%
1689
      \fi
      \pcol@Logend\pcol@output@clear
1690
      \@outputpage
1691
      \pcol@flushfloats
1692
1693
      \begingroup
1694
        \setbox\pcol@rightpage\box\voidb@x
        \@dblfloatplacement \let\f@depth\z@
1695
        \@makefcolumn\@dbldeferlist
1696
1697
        \@whilesw\if@fcolmade\fi{%
          \def\pcol@bg@floatheight{\pcol@bg@textheight}%
1698
1699
          \setbox\@outputbox\vbox to\textheight{%
            \pcol@bg@paintbox{Ff}\unvbox\@outputbox}%
1700
          \ifnum\pcol@ncolleft<\pcol@ncol
1701
            \setbox\pcol@rightpage\vbox to\textheight{\pcol@bg@paintbox{Ff}\vfil}%
1702
          \fi
1703
          \@outputpage
1704
1705
          \@makefcolumn\@dbldeferlist}%
1706
      \endgroup
1707
      \pcol@freshpage}
1708
```

 \colomakeflushedpage The macro $\colomakeflushedpage \langle ht \rangle$ is invoked from $\coloutput@flush$ or $\colomakeflushedpage \langle ht \rangle$ output@clear with $\langle ht \rangle = \colt and from \coltoutput@end with <math>\langle ht \rangle = \coltoutput@clear$ At first, we invoke $\colloutput@switch$ with setting $\ifpcol@clear = true$ to flush all pages up to $p_t - 1$ and to let $\kappa_c(\beta^b)$ have the ship-out image of the main vertical list of each column-page c in p_t . This invocation also lets $\pcol@colht = V'_P$ so that hereafter we will refer V'_P through $\langle ht \rangle$ if it is \pcol@colht for last page. Then after obtaining p_t 's page context to have $page(p_t) = \pi^p(p_t)$, $\colht = \pi^h(p_t)$ and $\ifpcol@nospan$ by $\col@getcurrpinfo$, we build the ship-out image of p_t in \Coutputbox, and \pcolCrightpage if parallel-paging, taking special care of the last page case as follows.

- (1) If $\ ext{ifpcol@lastpage} = false$, each of $\kappa_c(\beta^b)$ has ship-out image even if some or all of them are empty. It is unnecessary to be aware of the perfectly empty case because it should mean the page p_t is made blank intentionally.
- (2) If $\ text{ifpcol@lastpage} = true but \\ text{ifpcol@dfloats} = true too, the last page must have$ full size because we will have parallel columned pages having float columns for deferred

floats. However, if the page has nothing, i.e., $\pi^i(p_t) = \pi^f(p_t) = \bot$ and $V'_P = -\infty$, we must let \@outputbox = \bot (and \pcol@rightpage = \bot as well) to avoid an unnecessary blank page is shipped out. On the other hand, if $\pi^i(p_t) \neq \bot$ or $\pi^f(p_t) \neq \bot$ while $V'_P = -\infty$, we build a full size page as usual but letting \@textbottom = \vfil temporarily to avoid underfull in the process of building columns. Note that if $\pi^f(p_t) \neq \bot$, the page-wise footnotes are always put into \@outputbox regardless \ifpcol@mgfnote because the last page is not combined with post-environment stuff.

- (3) If $ifpcol@lastpage = true, \\ifpcol@dfloats = false and <math>V'_P = -\infty$, we have to let \@outputbox = \perp unless $\pi^i(p_t) \neq \perp$ or $\pi^f(p_t) \neq \perp$ having non-merged footnotes. If $\pi^f(p_t)$ has non-merged footnotes, \@outputbox and \pcol@rightpage must have $\pi^f(p_t)$ possibly with $\pi^i(p_t)$ but without any columns, and must be put into the main vertical list as the leading part of post-environment stuff by modifying $V'_P = 0$. On the other hand $\pi^f(p_t) = \perp$ or it has merged footnotes, \@outputbox must have only $\pi^i(p_t)^{208}$. Since page-wise floats become ordinary floats in post-environment stuff, we cannot paint its background and must remove \dbltextfloatsep at the bottom of $\pi^i(p_t)$.
- (4) If ifpcol@lastpage = true, ifpcol@dfloats = false and $V'_P > -\infty$, @outputpage and pcol@rightpage must have short columns of V'_P tall, together with $\pi^i(p_t)$ as in non-last pages but without $\pi^f(p_t)$ if it has merged footnotes.

To implement a part of special cares above, we at first let \if@tempswa = true iff \ifpcol@ lastpage = false, $V'_P > -\infty$ or $\pi^f(p_t) \neq \bot$.

- 1709 \def\pcol@makeflushedpage#1{%
- 1710 \pcol@cleartrue \pcol@output@switch \pcol@clearfalse
- 1711 \pcol@getcurrpinfo{\global\c@page}{\global\@colht}\@tempskipa
- 1712 \ifpcol@lastpage \@tempswafalse \else \@tempswatrue \fi
- 1713 \ifdim\pcol@colht=-\maxdimen\else \@tempswatrue \fi
- 1714 \ifvoid\pcol@footins\else \@tempswatrue \fi

Next, if ifpcol@nospan = true to mean the page p_t does not have spanning stuff in $\pi^i(p_t)$, we initialize both \@outputbox and \pcol@rightpage to be \perp . Otherwise, after letting if@tempswa = true if ifpcol@dfloats = true to make the last page full size if we are workingon it as discussed in (2), we put $\pi^i(p_t)$ in \Coutputbox, and paint its background by \pcol@bg@ paintbox $\$ being the height parameter $\$ pcol@bg@floatheight with h being the heightplus-depth of $\pi^i(p_t)$ with the following two exceptions; one is the case of ifpcol@firstpage =true to mean we are in starting page and thus the spanning stuff is pre-environment stuff having already been painted by pcol@output@start; and the other is the case of if@tempswa = falseto mean we are working on a truly last page being empty except for the spanning stuff itself and thus the page-wise floats become a part of deferred floats in post-environment stuff as discussed in (3). In the latter exceptional case, excluding the case that the last page is also the starting page²⁰⁹, we also remove the last skip being \dbltextfloatsep so that those floats are naturally connected with other floats given in post-environment stuff also as discussed in (3). Then we pack the Qoutputbox in itself by vbox so that any stretch/shrink factors in it cannot affect the ship-out image especially when we paint its background²¹⁰. Then we do the similar procedure for \pcol@rightpage and make its height and depth equal to those of $\content box^{211}$. Finally we temporarily add h to \topmargin as done in $\pcol@ioutputelt$

²⁰⁸\pcol@rightpage must have the counterpart in right parallel-page if the spanning stuff is pre-environment stuff, while it is made \perp by \pcol@output@end if the spanning stuff are page-wise floats.

²⁰⁹Extremely exceptional because the closing environment does not have anything.

²¹⁰Though that hardly happens.

²¹¹If page-wise floats become a part of post-environment stuff's floats, \pcol@rightpage will be made \perp by \pcol@output@end afterward.
so that background painting of columns and so on with infinite extension can reach the paper top edge.

1715	\begingroup
1716	\ifpcol@nospan
1717	\global\setbox\@outputbox\box\voidb@x
1718	\global\setbox\pcol@rightpage\box\voidb@x
1719	\else
1720	\ifpcol@dfloats \@tempswatrue \fi
1721	\let\@elt\relax
1722	\edef\pcol@bg@floatheight{%
1723	<pre>\@elt{\number\ht\pcol@spanning sp}\@elt{\number\dp\pcol@spanning sp}}%</pre>
1724	\def\reserved@a{%
1725	\ifpcol@firstpage\else \if@tempswa \pcol@bg@paintbox{Ff}\fi\fi}%
1726	\@tempdima\ht\pcol@spanning \advance\@tempdima\dp\pcol@spanning
1727	\global\setbox\@outputbox%
1728	\reserved@a \unvbox\pcol@spanning
1729	\ifpcol@firstpage\else \if@tempswa\else \unskip \fi\fi}%
1730	\global\setbox\@outputbox\vbox{\box\@outputbox}%
1731	\pcol@Fb
1732	\@cons\@freelist\pcol@spanning
1733	\pcol@Fe{makeflushedpage(spanning)}%
1734	\ifnum\pcol@ncolleft<\pcol@ncol
1735	\global\setbox\pcol@rightpage%
1736	\ifpcol@paired\else \advance\c@page\@ne \fi
1737	\reserved@a \unvbox\pcol@rightpage}%
1738	\global\ht\pcol@rightpage\ht\@outputbox
1739	\global\dp\pcol@rightpage\dp\@outputbox
1740	\global\setbox\pcol@rightpage\vbox{\box\pcol@rightpage}%
1741	\fi
1742	\advance\topmargin\@tempdima
1743	\fi

Next, after \globally letting \ifpcol@firstpage = false because we will ship a page which may be the starting page shortly, we build the ship-out image of columns if required fundamentally by \if@tempswa = true. First, if the page p_t has page-wise footnotes, we shrink \@colht = $\pi^h(p_t)$ by \pcol@shrinkcolbyfn to keep the room for the footnotes, to have $H = \@pageht$ being the possibly shrunk $\pi^h(p_t)$ for the reference in \pcol@imakeflushedpage after the further possible modification of \@colht we will make shortly. Second, if \ifpcol@lastpage = true but \ifpcol@dfloats = true too, we turn \ifpcol@lastpage = false because we need a full-sized last page, temporarily letting \@textbottom = \vfil if $V'_P = -\infty$ to avoid underfull due to perfectly empty column-pages as discussed in (2)²¹². Third, if we are working on a truly last page and $\langle ht \rangle < H$ to mean the tallest column is shorter than H, we let \@colht = $\langle ht \rangle$ to let \@makecol build short column-pages. Note that it is definitely $\langle ht \rangle \leq H$ because the pre-flushing column height check on the last page makes that sure. Fourth and finally, unless all columns in truly last page are empty as discussed in (3), we invoke \pcol@imakeflushedpage $\langle C^0 \rangle \langle C^1 \rangle \langle b \rangle$ once or twice, to put columns in right parallelpage to $b = \pcol@rightpage with [C^0, C^1] = [C_L, C)$ if $C_L < C$, and then to put left ones in $b = \@outputbox with [C^0, C^1] = [0, C_L)$ always²¹³.

1744 \global\pcol@firstpagefalse

²¹²Each column-page $cc_c(\beta^b)$ itself exists because the empty column-page has been visited by column-scan prior to **\output** request for environment closing.

²¹³The order of right to left is not essential in this macro but we follow the convention in \pcol@outputelt.

```
1745
        \if@tempswa
          \ifvoid\pcol@footins\else
1746
            \pcol@shrinkcolbyfn\@colht\pcol@footins\relax
1747
          \fi
1748
          \let\pcol@@hfil\relax \@pageht\@colht
1749
          \ifpcol@lastpage \ifpcol@dfloats
1750
            \ifdim\pcol@colht<\z@ \def\@textbottom{\vfil}\fi
1751
            \pcol@lastpagefalse
1752
1753
          \fi\fi
          \ifpcol@lastpage \ifdim#1<\@colht \@colht#1\fi\fi
1754
          \ifdim\@colht<\z@ \else
1755
            \ifnum\pcol@ncolleft<\pcol@ncol
1756
               \pcol@imakeflushedpage\pcol@ncolleft\pcol@ncol\pcol@rightpage
1757
            \fi
1758
            \pcol@imakeflushedpage\z@\pcol@ncolleft\@outputbox
1759
1760
          \fi
        \fi
1761
```

After putting all column-pages, we examine if the page p_t has page-wise footnotes in $\pi^f(p_t)$. If so, and unless p_t is a truly last page and merged footnote typesetting is in effect to mean the page-wise footnotes will be merged with post-environment stuff, we put the footnotes in $\pi^f(p_t)$ below the column-pages. Prior to this however, we let $\col@fnheight@lpage$ have the height-plus-depth of the footnote, so that $\col@output@end$ know the size for the background painting of the footnotes, which $\col@imakeflushedpage$ performed for non-last pages. We also put an empty box of the size into $\col@col@rightpage$ by $\col@phantom$ together with the \skip component of $\pi^f(p_t)$ to keep the space necessary especially when p_t is the last page. Then we put the footnotes in $\pi^f(p_t)$ into $\col@colputfootins$, reclaiming the contents of $\pi^f(p_t)$ and letting $\pi^f(p_t) = \bot$ so that $\col@colputfootins$, reclaiming the footnotes. We also let $V'_P = \col@colht = 0$ if p_t is a truly last page and it had $-\infty$ to indicate that the last page is not empty but has footnotes as discussed in (3).

1762	\gdef\pcol@fnheight@lpage{0pt}%
1763	\ifvoid\pcol@footins\else
1764	\@tempswatrue \ifpcol@lastpage \ifpcol@mgfnote \@tempswafalse \fi\fi
1765	\if@tempswa
1766	\pcol@Log\pcol@makeflushedpage{output}\pcol@footins
1767	\@tempdima\ht\pcol@footins \advance\@tempdima\dp\pcol@footins
1768	\xdef\pcol@fnheight@lpage{\number\@tempdima sp}%
1769	\ifnum\pcol@ncolleft<\pcol@ncol
1770	\global\setbox\pcol@rightpage\unvbox\pcol@rightpage
1771	\vskip\skip\pcol@footins \nointerlineskip
1772	\pcol@phantom\pcol@footins \vskip\z@}%
1773	\fi
1774	\global\setbox\@outputbox%
1775	\unvbox\@outputbox \pcol@putfootins\pcol@footins}%
1776	\pcol@Fb
1777	\@cons\@freelist\pcol@footins \gdef\pcol@footins{\voidb@x}%
1778	\pcol@Fe{makeflushedpage(pagefn)}%
1779	\ifdim\pcol@colht=-\maxdimen \global\pcol@colht\z@ \fi
1780	\fi
1781	\fi
1782	\endgroup}
1783	

 \collimateflushedpage The macro $\collimateflushedpage \langle C^0 \rangle \langle C^1 \rangle \langle b \rangle$ is invoked solely in \collimateflushedpage

but can be twice with $(C^0, C^1, b) = (C_L, C, \pcol@rightpage)$ if parallel-paging is in effect and with $(C^0, C^1, b) = (0, C_L, \ensuremath{\colored{charge}})$ always, to build the ship-out image of the right or left parallel-page p_t in the box b already having spanning stuff or its blank counterpart if any, respectively.

After opening the $\begin{subarray}{ll} \label{eq:subarray} After opening the <math>\begin{subarray}{ll} \label{eq:subarray} After opening the <math>\begin{subarray}{ll} \begin{subarray}{ll} \begin{subarray}$

Next, we invoke $\col@buildcolseprule$ for column-separating rule drawing and background painting giving it H in \colht possibly shrunk from $\pi^h(p_t)$ by page-wise footnotes, $[C^0, C^1)$ for the set of columns to be put, and $\colhectmath{\colhectmath{\mathsf{Cmaxdepth}}}$ for non-last pages to paint the backgrounds of columns and column-separating gaps so that those of the last segment reach the page bottom, while for last page we give 0 to let the bottom be the real bottom of the columns. Then we put the painted backgrounds in $\colhectmath{\colhectmath{\mathsf{cmpboxa}}}$ immediately.

```
1784 \def\pcol@imakeflushedpage#1#2#3{\global\setbox#3\vbox{%
      \ifpcol@paired\else\ifnum#1=\z@\else \advance\c@page\@ne \fi\fi
1785
1786
      \ifvoid\pcol@footins\else \ifpcol@lastpage\else
1787
        \def\pcol@bg@footnoteheight{%
          \@elt{\ht\pcol@footins}\@elt{\dp\pcol@footins}}%
1788
        \pcol@bg@paintbox{Nn}%
1789
      \fi\fi
1790
      \unvbox#3\nointerlineskip
1791
      \ifpcol@lastpage \pcol@buildcolseprule\@colht#1#2\z@
1792
1793
      \else
                        \pcol@buildcolseprule\@colht#1#2\@maxdepth
1794
      \fi
1795
      \unvbox\@tempboxa
```

Now we put columns in a **\hbox** of $W_T = \texttt{textwidth}$ wide. That is, for each c, being c' or C-1-c' for the c'-th iteration determined by **\pcol@swapcolumn** according to the effectiveness of column-swapping and the parity of $page(p_t)$, we obtain c's column-context κ_c by **\pcol@getcurrcol**, move $\kappa_c(\beta^b)$ into **\box255**, and let **\footins** = $\kappa_c(\tau)$ by **\pcol@getcurrfoot** returning it to **\@freelist** if c has column-wise footnotes.

After that we examine if $\kappa_c(\rho_t) = \infty$ to mean we are working on the last page and the column-page is for a float column whose floats can be put as top floats, and let \topfigrule = \relax temporarily because the floats are not top ones in reality, if so. Note that the abnormal setting $\kappa_c(\rho_t) = \infty$ is not recovered because it will never be referred to and the register \@toproom it represents will be updated with correct value before it is referred to in post-environment stuff. Then we also check $\langle ht \rangle = H$ to mean the last page is full size. If both of them hold, the floats in $\kappa_c(\lambda_t)$ should be (or may be) put in the float column as usual and thus we put them in \@outputbox of H tall by \pcol@makefcolpage. Otherwise we invoke \pcol@makecol²¹⁴, to have the ship-out image of the column-page in \@outputbox, possibly only for the deferred floats in $\kappa_c(\lambda_t)$ but without \topfigrule in this case. Note that we don't take care of the stretch/shrink of \skip\footins for page-wise footnotes because pre-flushing column height check on the column-page makes it sure that the natural height of the column-

²¹⁴Not \pcol@makecol because the main vertical list has \vfil and, if it has a synchronization point, a infinite shrink by \pcol@synccolumn at its tail already, and we should not do any special operations for page-wise footnotes. Also it is not \@makecol because we need to ensure the depth of resulting \@outputbox is capped.

page cannot be greater than \@colht. Also note that we give \@maxdepth to \pcol@@makecol for non-last pages for depth capping, but for the last page we pass 0 to the macro because H = \@colht should be large enough to accommodate everything in the column including its last box even if the box is unusually deep.

Then we put the \Coutputbox above in a \hbox of \columnwidth wide preceded by \pcolCC hfil being \relax for the first column, while it is $\colonfil(c^g)$, where $c^g = \colocolsepid$ being c or c-1 without or with column-swapping respectively, to put a column-separating gap possibly with column-separating rule segments in \pcol@tempboxa built by \pcol@ buildcolseprule. Finally, we save column-context especially those for float parameters into κ_c by \pcol@setcurrcolnf because all column-wise footnotes have been shipped out.

```
1796
      \hb@xt@\textwidth{%
        \@tempcntb#1\@whilenum\@tempcntb<#2\do{%
1797
          \pcol@swapcolumn\@tempcntb\pcol@currcol#1#2\relax
1798
          \pcol@getcurrcol
1799
1800
          \setbox\@cclv\box\@currbox
1801
          \ifvoid\pcol@currfoot\else
1802
            \pcol@Fb
            \@cons\@freelist\pcol@currfoot
1803
            \pcol@Fe{imakeflushedpage(colfn)}%
1804
          \fi
1805
          \pcol@getcurrfoot\box
1806
          \@tempswafalse
1807
1808
          \begingroup
            \ifdim\@toproom=\maxdimen
1809
               \let\topfigrule\relax \ifdim\@colht=\@pageht \@tempswatrue \fi
1810
            \fi
1811
            \if@tempswa
1812
              \pcol@Logstart{\pcol@makeflushedpage(1)}%
1813
              \setbox\@outputbox\pcol@makefcolpage
1814
              \pcol@Logend{\pcol@makeflushedpage(1)}%
1815
1816
            \else
              \pcol@Logstart{\pcol@makeflushedpage(2)}%
1817
              \ifpcol@lastpage \pcol@@makecol\z@ \else \pcol@@makecol\@maxdepth \fi
1818
              \pcol@Logend{\pcol@makeflushedpage(2)}%
1819
            \fi
1820
            \pcol@@hfil \hb@xt@\columnwidth{\box\@outputbox\hss}%
1821
1822
          \endgroup
          \edef\pcol@Chfil{\noexpand\pcol@hfil{\pcol@colsepid}}%
1823
          \pcol@setcurrcolnf
1824
         \advance\@tempcntb\@ne}}}
1825
1826
```

\pcol@flushfloats The macro \pcol@flushfloats is invoked from \pcol@output@clear and \pcol@output@ $\colorightarrow barbon barbo$ \textheight for float columns, we iterate shipping out a page having float columns while $\texttt{if@fcolmade} = \exists c \in [0, C) : (\kappa_c(\lambda_d) \neq ()).$

In the loop, we initialize $\formation{de} = false$, and then invoke $\col@iflushfloats$ twice or once according to $C_L < C$ or not to mean parallel-paging is in effect or not, respectively. That is, if $C_L < C$ we invoke the macro with $[C_L, C)$ and \pcol@rightpage for the right parallel-page, and do it with $[0, C_L)$ and **\Coutputbox** always. Note that if $C_L = C$, we let $\colletinghtpage = \bot$ to tell \colletinghtpage , which we invoke at the end of the loop to ship

out a page or a parallel-page pair, that the parallel-paging is not in effect.

The macro $\colorightarrow colorightarrow constraints (C⁰) (C¹) (b) opens a \vbox to be set into b. Then if$ $\ifpcol@paired = false and C⁰ > 0 to mean we are working on a right non-paired parallel$ $page, we temporarily add \c@page by one for page parity examination for mirrored background$ $painting. Then, the macro \pcol@buildcolseprule is invoked with \@colht = \textheight$ $and [C⁰, C¹) for column-separating rule drawing in \pcol@tempboxa and background painting$ $for columns and column-separating gaps in \@tempboxa put into b immediately.$

Then we open a **\hbox** of **\textwidth** wide and initialize $f = \if @tempswa$ to be $\if @fcolmade$. Then for each $c \in [C^0, C^1)$, being c' or C - 1 - c' for the c'-th iteration determined by $\pcol@swapcolumn$ according to the effectiveness of column-swapping and the parity of $\c@page$, we put an inner \hbox of $\columnwidth = w_c$ wide preceded by $\pcol@$ $\column-separating rule, where <math>c_g \in \{c, c-1\}$ without or with column-swapping respectively. That is, at first we obtain c's column-context including $\kappa_c(\lambda_d)$ by $\pcol@getcurrcol and pass <math>\kappa_c(\lambda_d)$ to \mbox . Then we do $f \leftarrow f \lor (\kappa_d(\lambda_d) \neq \emptyset)$ with $\kappa_d(\lambda_d)$ shrunk by $\mbox{makefcolumn}$ to let f have $\exists c \in [0, C^1) : (\kappa_c(\lambda_d) \neq \emptyset)$ at the end of the loop for c, and then save the column-context into κ_c by $\pcol@setcurrcolnf$ because we have no footnotes in c.

After the end of the loop, we move f to if@fcolmade for the termination check of the loop in pcol@flushfloats.

```
1827 \def\pcol@flushfloats{%
      \global\@colht\textheight
1828
      \@whilesw\if@fcolmade\fi{%
1829
1830
        \global\@fcolmadefalse
        \ifnum\pcol@ncolleft<\pcol@ncol
1831
          \pcol@iflushfloats\pcol@ncolleft\pcol@ncol\pcol@rightpage
1832
1833
        \else
1834
          \setbox\pcol@rightpage\box\voidb@x
1835
        \fi
        \pcol@iflushfloats\z@\pcol@ncolleft\@outputbox
1836
1837
        \@outputpage}}
1838 \def\pcol@iflushfloats#1#2#3{\setbox#3\vbox{%
      \ifpcol@paired\else\ifnum#1=\z@\else \advance\c@page\@ne \fi\fi
1839
      \pcol@buildcolseprule\@colht#1#2\@maxdepth \unvbox\@tempboxa
1840
      \hb@xt@\textwidth{%
1841
1842
        \let\pcol@@hfil\relax
1843
        \if@fcolmade \@tempswatrue \else \@tempswafalse \fi
1844
        \@tempcntb#1\@whilenum\@tempcntb<#2\do{%
1845
          \pcol@swapcolumn\@tempcntb\pcol@currcol#1#2\relax
1846
          \pcol@getcurrcol
1847
          \@makefcolumn\@deferlist
          \pcol@Chfil \hb@xt@\columnwidth{%
1848
            \if@fcolmade \box\@outputbox \else \vbox to\@colht{}\fi \hss}%
1849
          \ifx\@deferlist\@empty\else \@tempswatrue \fi
1850
1851
          \edef\pcol@dhfil{\noexpand\pcol@hfil{\pcol@colsepid}}%
1852
          \pcol@setcurrcolnf
1853
         \advance\@tempcntb\@ne}%
1854
        \if@tempswa \global\@fcolmadetrue \else \global\@fcolmadefalse \fi}}}
1855
```

\pcol@freshpage The macro \pcol@freshpage is invoked from \pcol@output@flush and \pcol@output@clear to start a new page after column flushing. At first, we let $p = p_b = p_t = 0$ and $\Pi = \emptyset$ because we know no pages are kept. Then we invoke $\col@startpage$ to start a new page with a $\definition of \pcol@currpage = {} to indicate the invoker is this macro (i.e., not <math>\pcol@opcol$). Then after keeping \colht in $h = \pcol@colht$, we do the followings for each column $c \in [0, C)$.

First we obtain c's column-context in κ_c by \pcol@getcurrcol but let p = 0 and \@colroom = h, which can be modified by c' < c, without referring to $\kappa_c(\beta^p)$ nor $\kappa_c(\beta^r)$ because they are obsolete. We also save \@currbox to \pcol@currboxsave because it may be modified by \pcol@opcol if we make float columns afterward. Then we invoke \pcol@getcurrpage to have the page context of p = 0, because it might be modified by a column c' < c by producing float columns. After that and the invocation of \pcol@floatplacement for setting float parameters, we invoke \pcol@startcolumn for c's column-page at p = 0, and iterate \pcol@opcol and \pcol@startcolumn while a float column is made by the latter²¹⁵. Note that we give the argument 0 to each invocation of \pcol@startcolumn to keep it from inserting deferred page-wise footnotes, which will be taken care of by \pcol@restartcolumn if any. At last in the loop, we restore \@currbox from \pcol@currboxsave, let $\kappa_c(\beta^b)$ be an empty \vbox because the main vertical list is empty, and save the column-context into κ_c by \pcol@setcurrcolnf because of no footnotes obviously, after saving p and \@colroom, which might be modified by the float column production, into $\kappa_c(\beta^p)$ and $\kappa_c(\beta^r)$.

After the loop above, finally we invoke \pcol@restartcolumn to return to the column in which \flushpage or \clearpage was issued.

```
1856 \def\pcol@freshpage{%
1857
      \global\pcol@page\z@ \global\pcol@toppage\z@ \global\pcol@basepage\z@
1858
      \global\let\pcol@pages\@empty \global\let\pcol@currpage\@empty
1859
      \pcol@startpage \pcol@colht\@colht
      \pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do{%</pre>
1860
        \pcol@getcurrcol \pcol@page\z@ \@colroom\pcol@colht
1861
        \let\pcol@currboxsave\@currbox
1862
1863
        \pcol@getcurrpage
1864
        \pcol@floatplacement
1865
        \pcol@startcolumn\z@
        \@whilesw\if@fcolmade\fi{\pcol@opcol \pcol@startcolumn\z@}%
1866
        \let\@currbox\pcol@currboxsave
1867
```

```
1868 \global\setbox\@currbox\vbox{}%
```

```
1869 \global\count\@currbox\pcol@page \global\dimen\@currbox\@colroom
```

```
1870 \pcol@setcurrcolnf
```

```
1871 \advance\pcol@currcol\@ne}%
```

```
1872 \pcol@restartcolumn}
```

```
1873
```

11.9 Last Page

Next, we define $\mathcal{M} = \text{pcol@mparbottom@out}$ as follows. First, we invoke \pcol@ getmparbottom@last giving it $y = V'_P - \text{ht}@outputbox}$ being the negative counterpart of the height of spanning stuff in the last page, to let \mathcal{M} have the occupancy information of the

 $^{^{215}}$ Each column can have deferred floats on the invocation from \pcol@output@flush.

bottom marginal note in each margin if any, or mpar(y, y) otherwise. Then we transform ycoordinates in \mathcal{M} from those for columns to those for text area by \pcol@bias@mpbout{-y} to have the final result. Then to pass \@mparbottom for post-environment typesetting, we invoke \pcol@do@mpbout \defining \pcol@do@mpbout@whole to do nothing and \pcol@do@mpbout@ elem to let \@mparbottom = b where $M_L^x = (mpar(t, b))$ and $x \in \{l, r\}$ according to the margin which post-environment marginal notes go to.

1874 %% Special Output Routines: Last Page

- 1875
 1876 \def\pcol@output@end{%
- 1877 \pcol@Logstart\pcol@output@end
- 1878 \pcol@makeflushedpage\pcol@colht
- 1879 \@tempdima\pcol@colht \ifdim\pcol@colht<\z@ \@tempdima\z@ \fi
- 1880 \advance\@tempdima-\ht\@outputbox
- 1881 \pcol@getmparbottom@last\@tempdima
- 1882 \pcol@bias@mpbout{-\@tempdima}
- 1883 \def\pcol@do@mpbout@whole##1##2##3##4{\setbox\@tempboxa\hbox{##1##2##3##4}}%
- 1884 \def\pcol@do@mpbout@elem\@elt##1##2{\global\@mparbottom##2sp}%
- 1885 \pcol@do@mpbout

Next we process one of the following cases.

The first case is for ifpcol@dfloats = true to mean the last page is followed by one or more pages having deferred column-wise floats and thus pcol@makeflushedpage builds the ship-out image of the last page in *full size* in @outputbox unless the page has nothing perfectly. Therefore, we ship the image out by @outputbox unless it is \perp for perfectly empty case. Then we invoke pcol@flushfloats to produce and ship out float pages, letting if@fcolmade =*true* to tell the macro that at least we will have one float page. Now we have shipped out everything in the closing environment and thus we let ifpcol@output = false to tell outputroutine to work ordinarily. Then we let $if@tempswa = f_{sp} = true$ to remember we will start a new page and thus $@pagedp = \delta = D_P = 1000$ to mimic T_EX 's prevdepth mechanism. Finally we let @mparbottom = 0 and $\mathcal{M} = \mathcal{M}_0$ because no marginal notes are carried over to post-environment typesetting.

- 1886 \@tempswafalse
- 1887 \ifpcol@dfloats
- 1888 \ifvoid\@outputbox\else \@outputpage \fi
- 1889 \global\@fcolmadetrue \pcol@flushfloats
- 1890 \global\pcol@outputfalse
- 1891 \@tempswatrue \@pagedp\@m\p@ \global\@mparbottom\z@
- 1892 \global\let\pcol@mparbottom@out\pcol@mparbottom@zero

Before proceeding to the second and third cases, we let $\ifpcol@output = false$ because we have nothing to ship out.

Then the second case is for $h = -\infty$ without deferred column-wise floats to mean all columns in the last page are empty and the page does not have non-merged page-wise footnotes. In this case, we examine if \pcol@firstprevdepth = \relax to mean we have had at least one new page in paracol environment, i.e., \pcol@startpage have been invoked at least once. If so, we let $f_{sp} = true$, $\delta = 1000$, \@mparbottom = 0 and $\mathcal{M} = \mathcal{M}_0$ again and put nothing to the main vertical list so that the post-environment stuff starts from the top of the page. However, we have to take care of the case that $f_{ns} = false$ and thus \@outputbox has spanning stuff. If so, we acquire an \insert from \@freelist by \@next to let it have the spanning stuff, i.e., the contents of \@outputbox²¹⁶. Then the \insert is added to the head of \@dbldeferlist

 $^{^{216}}$ It does not have \dbltextfloatsep at its tail because the skip has been removed by \pcol@makeflushedpage.

with the float placement code 10 to force LATEX's float placement mechanism to put it to the page to be started shortly.

On the other hand, $\col@firstprevdepth \neq \relax means that it has <math>\prevdepth = \delta'$ just before $\begin{paracol} in decimal integer representation. Since we have not started any$ pages in the environment, and all columns in the last page is empty, we have almost nothingin the environment. Note that the environment can have page-wise floats but they have not $yet put into any pages but are kept in <math>\col@bldeferlist$, or merged footnotes but they are merged to those in post-environment stuff. Therefore, the pre-environment stuff and postenvironment stuff must be *connected* naturally and thus we put the pre-environment stuff kept in $\col@outputbox$ to the main vertical list by \unvbox , letting $\delta = \delta'$ and keeping $f_{sp} = false^{217}$. In this case, the setting of $\mbox{marbottom}$ and \mathcal{M} done at the beginning of this macro is correct because they describe the marginal notes in pre-environment stuff including paracol environments preceding it even if any.

1893	\else
1894	\global\pcol@outputfalse
1895	\ifdim\pcol@colht=-\maxdimen
1896	\ifx\pcol@firstprevdepth\relax
1897	\@tempswatrue \@pagedp\@m\p@ \global\@mparbottom\z@
1898	\global\let\pcol@mparbottom@out\pcol@mparbottom@zero
1899	\ifpcol@nospan\else
1900	\pcol@Fb
1901	\@next\@currbox\@freelist{\global\setbox\@currbox\box\@outputbox}%
1902	\pcol@ovf
1903	\pcol@Fe{output@end(spanning)}%
1904	\count\@currbox10\relax
1905	{\let\@elt\relax \xdef\@dbldeferlist{\@elt\@currbox\@dbldeferlist}}%
1906	\global\setbox\pcol@rightpage\box\voidb@x
1907	\fi
1908	\else \unvbox\@outputbox \@pagedp\pcol@firstprevdepth sp\relax
1909	\fi

The last case without deferred floats and with some non-empty columns or non-merged pagewise footnotes is most usual. In this case, we may simply put \@outputbox letting \topskip = 0 because \topskip has already been inserted in column-pages or pre-environment stuff in the box²¹⁸.

However before putting the box back to the main vertical list, we have to take care of the background painting as follows. First we let $\ifpcol@havelastpage = true$ to let $\@outputpage$ paint the background of the post-environment stuff when the page having the last page completes. Second, we let $\pcol@bg@preposttop@left$ have the height-plus-depth of the $\@outputbox$ having the short last page because the background of post-environment stuff, or of pre-environment stuff if we have another paracol environment in the same page, to be painted is just below the box. We also $\pcol@bg@preposttop@right$ have the same value but only if $C_L < C$, because otherwise we have to keep this macro unchanged so that the non-existent right parallel-page of the closing environment stuff of a succeeding one with parallelpaging. Note that in the aforementioned *fresh page* cases and the perfectly empty case, we may be unaware of these macros because it should have been made 0 by the last invocation of $\@outputpage$ in the fresh page case or the pre-environment stuff and post-environment stuff are contiguous in the empty case.

²¹⁷The author of course know this situation is very unlikely but he is monomaniac.

 $^{^{218}}$ If the last page has non-merged page-wise footnotes without any other items, **\topskip** has not been inserted, but this inconsistency without **\topskip** is acceptable.

Third and finally, we have to paint the background of non-merged page-wise footnotes because the painting is left by $\col@makeflushedpage$ for this macro. Therefore, if $\col@fnheight@lpage > 0$ to mean we have footnotes whose total height-plus-depth is in the macro, we paint their background by $\col@bg@paintbox \defining \pcol@bg@$ $footnoteheight with the size and temporarily re\defining <math>\col@bg@textheight$ to be the height-plus-depth of \coutputbox because the footnotes are at the bottom of the box instead of the page. Note that the order of painting is right first and then left second if we have parallelpages because we refer the height-plus-depth of \coutputbox being put into the main vertical list making the box \perp . Also note that if the right parallel-page is non-paired, we temporarily increment $\col@age in \col@cl@tputbox because to let \col@bg@paintbox handle infinite extension$ $to side margins correctly. Another remark is that we don't modify <math>\delta = \col@agedp$ and thus it keeps D_P in this case, and f_{sp} is kept false.

1910	\else
1911	\global\pcol@havelastpagetrue
1912	\@tempdima\ht\@outputbox \advance\@tempdima\dp\@outputbox
1913	\xdef\pcol@bg@preposttop@left{\number\@tempdima sp}%
1914	\ifnum\pcol@ncolleft<\pcol@ncol
1915	\global\let\pcol@bg@preposttop@right\pcol@bg@preposttop@left
1916	\fi
1917	\def\pcol@bg@textheight{\@elt{\ht\@outputbox}\@elt{\dp\@outputbox}}%
1918	\def\reserved@a{%
1919	\ifdim\pcol@fnheight@lpage>\z@
1920	\def\pcol@bg@footnoteheight{\@elt\pcol@fnheight@lpage}%
1921	\pcol@bg@paintbox{Nn}%
1922	\fi}%
1923	\ifnum\pcol@ncolleft<\pcol@ncol
1924	\global\setbox\pcol@rightpage%
1925	\ifpcol@paired\else \advance\c@page\@ne \fi
1926	\reserved@a \unvbox\pcol@rightpage}%
1927	\fi
1928	\topskip\z@ \vbox{\reserved@a \unvbox\@outputbox}%
1929	\fi
1930	\fi

Now we have put almost everything in the last page but we may still have page-wise footnotes in $\pi^f(p_t)$ to be merged with those in post-environment stuff. Therefore, we **\insert** them through **\footins** as a part of post-environment stuff, and then do that for deferred footnotes in $\Phi = \col@topfnotes$ without using **\pcol@deferredfootins** because we don't need the height capping.

```
1931 \ifvoid\pcol@footins\else
```

```
1932 \pcol@Log\pcol@output@end{insert}\pcol@footins
```

```
1933 \pcol@Fb
```

```
1934 \insert\footins{\unvbox\pcol@footins}\@cons\@freelist\pcol@footins
```

1935 \pcol@Fe{output@end(pagefn)}%

```
1936 \fi
```

1937 \ifvoid\pcol@topfnotes\else \insert\footins{\unvbox\pcol@topfnotes}\fi

The following operations are for clean-up and set-up for the post-environment stuff; for all c, return $\kappa_c(\beta)$ obtained by \pcol@getcurrcol and $\gamma_0^c \neq \bot$ letting it \bot to \@freelist; reestablish the color stack by \pcol@restorecolorstack for column-0²¹⁹ so that the color stack is just Γ and is rewound at \end{paracol}, and let $\Gamma = \bot$; reload κ_d for $d = \col@lastcol being the column in which \end{paracol} ccurs to let \everypar = <math>\kappa_d(\varepsilon)$ and to let \if@nobreak

 $^{^{219}}$ It can be any other column.

and \if@afterindent have the value represented by $\kappa_d(\sigma)$, so that the first paragraph of the post-environment stuff is typeset following them²²⁰; let \pcol@prevdepth = δ so that it is set to prevdepth by pcol@invokeoutput; let $@colht = @colroom = \\textheight$ to mean the single-column page does not have any floats so far because those produced in or before the environment have already been shipped out, are put to the main vertical list packed in \Coutputbox, or are in \Cdbldeferlist.

As for deferred page-wise floats produced in the environment, including those once put in the last page but returned to the list by the operation described above, we move them to \@deferlist because they are now column-wise floats. Then we invoke \pcol@ floatplacement to reinitialize float placement parameters. Finally, if $f_{sp} = true$, we invoke \@startcolumn and then repeat invocations of \@opcol and \@startcolumn while float pages are produced, after letting $\ false to make \ combinefloats work$ as $\[AT_{F}X'\]$'s original²²¹.

```
\pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do{%</pre>
1938
1939
        \pcol@Fb
        \pcol@getcurrcol \@cons\@freelist\@currbox
1940
        \ifvoid\pcol@ccuse{@box}\else
1941
1942
          \@cons\@freelist{\pcol@ccuse{@box}}%
          \pcol@ccxdef{\voidb@x}%
1943
1944
        \fi
        \pcol@Fe{output@end(col)}%
1945
1946
       \advance\pcol@currcol\@ne}%
1947
      \pcol@currcol\z@ \pcol@restorecolorstack
1948
      \global\setbox\pcol@colorins\box\voidb@x
1949
      \pcol@currcol\pcol@lastcol\relax \pcol@getcurrcol
      \global\pcol@prevdepth\@pagedp
1950
      \global\@colht\textheight
1951
      \global\@colroom\textheight
1952
      \global\let\@deferlist\@dbldeferlist \gdef\@dbldeferlist{}%
1953
      \pcol@floatplacement
1954
      \pcol@lastpagefalse
1955
      \if@tempswa
1956
1957
        \@startcolumn \@whilesw\if@fcolmade\fi{\@opcol\@startcolumn}%
1958
      \fi
      \pcol@Logend\pcol@output@end
1959
1960 }
1961
```

12**Starting Environment**

\pcol@invokeoutput Before giving the definition of paracol environment and commands used in it, we define the macro $\pcol@invokeoutput(pen)$ invoked from them to make an \output -request with **\penalty** of $\langle pen \rangle = \mathbf{pcol@op@} f$. The macro's structure is similar to that for the request sequence in $\end{@float}$ as follows; insert a \penalty of -10004 to save the main vertical list in \Choldpg; save \prevdepth; insert a \vbox to make it sure the following \penalty of $\langle pen \rangle$ is kept even when we are at the top of a page; and finally restore \prevdepth.

> A difference is that we zero-clear $\ \$ because it can be reach $\$ maxdeadcycles = 100 easily if a page has many synchronizations and many columns. Another and more important

 $^{^{220}}$ For rare cases that the last item of the closing environment is a sectioning command, but a user has such very unusual usage.

²²¹Letting \pcol@textfloatsep = ∞ is done by \pcol@floatplacement.

difference is in the save/restore of \prevdepth. First, the value of the register is saved in our own \pcol@prevdepth instead of \@tempdima by a \global assignment so that \outputroutine refers to it²²². Second, the value restored to \prevdepth may be different from that we just have saved because \output-routine may update \pcol@prevdepth to have, for example, the value saved in $\kappa_c(\delta)$ when we left from c which we are now restarting.

In addition to above, after the invocation of \output-routine, we let \linewidth = $w_c - \mu$ so that the register is shrunk from w_c by the total width of left and right margins of the list-like environment surrounding paracol if $\mu = \text{pcol@Irmargin} > 0$ to mean that. Then if so, we set \parshape to let every line of paragraphs in the column c is indented by \@totalleftmargin and has width of \linewidth, as IATEX's \list does. We also let \hsize = w_c because it should have the width of the column even in a list-like environment.

The macro is invoked from \pcol@zparacol (f = start), \pcol@switchcol for \switch column and column-switching environments (f = switch), \pcol@visitallcols for column-scan prior to synchronized column-switching and page flushing (f = switch), \pcol@flushclear for pre-flushing column height check (f = switch), \pcol@com@flushpage for \flushpage (f = flush), \pcol@com@clearpage for \clearpage (f = clear), and \endparacol (f = end).

```
1962 %% Starting Environment
1963
1964 \def\pcol@invokeoutput#1{\deadcycles\z@
      \pcol@Logstart{\pcol@invokeoutput
1965
        {#1:\the\pcol@currcol/\the\pcol@nextcol%
1966
1967
         \ifnum#1=-10011:\ifpcol@sync s\fi \ifpcol@clear c\fi\fi}}%
1968
      \penalty-\@Miv \global\pcol@prevdepth\prevdepth \vbox{}%
1969
      \penalty#1\relax \prevdepth\pcol@prevdepth
1970
      \linewidth\columnwidth \advance\linewidth-\pcol@lrmargin
1971
      \ifdim\pcol@lrmargin>\z@ \parshape\@ne\@totalleftmargin\linewidth \fi
1972
      \hsize\columnwidth
      \pcol@Logend{\pcol@invokeoutput{#1}}}
1973
1974
```

```
\paracol The API macro \paracol[C_L][*]{C}[text] is invoked by \begin{paracol} to start a 
\pcol@xparacol paracol environment. The macro simply examines the existence of the optional argument 
\pcol@yparacol C_L, whose default value C is given by \pcol@xparacol, to decide the number of columns in 
\pcol@zparacol left parallel-pages. Then if the optional argument is given, \pcol@yparacol examines the ex-
istence of '*' following it for non-paired parallel-paging to let \ifpcol@paired = false, while 
\paracol gave the default true for paired one to the switch. Then the all other operations to 
start the environment is done by \pcol@zparacol.
```

```
1975 \def\paracol{\global\pcol@pairedtrue \@ifnextchar[%]
1976 \pcol@yparacol\pcol@xparacol}
1977 \def\pcol@xparacol#11{\pcol@zparacol[#1]{#1}}
1978 \def\pcol@yparacol[#1]{%
1979 \@ifstar{\global\pcol@pairedfalse \pcol@zparacol[#1]}%
1980 {\pcol@zparacol[#1]}}
```

In $\clicklinetright product product$

 $^{^{222}}$ The assignment is not necessary to be done \globally but we dare to do it to make all assignments to \pcol@prevdepth being \global consistently.

ifpcol@paired = true regardless the setting in pcol@yparacol</code> because non-paired typesetting is meaningless without parallel-paging. On the other hand, if non-paired typesetting isspecified, we let <math>ifpcol@swapcolumn = false but not globally because column-swapping is meaningless in non-paired mode in the environment now starting.

Second, we perform the operations done by <code>\item if \if@newlist = true</code> and <code>\if@inlabel = false</code> to mean the first one in a <code>list-like</code> environment will appear at the very first line of the leftmost column. That is, we invoke <code>\@nbitem</code> if <code>\if@nobreak = true</code>, or add a penalty <code>\@beginparpenalty</code> and a vertical skip <code>\@topsep-\parskip-\itemsep</code> so that the first <code>\item</code> is <code>\@topsep</code> apart from the last line above the environment, and then let <code>\if@newlist = false</code>. The reason why we do these operations here is that, if the <code>paracol</code> environment is enclosed in a <code>list-like</code> environment without anything between two <code>\begin</code> for environments, we have to align all first <code>\items</code> in all columns. That is, if we did not do that, the *literally first* <code>\item</code> would do that resulting in the column having the <code>\item</code> led by the vertical skip of <code>\@topsep</code> while others should have ordinary inter-<code>\item</code> skips. Therefore, we perform the <code>operations</code> on behalf of all first <code>\items</code> in all columns to have the skip of <code>\@topsep</code> above the <code>paracol</code> environment we are opening. Note that if <code>\begin{paracol}</code> immediately follows a <code>\begin</code> for a <code>trivlist-like</code> environment, <code>\if@inlabel = true</code> because the first <code>\item</code> was given in the opening macro and thus the operations shown above has already been performed.

```
1981 \def\pcol@zparacol[#1]#2{\par
      \ifinner \@parmoderr \fi
1982
1983
      \if@twocolumn \PackageError{paracol}{%
        Environment paracol cannot work with ordinary two-column
1984
        typesetting.}\@ehb\fi
1985
      \global\pcol@ncolleft#1\relax \global\pcol@ncol#2\relax
1986
      \ifnum\pcol@ncolleft>\pcol@ncol \global\pcol@ncolleft\pcol@ncol \fi
1987
      \ifnum\pcol@ncolleft<\pcol@ncol\else \global\pcol@pairedtrue \fi
1988
      \ifpcol@paired\else \pcol@swapcolumnfalse \fi
1989
1990
      \if@newlist \if@inlabel\else
1991
        \if@nobreak \@nbitem
1992
        \else
1993
          \addpenalty\@beginparpenalty
1994
          \addvspace\@topsep
          \addvspace{-\parskip}\addvspace{-\itemsep}%
1995
        \fi
1996
1997
        \global\@newlistfalse
1998
      \fi\fi
```

Next we scan Θ^l applying \pcol@thectrelt to each element $\theta^l \in \Theta^l$ to let \pcol@thectr@ $\theta^l = \begin{subarray}{l} \theta^l & \theta^l & \theta^l \\ \theta^l = \begin{subarray}{l} \theta^l = \begin{subarray}{l} \theta^l & \theta^l & \theta^l \\ \theta^l & \theta^l & \theta^l & \theta^l$

Next we give the initial value of $val_c(\theta^l)$ for each column c and local counter $\theta^l \in \Theta^l$ by the followings enclosed in a group. First we scan Θ_0 applying \pcol@loadctrelt to each $\theta^l \in \Theta'_0 = \{\theta \mid \langle \theta, val_0(\theta) \rangle \in \Theta_0\}$ to have the value $val_0(\theta^l)$ in \colectredel temporarily. Next we scan Θ^l to pick local counters θ such that $val(\theta) \neq val_0(\theta)$ where $val(\theta)$ is the value of θ outside paracol environment, or $\theta \notin \Theta'_0$, to let them be listed in \colectredel the previous paracol, or everything in Θ^l at the first $\colectredel paracol$ because $\Theta_0 = \emptyset^{223}$. Finally, we invoke $\colectede paracol environment to let <math>val_c(\theta) = val(\theta)$ for all c and for each θ in $\colecterede paracol environment appears two or more times, the value of a$ local counter at the beginning of the second or succeeding environment is kept unchanged fromthat at the end of the previous environment, unless it has been updated between them. Note $that these scans above are enclosed in a group in order to make <math>\colectrede \theta^l$ local and thus collected as a garbage at \endgroup .

```
1999
      \global\let\pcol@counters\cl@@ckpt
      \let\@elt\pcol@remctrelt \pcol@gcounters
2000
      \let\@elt\pcol@thectrelt \pcol@counters
2001
2002
      \begingroup
2003
        \let\@elt\pcol@loadctrelt \csname pcol@counters0\endcsname
2004
        \let\@elt\pcol@cmpctrelt \global\let\@gtempa\@empty \pcol@counters
2005
        \pcol@synccounter\@gtempa
      \endgroup
2006
```

Fourth, we set up a few LATEX's typesetting parameters which should have appropriate values in the environment. We let if@twocolumn = true so that *float** environments work for page-wise floats and LaTeX's @addmarginpar</code> determine the margin for marginal notes by<math>if@firstcolumn whose truth value is determined by our own @addmarginpar. We also let col@number = 1 instead of C so that its (almost surely) sole user maketitle will not produce the title with twocolumn which cannot be in the environment.

Then we invoke $\closetcolumnwidth \langle C^0 \rangle \langle C^1 \rangle \langle r \rangle \langle s \rangle$ once or twice with $(C^0, C^1, r, s) = (0, C_L, \closetcolumnratioleft, \closetcolumdthspecieft)$ always for left parallel-page, and with $(C_L, C, \closetcolumnrationight, \closetcolumnwidthspecieft)$ for right one if $C_L < C$ to define column widths $w_c = \closetcolumnwidth c$ and that of column-separating gaps $g_c = \closetcolumnsep c$ for all $c \in [0, C) = [0, C_L) \cup [C_L, C)$.

Then we initialize other variables as follows; $\mu = \col@lrmargin = \textwidth - \linewidth so that, if <math>\mu > 0$, \linewidth for c has $w_c - \mu$ reflecting the paragraph shape of the list-like environment surrounding paracol environment; $\col@topskip = \topskip$ for the second and succeeding pages; $\col@textfloatsep = \infty$ to mean we don't have any synchronization points so far; $\forcel@lastpage = false$ because the starting page is not the last so far; and $\col@firstprevdepth = \prevdepth$ in decimal integer form for the extreme empty case.

We also make the macro $\combinefloats \let-equal to our own \pcol@combinefloats throughout the environment, after saving its original definition into \pcol@combinefloats for processing \output request sneaked from outside of environment, so that our customization is in effect for any invocations including those from LATEX's own macros. Similarly, \@addmarginpar is made \let-equal to our own \pcol@addmarginpar while its original definition is saved into \pcol@Caddmarginpar but in this case we need the original for the implementation of our own. On the other hand, \end@dblfloat is simply replaced with our own \pcol@end@dblfloat being what LATEX had had until 2014 as discussed in item-(1) of §1.8.$

```
2007 \global\@twocolumntrue \col@number\@ne
2008 \pcol@setcolumnwidth\z@\pcol@ncolleft
2009 \pcol@columnratioleft\pcol@colwidthspecleft
```

 $^{^{223}}$ Undefined in fact.

```
2010 \ifnum\pcol@ncolleft<\pcol@ncol
```

```
2011 \pcol@setcolumnwidth\pcol@ncolleft\pcol@ncol
```

```
2012 \pcol@columnratioright\pcol@colwidthspecright
```

2013 \fi

- 2014 \pcol@lrmargin\textwidth \advance\pcol@lrmargin-\linewidth
- 2015 \global\pcol@topskip\topskip
- $2016 \quad \verb+\global\pcol@textfloatsep\maxdimen$
- 2017 \pcol@lastpagefalse \xdef\pcol@firstprevdepth{\number\prevdepth}%
- 2018 \let\pcol@@combinefloats\@combinefloats \let\@combinefloats\pcol@combinefloats
- 2019 \let\pcol@addmarginpar\@addmarginpar \let\@addmarginpar\pcol@addmarginpar
- $2020 \quad \verb+let+end@dblfloat+pcol@end@dblfloat+$

Fifth, we save the original definition of $\set@color into \pcol@set@color$, and then examine if $\set@color \neq \relax$ meaning some coloring package is loaded. If any coloring packages are not loaded, we make macros for background painting, namely $\pcol@bg@paintpage$, $\pcol@bg@paintcolumns$ and $\pcol@bg@paintbox$, $\let-equal$ to \relax for the first two and to \gobble for the last so that they do nothing without coloring package.

If the coloring is enabled, on the other hand, we redefine LATFX's \set@color so that it works as \pcol@set@color@push with color stack. We also prepare the text coloring mechanism to let ifpcol@inner = true in every vbox in the paracol environment as follows. First, we let ifpcol@inner = false because we are not in any vboxes obviously. Then, to use everyvboxfor our own purpose, we do the followings; (1) \globally assign a token \pcol@dummytoken, which should never occurs, to \pcol@everyvbox; (2) save \everyvbox into \pcol@everyvbox locally; (3) let \everyvbox have a \the-reference to \pcol@everyvbox and \pcol@innerture to let ifpcol@inner = true; and then (4) make veryvbox let-equal to <math>pcol@everyvbox. By the last operation (4), any \everyvbox appearing in the paracol environment is replaced with \pcol@everyvbox to keep the real \everyvbox from modified nullifying our own operation \pcol@innertrue. On the other hand, since both \everyvbox and \pcol@everyvbox are registers to hold tokens and thus any operations applicable to **\everyvbox** are also applicable to \pcol@everyvbox, any updates on \everyvbox and explicit references to it are simulated by \pcol@everyvbox. Then the initial tokens given to \pcol@everyvbox by the saving operation (2) or tokens given inside the environment are correctly processed whenever a \vbox is opened, together with \pcol@innertrue to fulfill our own purpose, because the real \everyvbox is let restoreeveryvbox by \aftergroup so that the macro is invoked just after \end{paracol} to examine if any \global assignments to \everyvbox has been made in the environment. The funny **\global** assignment (1) is done for this examination so that we detect global assignments done in the environment having been closed because they should have changed the global value of \pcol@everyvbox to something different from \pcol@dummytoken.

Then we continue the case having some coloring package to make background painting macros \pcol@bg@paintpage, \pcol@bg@paintbox and \pcol@bg@paintcolumns activated by making them \let-equal to their @@ counterparts namely \pcol@bg@@paintpage, \pcol@bg@@paintbox and \pcol@bg@@paintbox and \pcol@bg@@paintbox and \pcol@bg@@paintbox.

Finally we empty the shadow color stack $\tilde{\Gamma} = \clicklinel{eq:regardless}$ to give it initial value regardless of the availability of coloring package.

- 2021 \global\let\pcol@set@color\set@color
- 2022 \ifx\set@color\relax
- 2023 \let\pcol@bg@paintpage\relax \let\pcol@bg@paintbox\@gobble
- 2024 \let\pcol@bg@paintcolumns\relax

2027 \pcol@innerfalse

^{2025 \}else

^{2026 \}let\set@color\pcol@set@color@push

2028 \global\pcol@everyvbox{\pcol@dummytoken}%

- 2029 \pcol@everyvbox\everyvbox
- 2030 \everyvbox{\the\pcol@everyvbox \pcol@innertrue}
- 2031 \let\everyvbox\pcol@everyvbox
- 2032 \aftergroup\pcol@restoreeveryvbox
- 2033 \let\pcol@bg@paintpage\pcol@bg@@paintpage
- 2034 \let\pcol@bg@paintbox\pcol@bg@@paintbox
- 2035 \let\pcol@bg@paintcolumns\pcol@bg@@paintcolumns
- 2036 \fi
- 2037 \gdef\pcol@colorstack@shadow{}%

The sixth settings are for (mainly column-wise) footnotes. We initialize two footnote-related count registers letting $b_f = \col@footnotebase$ have $\c@footnote$ and zero-clearing $n_f = \col@nfootnotes$. Then we redefine LATEX's API macros \footnote, \footnotemark and \footnotetext to let them be our own $\col@footnote, \col@footnotemark$ and $\col@footnotetext$ so that they have starred-versions. The other API macro to be redefined, if pagewise footnote typesetting is in effect, is \footnoterule which lets $\columnwidth = \textwidth$ before invoking its original version saved in $\col@footnoterule$ so that it acts as in single-columned typesetting rather than multi-columned. Then we redefine LATEX's internal macro $\col@footnotetext^{224}$ letting it be our own $\col@fntext$ for encapsulating a footnote in a \vbox and for deferred \insertion with page-wise footnote typesetting.

```
2038
      \pcol@footnotebase\c@footnote \global\pcol@nfootnotes\z@
2039
      \let\footnote\pcol@footnote
2040
      \let\footnotemark\pcol@footnotemark
2041
      \let\footnotetext\pcol@footnotetext
2042
      \ifpcol@scfnote
        \def\footnoterule{{\columnwidth\textwidth \pcol@footnoterule}}%
2043
      \fi
2044
2045
      \@ifundefined{H@@footnotetext}{%
2046
        \let\@footnotetext\pcol@fntext
2047
      }{%
        \let\H@@footnotetext\pcol@fntext
2048
     }
2049
```

Seventh, we let \marginpar, \@mn@@marginnote and \@xympar be our own versions \pcol@marginpar, \pcol@marginnote and \pcol@xympar respectively for the emulation of \marginnote, saving the original version of the first and third into \pcol@@marginpar and \pcol@@xympar. Then we inactivate API macros \twosided and \footnoteplacement together with their backward-compatible macros \swapcolumninevenpages, \noswapcolumnineven pages, \footnotelayout, \multicolumnfootnotes, \singlecolumnfootnotes and \mergedfootnotes, so that they commonly invoke \pcol@ignore because their inherent operations turning corresponding switches are harmful in paracol environment. Note that the inactivation of \twosided is done by redefinition of \pcol@twosided because we need optional argument processing by \twosided even when it is inactivated. Further note, that since footmisc defines its own version of \footnotelayout, we must only redefine \footnotelayout if it is what we expect, i.e. an alias to \footnoteplacement.

```
2050 \let\pcol@@marginpar\marginpar \let\marginpar\pcol@marginpar
```

```
2051 \let\@mn@@marginnote\pcol@marginnote
```

```
2052 \let\pcol@dxympar\dxympar \let\dxympar\pcol@xympar
```

```
2053 \def\pcol@twosided[#1]{\pcol@ignore\twosided}%
```

```
2054 \def\swapcolumninevenpages{\pcol@ignore\swapcolumninevenpages}%
```

²²⁴This is called \H@@footnotetext if hyperref (with option hyperfootnote) is loaded.

```
\def\footnoteplacement#1{\pcol@ignore\footnoteplacement}%
2056
2057
      \ifx\footnotelayout\footnoteplacement
        \def\footnotelayout#1{\pcol@ignore\footnotelayout}%
2058
```

\fi 2059

```
\def\multicolumnfootnotes{\pcol@ignore\multicolumnfootnotes}%
2060
```

\def\singlecolumnfootnotes{\pcol@ignore\singlecolumnfootnotes}% 2061

```
\def\mergedfootnotes{\pcol@ignore\mergedfootnotes}%
2062
```

Eighth, we scan the list \collocalcommands of $\langle com \rangle$ being the name of commands, e.g., switchcolumn, available only in the environment or customized for the environment, applying $\coll def comelt$ to each $\langle com \rangle$ to let $\langle com \rangle = \coll com 0 \cdot \langle com \rangle$ the latter of which is the real implementation of the former. Note that the list does not have all environment-local API commands but we omit \column(*) for column(*) environments because their implementations \pcol@com@column(*) are modified after the first invocation. Therefore, we \define \column(*) to have $\pcol@com@column(*)$ in their bodies²²⁵. We also give the first \definitions of $\pcol@com@column(*)$ com@column(*) to let them do nothing but re\define themselves by \pcol@defcolumn unless \pcol@com@column* is given an optional spanning text argument which is directly processed by \pcol@sptext, if they appear as the first column-switching command/environment after \begin{paracol}. Then we re\define \paracol itself so that it will complain of illegal nesting by \PackageError.

```
2063
      \let\@elt\pcol@defcomelt \pcol@localcommands
2064
      \def\column{\pcol@com@column}%
2065
      \@namedef{column*}{\@nameuse{pcol@com@column*}}%
2066
      \global\let\pcol@com@column\pcol@defcolumn
      \global\@namedef{pcol@com@column*}{\pcol@defcolumn
2067
2068
        \@ifnextchar[%]
         \pcol@sptext\relax}%
2069
      \def\paracol##1{\PackageError{paracol}{%
2070
2071
        Environment paracol cannot be nested.}\@eha}%
```

Ninth, we let \output have our output routine \pcol@output as its sole token, and then make \output request with \penalty = \pcol@op@start by \pcol@invokeoutput to invoke $\colloutput@start for initialization, after letting \elt = \relax to make it sure that any$ lists can be manipulated without unexpected application of a macro to their elements.

```
2072
      \output{\pcol@output}%
```

```
2073
      \let\@elt\relax
```

2074\pcol@invokeoutput\pcol@op@start

tional argument for spanning text, and invoke \pcol@sptext if it has. Otherwise, we invoke \pcol@colpream0 being the column preamble of the first column 0, which will be invoked by \pcol@switchcol if spanning text is given.

```
2075
     \pcol@nextcol\z@
2076
     \ [\%]
       \pcol@sptext{\@nameuse{pcol@colpream0}}}
2077
```

```
\pcol@paracol The macro \pcol@paracol has the definition of \paracol, which is redefined in the macro
              itself, so that the only referrer \pcol@icolumncolor examines if it appears in paracol, i.e.,
              \pcol@paracol \neq \paracol.
```

2078 \let\pcol@paracol\paracol 2079

 $^{^{225}}$ We can do this for other commands instead of adhering to \let to eliminate the exception, but the author loves to use \let as much as possible.

- \pcol@ignore The macro \pcol@ignore $\langle macro \rangle$ is to complain that the $\langle macro \rangle$ being one of the followings appears in paracol environment.

\twosided, \swapcolumninevenpages, \noswapcolumninevenpages, \footnoteplacement, \footnotelayout, \multicolumnfootnotes, \singlecolumnfootnotes, \mergedfootnotes

That is, these macros, except for \twosided, are re\defined in \pcol@zparacol to invoke this macro with the argument identifying themselves, which is shown in the warning message given by \PackageWarning. As for \twosided, the target of the re\definition is \pcol@twosided so that its optional argument is captured before the complaint.

2082 \def\pcol@ignore#1{\PackageWarning{paracol}{The command \string#1 is not 2083 effective in paracol environment and thus ignored}} 2084

\pcol@localcommands The macro \pcol@localcommands is the list of the names of the following *environment-local* API commands (or *local commands* in short) and is solely referred to by \pcol@zparacol.

\switchcolumn	$\operatorname{endcolumn}(*)$	$\t(*)$	$\verb+endnthcolumn(*)$
$\verb+leftcolumn(*)$	$\verb+endleftcolumn(*)$	$\operatorname{rightcolumn}(*)$	$\operatorname{endrightcolumn}(*)$
\flushpage	\clearpage	\cleardoublepage	
\synccounter	\syncallcounters		

Note that we omit column(*) from the list as discussed in the description of pcol@zparacol.

2085	/dei/pcol@localcommands{%
2086	\@elt{switchcolumn}%
2087	\@elt{endcolumn}\@elt{endcolumn*}%
2088	\@elt{nthcolumn}\@elt{endnthcolumn}\@elt{nthcolumn*}\@elt{endnthcolumn*}%
2089	\@elt{leftcolumn}\@elt{endleftcolumn}\@elt{leftcolumn*}\@elt{endleftcolumn*}%
2090	\@elt{rightcolumn}\@elt{endrightcolumn}%
2091	\@elt{rightcolumn*}\@elt{endrightcolumn*}%
2092	\@elt{flushpage}\@elt{clearpage}\@elt{cleardoublepage}%
2093	\@elt{synccounter}\@elt{syncallcounters}}

```
2094 \def\pcol@defcomelt#1{%
2095 \expandafter\let\expandafter\reserved@a\csname pcol@com@#1\endcsname
2096 \expandafter\let\csname #1\endcsname\reserved@a}
2097
```

\@dbldeferlist As discussed in §1.8, 2015 version of LATEX no longer uses \@dbldeferlist but the macro itself \pcol@end@dblfloat is still kept in LATEX. However it will be removed in future to make the first \@cons with it resulting in an error. Therefore, here we have its top level definition with empty duplicatedly in case of its future elimination. The macro \end@dblfloat, on the other hand, is replaced with a new definition in the new LATEX of course, and thus we define \pcol@end@dblfloat

here to keep its old definition and to replace the new one in **paracol** environment as discussed in item-(1) of §1.8.

```
2098 \gdef\@dbldeferlist{}
2099 \def\pcol@end@dblfloat{%
      \if@twocolumn
2100
        \@endfloatbox
2101
        \ifnum\@floatpenalty <\z@
2102
          \@largefloatcheck
2103
           \@cons\@dbldeferlist\@currbox
2104
2105
        \fi
2106
        \ifnum \@floatpenalty =-\@Mii \@Esphack\fi
2107
      \else
2108
        \end@float
2109
      \fi
2110 }
```

13Column Width Setting

\columnratio The API macro \columnratio $\{r_0^l, r_1^l, \cdots, r_{k^l-1}^l\}$ $[r_0^r, r_1^r, \cdots, r_{k^r-1}^r]$ defines the column width \pcol@icolumnratio fraction r_c^l for column c in left parallel-pages and optionally r_c^r for those in right parallel-\pcol@columnratioleft pages. This macro and its callee \pcol@icolumnratio just \globaly \define macros \pcol@ \pcol@columnratioright columnratioleft and \pcol@columnratioright whose bodies have the first and second arguments respectively, or commonly have the first if the second optional one is not given, so that they are given to \pcol@setcolwidth@r as its third argument through \pcol@setcolumnwidth invoked in \pcol@zparacol. Both of \pcol@columnratioleft and \pcol@columnratioright are initialized to be empty so that all columns have same width and are separated by \columnsep as default. Note that \pcol@columnratioleft can be made \let-equal to \relax by the related API macro \setcolumnwidth so that \pcol@setcolumnwidth knows which of specifications given by two API macros is effective and chooses \pcol@setcolwidth@r or \pcol@setcolwidth@s.

```
2111 %% Column Width Setting
2112
2113 \def\columnratio#1{\global\let\pcol@colwidthspecleft\relax
      \gdef\pcol@columnratioleft{#1}%
2114
      \ [\%]
2115
        \pcol@icolumnratio{\gdef\pcol@columnratioright{#1}}}
2116
2117 \def\pcol@icolumnratio[#1] {\gdef\pcol@columnratioright{#1}}
2118 \columnratio{}\relax
2119
```

\setcolumnwidth The API macro \setcolumnwidth $\{s_0^l, s_1^l, \dots, s_{k^l-1}^l\}$ $[s_0^r, s_1^r, \dots, s_{k^r-1}^r]$ defines the column $\colored c in left parallel-pages and optionally <math>s_c^r$ for those in $\pcol@colwidthspecleft$ right parallel-pages, where each specification s_c^x has the form of $[w_c][/[g_c]]$ for width $\col@colwidthspecright$ and gap specifier w_c and g_c . After $\col@colwintmatioleft = \colwidthspecright$ to disable the setting by \columnratio and to enable that done by this macro, the macro and its callee \pcol@isetcolumnwidth just \globaly \define macros \pcol@colwidthspecleft and \pcol@colwidthspecright whose bodies have the first and second arguments respectively, or commonly have the first if the second optional one is not given, so that they are given to \pcol@setcolwidth@s as its fourth argument through \pcol@setcolumnwidth invoked in

\pcol@zparacol. Both of \pcol@colwidthspecleft and \pcol@colwidthspecright are initially undefined because the default specification is given by \columnratio{}.

```
2120 \def\setcolumnwidth#1{\global\let\pcol@columnratioleft\relax
2121 \gdef\pcol@colwidthspecleft{#1}%
2122 \@ifnextchar[%]
2123 \pcol@isetcolumnwidth{\gdef\pcol@colwidthspecright{#1}}
2124 \def\pcol@isetcolumnwidth[#1]{\gdef\pcol@colwidthspecright{#1}}
2125
```

 $\col@setcolumnwidth$ The macro $\col@setcolumnwidth \langle C^0 \rangle \langle C^1 \rangle \langle ratio \rangle \langle spec \rangle$ is invoked solely from $\col@setcolumnwidth$;

 $(C^0, C^1, \langle ratio \rangle, \langle spec \rangle) = (0, C_L, \pcol@columnratioleft, \pcol@colwidthspecleft)$

always and with;

 $(C^0, C^1, \langle ratio \rangle, \langle spec \rangle) = (C_L, C, \pcol@columnratioright, \pcol@colwidthspecright)$

if $C_L < C$ for parallel-paging. The macro simply invokes $\col@setcolwidth@s$ if $\col@columnratioleft = \relax because \setcolumnwidth did so, or <math>\col@setcolwidth@r otherwise$, with all arguments given by $\col@zparacol$.

2126 \def\pcol@setcolumnwidth{%

```
2127 \ifx\pcol@columnratioleft\relax \let\reserved@a\pcol@setcolwidth@s
2128 \else \let\reserved@a\pcol@setcolwidth@r
2129 \fi
2130 \reserved@a}
```

2131

First, we calculate $W = \langle textwidth - (C^1 - C^0 - 1) \times \langle columnsep being the sum of <math>w_c$ for all $c \in [C^0, C^1)$. Then we let $w_c = r_d W$ and $g_c = \langle columnsep$ for all $c \in [C^0, k')$ where $k' = \min(k, C^1 - 1)$, in the $\langle cfor loop scanning r_d$ for all $d = c - C^0 \in [0, k)$. Finally, we let $w_c = (W - \sum_{d=C^0}^{k'-1} w_d)/(C^1 - C^0 - k')$ and $g_c = \langle columnsep$ for all $c \in [k', C^1)$. Note that $\langle columnwidth c$ and $\langle columnsep c$ are macros having the integer representations of w_c and g_c with the unit sp.

```
2132 \def\pcol@setcolwidth@r#1#2#3#4{%
      \@tempcntb#2\advance\@tempcntb-#1\advance\@tempcntb\m@ne
2133
      \@tempdima-\columnsep \multiply\@tempdima\@tempcntb
2134
2135
      \advance\@tempdima\textwidth \@tempdimb\@tempdima
      \@tempcnta#1\relax\@tempcntb#2\advance\@tempcntb\m@ne
2136
      \@for\reserved@a:=#3\do{%
2137
        \ifnum\@tempcnta<\@tempcntb
2138
2139
          \@tempdimc\reserved@a\@tempdima
2140
          \expandafter\xdef\csname pcol@columnwidth\number\@tempcnta\endcsname{%
2141
            \number\@tempdimc sp}%
          \global\@namedef{pcol@columnsep\number\@tempcnta}{\columnsep}%
2142
          \advance\@tempdimb-\@tempdimc
2143
```

```
2144
          \advance\@tempcnta\@ne
        \fi}%
2145
      \@tempcntb#2\advance\@tempcntb-\@tempcnta
2146
      \divide\@tempdimb\@tempcntb
2147
      \@whilenum\@tempcnta<#2\do{%
2148
        \expandafter\xdef\csname pcol@columnwidth\number\@tempcnta\endcsname{%
2149
2150
          \number\@tempdimb sp}%
        \global\@namedef{pcol@columnsep\number\@tempcnta}{\columnsep}%
2151
2152
        \advance\@tempcnta\@ne}%
2153
2154
```

 $\label{eq:constraint} $$ \collocates through (C^0)(C^1)(ratio)(spec) is invoked solely from (pcol@zparacol (pcol@setcw@c) (pcol@setcol@mnwidth once or twice with the arguments described in the explanation (pcol@setcw@s) of the latter macro. The macro calculates <math>w_c = \col@columnwidth c$ for all $c \in [C^0, C^1)$ and (pcol@setcw@filunit $g_c = \col@columnsep c$ for all $c \in [C^0, C^{1-1})$, from the column/gap specifications $s_0, s_1, \ldots, s_{k-1}$ given through the fourth argument (spec), which was given to (setcolumnwidth and then (spec)) and (spec) (spe

kept in \pcol@colwidthspecleft or \pcol@colwidthspecright.

Each specification s_d for w_c and g_c where $c = C^0 + d$ has the form $[w'_d] [/ [g'_d]]$ to specify the natural width w^n_d and g^n_d and infinite stretch factor w^f_d and g^f_d of column/gap specification as follows;

$$w_d^n = \begin{cases} 0 & w_d' = \emptyset \\ 0 & w_d' = f \setminus \text{fill} \\ natural(w_d') & \text{otherwise} \end{cases} \qquad w_d^f = \begin{cases} 1 & w_d' = \emptyset \\ f & w_d' = f \setminus \text{fill} \\ stretch(w_d') & \text{otherwise} \end{cases}$$
$$g_d^n = \begin{cases} \text{\columnsep} & g_d' = \emptyset \\ 0 & g_d' = f \setminus \text{fill} \\ natural(g_d') & \text{otherwise} \end{cases} \qquad g_d^f = \begin{cases} 0 & g_d' = \emptyset \\ f & g_d' = f \setminus \text{fill} \\ stretch(g_d') & \text{otherwise} \end{cases}$$

where natural(x) is the natural width of the skip x and stretch(x) is the infinite stretch factor of x. Note that any finite stretch factors or any shrink factors do not affect them, and infinite stretch units fil, fill and filll are not distinguished. From factors above, we determine w_c and g_c as follows;

$$W = \sum_{d=0}^{m-2} (w_d^n + g_d^n) + w_{m-1}^n$$

$$F = \sum_{d=0}^{m-2} (w_d^f + g_d^f) + w_{m-1}^f$$

$$x_c = \begin{cases} (W_T/W) x_{c-C^0}^n & W \ge W_T \lor F \le 0\\ x_{c-C^0}^n + (x_{c-C^0}^f/F)(W_T - W) & W < W_T \land F > 0 \end{cases} \quad (x \in w, g)$$

where $W_T = \det m = C^1 - C^0$.

To perform the assignments above, the macro at first invoke $\col@setcw@scan \langle C^0 \rangle \langle C^1 \rangle$ {spec} letting $\col@setcw@c = \col@setcw@s = \col@setcw@accumwd and \col@setcw@filunit = 1 pt to scan <math>s_d$ for all $d \in [0,m)$ and to accumulate $W + g_{m-1}^n$ and $F + g_{m-1}^f$ in $\col@setcw@filunit = 1$ pt to scan s_d for all $d \in [0,m)$ and to accumulate $W + g_{m-1}^n$ and $F + g_{m-1}^f$ in $\col@setcw@filunit = 1$ pt to scan s_d for all $d \in [0,m)$ and to accumulate $W + g_{m-1}^n$ and $F + g_{m-1}^f$ in $\col@setcw@filunit = 1$ pt to scan s_d for all $d \in [0,m)$ and to accumulate $W + g_{m-1}^n$ and $F + g_{m-1}^f$ in $\col@setcw@filunit = 1$ pt to scan s_d for all $d \in [0,m)$ and to accumulate $W + g_{m-1}^n$ and $F + g_{m-1}^f$ from them to have W and F. Note that F is represented by a dimension with the unit of pt by the definition of $\col@setcw@filunit$. Then we invoke $\col@setcw@calcfactors$ to calculate $(W_T/W) = \col@setcw@scale and (W_T - W)/F = \col@setcw@filunit.$ again but in this case we let \pcol@setcw@c = \pcol@setcw@set{width}, \pcol@setcw@s = \pcol@setcw@set{sep} and \pcol@setcw@filunit = \@tempdimb = $(W_T - W)/F$ to let w_c and g_c have the values shown above.

2155 \def\pcol@setcolwidth@s#1#2#3#4{\begingroup

\dimen@\z@ \dimen@ii\z@ \def\pcol@setcw@filunit{\@ne\p@}% 2156

- 2157\let\pcol@setcw@c\pcol@setcw@accumwd \let\pcol@setcw@s\pcol@setcw@accumwd
- 2158\pcol@setcw@scan#1#2{#4}%
- \advance\dimen@-\@tempdima \advance\dimen@ii-\@tempdimb 2159
- \pcol@setcw@calcfactors 2160
- \def\pcol@setcw@c{\pcol@setcw@set{width}}% 2161
- \def\pcol@setcw@s{\pcol@setcw@set{sep}}% 2162
- \let\pcol@setcw@filunit\dimen@ii 2163
- 2164\pcol@setcw@scan#1#2{#4}%
- 2165\endgroup}
- $\label{eq:loss} \label{eq:loss} \label{eq:lo$ s_0, s_1, \ldots being the column/gap specifications given to \setcolumnwidth. At first we add ',' as many as m to the tail of (spec) to make it sure the resulting (spec) has m or more elements. Then we scan all elements in the extended (spec) by a \@for loop having many \expandafter but equivalent to;

In the body above, we invoke $\col@setcw@getspec s_i//\column i to parse s_i$ to have w_i^n, w_i^f to be processed by \pcol@setcw@c and g_i^n and g_i^f by \pcol@setcw@s, for all $i \in [0, m)$.

\@tempcnta#1\relax \@whilenum\@tempcnta<#2\do{ 2167

```
\edef\reserved@a{\reserved@a,}\advance\@tempcnta\@ne}%
2168
```

- \@tempcnta#1\relax 2169
- 2170 \expandafter\@for\expandafter\reserved@a\expandafter:\expandafter=\reserved@a 2171\do{%
- 2172\ifnum\@tempcnta<#2\relax
- 2173\expandafter\pcol@setcw@getspec\reserved@a//\@nil
- 2174\fi

```
\advance\@tempcnta\@ne}}
2175
```

 $\col@setcw@getspec$ The macro $\col@setcw@getspec(w'_d)/(g'_d)/(garbage)\col@setcw@getspec(w'_d)/(g'_d)/(garbage)\col@setcw@getspec(w'_d)/(g'_d)/(g'_d)/(g'_d))$ \pcol@setcw@fill

 $\coll{getspec@i}$ scan to parse a column/gap specification $s_d = [w'_d] [/[g'_d]]$, to extract factors w^n_d , w^f_d , g^n_d and g_d^f , and to process width factors by \pcol@setcw@c and gap factors by \pcol@setcw@s. Since the macro is invoked with arguments in the form of $s_d//\langle \text{Onil}, \text{ if } s_d \text{ has } \prime \prime$ in it w'_d and g'_d should have everything preceding and following the '/' respectively while $\langle garbage \rangle$ should have the redundant '/'. Otherwise, i.e., if s_d does not have '/', $w'_d = s_d$ and $g'_d = \emptyset$ while $\langle garbage \rangle = \emptyset^{226}$. Therefore, we invoke \pcol@setcw@getspec@i $\langle default \rangle \{x'_d\}$ twice with $(\langle default \rangle, x'_d) = (\texttt{lill}, w'_d)$ for a column and $(\langle default \rangle, x'_d) = (\texttt{columnsep}, g'_d)$ for a gap, and \pcol@setcw@c and \pcol@setcw@s after each invocation respectively.

> In this macro, at first we scan all tokens in x'_d by *\@tfor* to remove all space tokens in it²²⁷. Then if x'_d after the space removal has nothing, we let $x'_d = \langle default \rangle$. Next we examine if $x'_d = f$ fill in a tricky way by temporarily \letting \@gtempa = \relax, defining

 $^{^{226}}$ If s_d have two or more '/', everything following the second one is thrown away into $\langle garbage \rangle$ together with '//'. Therefore we could check if s_d has at most one '/' by examining $\langle garbage \rangle$ but we abandon it simply ignoring $\langle garbage \rangle$. ²²⁷A proper skip specification and "f\fill" is always proper without space tokens in them.

\fill as "1pt\gdef\@gtempa{}" and making an assignment "\@tempskipa x'_d ". That is, if $x'_d = f$ \fill, \@tempskipa will have $f \cdot 1$ pt being a proper dimension and \@gtempa is made empty. Otherwise, \@tempskipa should have x'_d which must be a proper skip and \@gtempa remains unchanged from \relax. Therefore, if \@gtempa = \relax we let \@tempskipa = x'_d again²²⁸. Otherwise, we invoke \pcol@setcw@fill x'_d to let \@tempskipa have 0 pt plus f fil where f is replaced by 1 if $f = \emptyset$.

Now \@tempskipa has x_d^n as its natural component and may have some infinite stretch component x_d^f specified explicitly or with \fill. Therefore, we assign \@tempskipa to \@tempdima so that it has x_d^n , and then, after adding 0pt plus 1000pt minus 1000pt to \@tempskipa to make it sure it has both stretch and shrink components²²⁹ keeping infinite stretch factor if any, invoke \pcol@extract@fil giving it \the-expansion of \@tempskipa as the argument to let \@tempdimb = $x_d^f \times \pcol@setcw@filunit.$

```
2176 \def\pcol@setcw@getspec#1/#2/#3\@nil{%
      \pcol@setcw@getspec@i\fill{#1}\pcol@setcw@c
2177
      \pcol@setcw@getspec@i\columnsep{#2}\pcol@setcw@s}
2178
2179 \def\pcol@setcw@getspec@i#1#2{%
      \def\reserved@a{}%
2180
      \@tfor\reserved@b:=#2\do{\edef\reserved@a{\reserved@a\reserved@b}}
2181
      \ifx\reserved@a\@empty \let\reserved@a#1\fi
2182
      \let\@gtempa\relax
2183
      {\def\fill{1\p0\gdef\0gtempa{}}\0tempskipa\reserved0a}%
2184
      \ifx\@gtempa\relax \@tempskipa\reserved@a\relax
2185
      \else \expandafter\pcol@setcw@fill\reserved@a
2186
      \fi
2187
2188
      \@tempdima\@tempskipa
      \advance\@tempskipa0\p@\@plus\@m\p@\@minus\@m\p@\relax
2189
2190
      \expandafter\pcol@extract@fil\the\@tempskipa\@nil}
2191 \def\pcol@setcw@fill#1\fill{\def\reserved@b{#1}%
      \ifx\reserved@b\@empty \let\reserved@b\@ne \fi
2192
      \@tempskipa0\p@\@plus\reserved@b fil\relax}
2193
2194
```

 $\label{eq:lossetcw@accumwd} \end{tabular} The macro \col@setcw@accumwd is made \let-equal to \col@setcw@c and \col@setcw@setcw@setcw@getspec with setting \col@setcws@setcw@setcw@setcw@$

2195 \def\pcol@setcw@accumwd{\advance\dimen@\@tempdima \advance\dimen@ii\@tempdimb}

 $(\clicklineta conditions) \in \{(\emptyset, (x_d^f/F)(W_T - W)), (W_T/W, 0)\}$

Therefore, we calculate $x_c = \col@setcw@scale \times \dempdima + \dempdimb and \xdefine \pcol@column (wors) c to let it have the integer representation of <math>x_c$ with the unit sp. 2196 \def\pcol@setcw@set#1{%}

2197 \dvectorempdima\pcol@setcw@scale\dvectorempdima \advance\dvectorempdima\dvectorempdimb 2198 \expandafter\xdef\csname pcol@column#1\number\dvectorempcnta\endcsname{%

 $^{^{228}\}mbox{Because the first assignment is done in a group.}$

 $^{^{229}}$ Almost sure because they could be -1000 pt, but we ignore the possibility.

2199 \number\@tempdima sp}} 2200

 $\col@setcw@calcfactors The macro \pcol@setcw@calcfactors is used solely in \pcol@setcolwidth@s to calculate \pcol@setcw@calcf $\phi_s = \pcol@setcw@scale and $\phi_f = \dimen@ii as follows \pcol@setcw@scale $\pcol@setcw@scale $\pcol@setcw@scale$

$$(\phi_s, \phi_f) = \begin{cases} (W_T/W, 0) & W \ge W_T \lor F \le 0\\ (1, (W_T - W)/F) & W < W_T \land F > 0 \end{cases}$$

where $W = \dim 0$, $F \times 1 \text{ pt} = \dim 0$ i and $W_T = \det 0$, and $\phi_s = 1$ is represented by empty body of $\operatorname{col@setcw@scale}$. First we deal with the special and trivial case of $W = W_T$ to let $\phi_s = 1$ and $\phi_f = 0$ so as to avoid arithmetic error in the calculation of W_T/W . If $W \neq W_T$ on the other hand, we calculate W_T/W by $\operatorname{col@setcw@calcf}(W_T)\langle W \rangle \langle \phi_s \rangle$ to have a provisional result. Then if $W < W_T$ and F > 0, we let $\phi_s = 1$ and invoke $\operatorname{col@setcw@calcf}(W_T - W)$ and $F \times 1 \text{ pt}$ but throw away the result $(W_T - W)/(F \times 1 \text{ pt})$ because $\operatorname{col@mendimb}$ should have $(W_T - W)/F$ which is then set into $\phi_f = \operatorname{dimendii}$. Otherwise, we keep the provisional result of ϕ_s as the final one and let $\phi_f = \operatorname{dimendii} = 0$.

The macro $\col@setcw@calcf(x)(y)(z)$ calculates $z \approx x/y$ and let $\colmmode z = z \times 1$ pt as follows. First we find the following three parameters.

$$k_1 = \min\{k \mid k \ge 0, \ x \cdot 2^k \ge 2^{13} \text{ pt}\}$$

$$k_2 = \max\{k \mid y \mod 2^k = 0\}$$

$$k_3 = \min\{k \mid k \ge 0, \ \lfloor y/2^{k_2+k} \rfloor \le 2^{15}\}$$

With these parameters, we calculate $z' = \lfloor (x \cdot 2^{k_1}) / \lceil y/2^{k_2+k_3} \rceil \rfloor$ to have a good approximation of $(x/y) \cdot 2^k$ where $k = k_1 + k_2 + k_3$ without arithmetic overflow. Then if $z'/2^k \ge 2^{14}$ or in other words Z is larger than \maxdimen, we complain that by \PackageError and, in case a user dare to continue the typesetting process, we let $Z = 10000 \, \text{pt}$. Otherwise, we calculate $Z = (z'/2^k) \cdot 2^{16} = z' \cdot 2^{16-k}$ to have it in \@tempdimb by $Z = z' \times 2^{16-k}$ if k < 16, or by $Z = z'/2^{k-16}$ otherwise. Finally we invoke \pcol@extract@pt giving it \the-representation of Z to have z.

Note that it is assured $z \leq x/y$ regardless of successfulness of the calculation and thus the scaling $\phi_s x_d^n$ and stretching $x_d^n + \phi_f x_d^f$ cannot exceed their exact value to make it also sure that $\sum_{c=C_0}^{C^1-2} (w_c + g_c) + w_{C^1-1} \leq W_T$ and thus the series of columns and column-separating gaps should not cause overfull when a page is shipped out with fil added to each column-separating gap for underfull avoidance.

```
2201 \def\pcol@setcw@calcfactors{%
      \ifdim\dimen@=\textwidth \def\pcol@setcw@scale{}\dimen@ii\z@
2202
2203
      \else
        \pcol@setcw@calcf\textwidth\dimen@\pcol@setcw@scale
2204
        \ifdim\dimen@<\textwidth \ifdim\dimen@ii>\z@
2205
          \def\pcol@setcw@scale{}%
2206
          \@tempdimc\textwidth \advance\@tempdimc-\dimen@
2207
          \pcol@setcw@calcf\@tempdimc\dimen@ii\reserved@a \dimen@ii\@tempdimb
2208
2209
        \else \dimen@ii\z@ \fi
        \else \dimen@ii\z@ \fi
2210
2211
      \fi}
2212 \def\pcol@setcw@calcf#1#2#3{%
      \@tempdimb#1\@tempdima#2\@tempcnta\z@
2213
      \ifdim\@tempdima=\z@ \@tempdima1sp\relax\fi
2214
      \@whiledim\@tempdimb<8192\p@\do{%
2215
```

```
\multiply\@tempdimb\tw@ \advance\@tempcnta\@ne}%
                                  2216
                                                 \@tempdimc\@tempdima
                                  2217
                                                 \@whiledim\@tempdima=\@tempdimc\do{%
                                  2218
                                                     \divide\@tempdimc\tw@ \multiply\@tempdimc\tw@
                                  2219
                                  2220
                                                     \ifdim\@tempdima=\@tempdimc
                                                          \divide\@tempdima\tw@ \divide\@tempdimc\tw@ \advance\@tempcnta\@ne
                                  2221
                                  2222
                                                     \fi}
                                                 \advance\@tempdima-1sp\relax
                                  2223
                                                 \@whilenum\@tempdima>32768\do{\divide\@tempdima\tw@ \advance\@tempcnta\@ne}%
                                  2224
                                  2225
                                                 \advance\@tempdima1sp\relax
                                                 \divide\@tempdimb\@tempdima \@tempdimc\@tempdimb \@tempcntb\@tempcnta
                                  2226
                                                 \@whilenum\@tempcntb>\z@\do{\divide\@tempdimc\tw@ \advance\@tempcntb\m@ne}
                                  2227
                                                 \ifnum\@tempdimc>16383\relax
                                  2228
                                                     \PackageError{%
                                  2229
                                  2230
                                                          Scaling/filling factor for column/gap width is too large.}\@eha
                                  2231
                                                     \@tempdimb\@M\p@
                                  2232
                                                 \else
                                                     \@tempcntb\sixt@@n \advance\@tempcntb-\@tempcnta
                                  2233
                                  2234
                                                     \ifnum\@tempcntb<\z@
                                                          \@whilenum\@tempcntb<\z@\do{\divide\@tempdimb\tw@ \advance\@tempcntb\@ne}%
                                  2235
                                  2236
                                                     \else
                                                          \@whilenum\@tempcntb>\z@\do{%
                                  2237
                                                               \multiply\@tempdimb\tw@ \advance\@tempcntb\m@ne}%
                                  2238
                                                     \fi
                                  2239
                                  2240
                                                \fi
                                  2241
                                                 \expandafter\pcol@extract@pt\the\@tempdimb#3}
                                  2242
      \pcol@kw@pt at the top level to \define \pcol@kw@pt, \pcol@kw@plus, \pcol@kw@minus and \pcol@kw@fil
  \pcol@kw@plus letting them have \langle pt \rangle = pt, \langle plus \rangle = plus, \langle minus \rangle = minus and \langle fil \rangle = fil in their body
\colorwdminus respectively but with \colorwdminus respectively respectiv
```

\pcol@kw@fil the definition, we invoke \pcol@defkw giving it \the-representation of \@tempskipa letting it have 1pt plus 1 fil minus 1 fil having all keywords we need to have²³⁰. The macro \pcol@ kw@pt is used in \pcol@extract@fil@ii $\langle unit \rangle$ \@nil to examine if $\langle unit \rangle = pt$, and in \pcol@ def@extract@pt to \define \pcol@extract@pt having pt in its argument specification. The macros \pcol@kw@plus and \pcol@kw@minus are used only in \pcol@def@extract@fil, and \pcol@kw@fil only in \pcol@def@extract@fil@iii, to \define \pcol@extract@fil having plus and minus, and \pcol@extract@fil@iii having fil, in their argument specifications respectively.

```
2243 \@tempskipa 1\p@\@plus1fil\@minus1fil\relax
2244 \def\pcol@defkw1.0#1 #2 1.0#3 #4 1.0#5\@nil{%
2245
      \def\pcol@kw@pt{#1}\def\pcol@kw@plus{#2}\def\pcol@kw@fil{#3}%
2246
      \def\pcol@kw@minus{#4}}
2247 \expandafter\pcol@defkw\the\@tempskipa\@nil
2248
```

 $^{^{230}}$ We can do what \pcol@defkw does by temporarily giving \catcode = 12 to the characters for the keywords of course, but this method is much easier.

 $\clicklel{local_$ \clicklinet $\verb|pcol@extract@fil@i column/gap specification x'_d and to let \verb|@tempdimb = f \cdot u where u = \verb|pcol@setcw@filunit \in wdd and to let |@tempdimb = f \cdot u where u = \verb|pcol@setcw@filunit \in wdd and to let |@tempdimb = f \cdot u where u = \verb|pcol@setcw@filunit \in wdd and to let |@tempdimb = f \cdot u where u = \verb|pcol@setcw@filunit \in wdd and to let |@tempdimb = f \cdot u where u = \verb|pcol@setcw@filunit \in wdd and to let |wdd and to le$ $\coldextract@fil@ii {1pt, } \phi_f = \coldextract@fil@ii {1pt, } \phi_f = \coldextract@fil@ii } if f exist or \coldextract@fil@ii = 0 otherwise. First of all, since the macro$ $\colored extractOfilOiii$ has keywords plus and minus in $\colored e = 12$ in its argument specification, we \define it \pcol@extract@fil@iii using \pcol@def@extract@fil, whose body is equivalent to

\def\pcol@extract@fil#1_plus_#2_minus#3\@nil{\pcol@extract@fil@i#2\@nil}

just once at the top level. Then since s should have the form $\langle n \rangle . \langle m \rangle \langle unit \rangle$ where n and m are decimal digit sequences and $\langle unit \rangle \in \{pt, fil, fill, fill\}, we examine if$ $\langle unit \rangle = pt \text{ or not by a tricky way in \pcol@extract@fil@i(n).(m.unit)\@nil. That is, we do$ $\operatorname{count}(m \cdot unit) \operatorname{lin}(unit) \operatorname{count}(unit) \operatorname{count}(unit) \operatorname{lin}(unit) \operatorname{lin}$ after m is assigned to \count@ to capture $\langle unit \rangle$. Then if it is pt we let \@tempdimb = 0, or otherwise invoke $\colored colored co$ have a postfix being fil, fill or filll, to have $\langle \texttt{Ctempdimb} = f \cdot u$ finally. Note that since \pcol@extract@fil@iii also has the keyword fil in its argument specification, we \define it using \pcol@def@extract@fil@iii, whose body is equivalent to

\def\pcol@extract@fil@iii#1fil#2\@nil{% \@tempdimb\pcol@setcw@filunit\relax \@tempdimb#1\@tempdimb}

just once at the top level too.

```
2249 \edef\pcol@def@extract@fil{%
      \def\noexpand\pcol@extract@fil
2250
      ##1\space\pcol@kw@plus\space##2\space\pcol@kw@minus##3\noexpand\@nil{%
2251
        \noexpand\pcol@extract@fil@i##2\noexpand\@nil}}
2252
2253 \pcol@def@extract@fil
2254 \def\pcol@extract@fil@i#1.#2\@nil{\def\reserved@a{#1.#2}%
2255
      \afterassignment\pcol@extract@fil@ii\count@#2\@nil}
2256 \def\pcol@extract@fil@ii#1\@nil{\def\reserved@b{#1}%
2257
      \ifx\reserved@b\pcol@kw@pt \@tempdimb\z@
2258
      \else \expandafter\pcol@extract@fil@iii\reserved@a\@nil
2259
      \fi}
2260 \edef\pcol@def@extract@fil@iii{%
      \def\noexpand\pcol@extract@fil@iii##1\pcol@kw@fil##2\noexpand\@nil{%
2261
        \@tempdimb\noexpand\pcol@setcw@filunit\relax \@tempdimb##1\@tempdimb}}
2262
2263 \pcol@def@extract@fil@iii
2264
```

 $\colored extractor the macro \colored extractor f bt (scale) is solely used in \colored extract f$ \coldextractOpt from a dimension in the form of fpt and to let the macro $\langle scale \rangle$ have f. Since this macro has the keyword pt in its argument specification, we \define it using \pcol@def@extract@pt, whose body is equivalent to

\def\pcol@extract@pt#1pt#2{\def#2{#1}}

```
just once at the top level again.
2265 \edef\pcol@def@extract@pt{%
      \def\noexpand\pcol@extract@pt##1\pcol@kw@pt##2{\def##2{##1}}}
2266
2267 \pcol@def@extract@pt
2268
```

14 Counter Operations

 $\climits define the API macro \globalcounter {ctr}, implemented by \pcol@globalcounter and also used$ $\cologlobalcounter@s$ in $\cologlobalcounter@s$ is a global counter, defines that $\langle ctr \rangle$ is a global counter, $\colored pcolored counter$ and thus adds it to $\Theta^g = \colored gcounters$, which has page at initial. Note that we examines **\pcol@gcounters** if $\langle ctr \rangle \in \Theta^g$ prior to the addition to avoid the duplication in Θ^g . Also note that initial definition of \pcol@gcounters is done by \gdef just for consistent \global assignments to it. On the other hand \globalcounter*, implemented by \pcol@globalcounter@s, makes all counters kept in \cl@ckpt global by letting \pcol@gcounters have the list. Switching these two functionality is done by \globalcounter examining if it is followed by a * by \@ifstar. 2269 %% Counter Operations 2270 2271 \def\globalcounter{\@ifstar\pcol@globalcounter@s\pcol@globalcounter} 2272 \def\pcol@globalcounter@s{\global\let\pcol@gcounters\cl@@ckpt} 2273 \def\pcol@globalcounter#1{{% \@tempswafalse \def\reserved@a{#1}% 2274\def\@elt##1{\def\reserved@b{##1}% 2275\ifx\reserved@a\reserved@b \@tempswatrue \fi}% 22762277\pcol@gcounters 2278\if@tempswa\else \@cons\pcol@gcounters{{#1}}\fi}} 2279 \gdef\pcol@gcounters{\@elt{page}} localcounter The API macro $localcounter{ctr}$, also used in pcol@fnlayout@c to localize the counter footnote, declares that $\langle ctr \rangle$ is a local counter, and thus removes it from Θ^g by \pcol@ remove counter if $\langle ctr \rangle \neq$ page. 2280 \def\localcounter#1{% \expandafter\ifx\csname c@#1\endcsname\c@page\else 2281 \pcol@removecounter\pcol@gcounters{#1}% 2282 2283 fi \coloremctrelt The macro $\coloremctrelt{\theta^g}$ is invoked solely from $\coloremccoloremcoloremctrelt{output}$ and is applied to each \pcol@removecounter global counter $\theta^g \in \Theta^g$ to remove it from $\Theta =$ \pcol@counters in which we have Θ^l finally. \pcol@iremctrelt The macro also moves $cl@.\theta^g = \zeta(\theta^g)$ to $pcol@cl@.\theta^g$ to keep the list of the descendant

local counters of θ^g in it, and then re\defines $cl@\theta^g = cl@stepcounter{\theta^g}$ so that it is invoked on $stepcounter{\theta^g}$ to let $val_c(\theta^l) = 0$ for all $c \in [0, C)$ and $\theta^l \in \zeta(\theta^g)$, if $\theta^g \neq page$. These operations are performed by a lengthy sequence with many occurrences of \expandafter, \csname and \endcsname but the sequence is equivalent to the following.

As for the removal of θ^g from Θ , we invoke $\coloremovecounter \langle \Theta' \rangle \{\theta\}$ giving it $\Theta' = \Theta$ and $\theta = \theta^g$. This macro, also invoked from $\coloremovecounter \{\theta^l\}$ with $\Theta' = \Theta^g$ and $\theta = \theta^l$, does $\Theta'' \leftarrow \Theta', \Theta' = \emptyset$, and then apply $\coloremovecounter \{\Theta'\}$ to each $\theta' \in \Theta''$ to let $\Theta' \leftarrow \Theta' \cup \{\theta'\}$ by $\coloremovecounter \{\theta'\} = \theta$.

```
2284 \def\pcol@remctrelt#1{%
2285 \expandafter\let\expandafter\reserved@a\csname cl@#1\endcsname
2286 \expandafter\let\csname pcol@cl@#1\endcsname\reserved@a
2287 \expandafter\ifx\csname c@#1\endcsname\c@page\else
2288 \@namedef{cl@#1}{\pcol@stepcounter{#1}}%
2289 \fi
2290 \pcol@removecounter\pcol@counters{#1}}
```

```
2291 \def\pcol@removecounter#1#2{%
      \def\reserved@a{#2}\let\reserved@b#1\relax \global\let#1\@empty
2292
      {\def\@elt{\pcol@iremctrelt#1}\reserved@b}}
2293
2294 \def\pcol@iremctrelt#1#2{%
      \def\reserved@b{#2}%
2295
      \ifx\reserved@a\reserved@b\else \@cons#1{{#2}}\fi}
2296
2297
```

- \define the counter The API macro \define the counter $\langle \theta^l \rangle \langle c \rangle \langle rep \rangle$ define the local representation $\langle rep \rangle$ for a local counter θ^l in a column c. It \defines \pcol@thectr@ $\theta^l \cdot c$ to have $\langle rep \rangle$ in its body. 2298 \def\definethecounter#1#2#3{\@namedef{pcol@thectr@#1#2}{#3}}
 - $\verb|pcol@thectrelt The macro \pcol@thectrelt \\\langle \theta^l \rangle is invoked solely in \pcol@zparacol and is applied to each$ $\theta^l \in \Theta^l$ to define its local representation of default and that of the leftmost column 0. To give unique representations θ^l used by hyperref, it prepends the current column number as \pcol@thecurrcol to them. The macro performs a lengthy sequence with many occurrences of \expandafter, \csname and \endcsname but the sequence is equivalent to the following.

```
\verb+let+pcol@thectr@+\theta^l=+the+\theta^l
\label{eq:linear} $$ \int d\theta = \theta^{-1} - \theta^{-1} -
```

```
2299 \def\pcol@thectrelt#1{%
2300
      \expandafter\let\expandafter\reserved@a\csname the#1\endcsname
2301
      \expandafter\let\csname pcol@thectr@#1\endcsname\reserved@a
      \expandafter\let\expandafter\reserved@a\csname pcol@thectr@#10\endcsname
2302
      \ifx\reserved@a\relax\else
2303
2304
        \expandafter\let\csname the#1\endcsname\reserved@a
2305
      \fi
      \mathbb{I}_{\mathbb{I}}^{\mathbb{I}}
2306
        \expandafter\def\csname theH#1\expandafter\expandafter\expandafter\endcsname
2307
          \expandafter\expandafter\expandafter{%
2308
          \expandafter\expandafter\expandafter\pcol@thecurrcol\csname theH#1\endcsname
2309
2310
        7%
2311
     3%
2312 }
2313 \def\pcol@thecurrcol{column\number\pcol@currcol.}
2314
```

 \clicklinet \pcol@loadctrelt The macro \pcol@loadctrelt $\langle \theta^l \rangle \langle val_c(\theta^l) \rangle$ is invoked from \pcol@zparacol and \pcol@ \pcol@storecounters synccounter and is applied to each element $\langle \theta^l, val_c(\theta^l) \rangle \in \Theta_c$ for a column c to define a $\col@storectrelt macro \col@ctr@.θ having <math>val_c(\theta^l)$ in its body for a temporary use. This macro or its redefined version is then referred to by $\clicklinet pcol@cmpctrelt \langle \theta^l \rangle$ or $\clicklinet pcol@storectrelt \langle \theta^l \rangle$. The latter is invoked from \pcol@storecounters via \pcol@sscounters to add $\langle \theta^l, v(\theta^l) \rangle$ to \Qgtempa by \Qcons to rebuild Θ_c for a column c in \Qgtempa.

> The macro $\col@storecounters$ is invoked solely from $\col@synccounter(\theta)$ to update a local counter θ with $val(\theta)$ for counter synchronization. That is, \pcol@storecounters is used to add $\langle \theta^l, v(\theta^l) \rangle$ to \Ogtempa for all $\theta^l \in \Theta^l$ by \pcolOsscounters giving it \pcolO storectrelt as its argument, where $v(\theta^l)$ is modified if $\theta^l = \theta$ or unmodified otherwise after it is defined by \pcol@loadctrelt.

2315 \def\pcol@loadctrelt#1#2{\@namedef{pcol@ctr@#1}{#2}}

	2316 \def\pcol@storecounters{\pcol@sscounters\pcol@storectrelt} 2317 \def\pcol@storectrelt#1{\@cons\@gtempa{{#1}{\@nameuse{pcol@ctr@#1}}}}
\pcol@savecounters \pcol@savectrelt	The macro <code>\pcol@savecounters</code> is invoked from <code>\pcol@com@syncallcounters</code> , <code>\pcol@stepcounter</code> and <code>\pcol@switchcol</code> to let Θ_c for a column c have the list of $\langle \theta^l, val_c(\theta^l) \rangle$ where $val_c(\theta^l)$ is the value of $\langle c0.\theta^l$ to be saved in the list. It does this operation invoking <code>\pcol@savectrelt</code> as its argument. The macro <code>\pcol@savectrelt \langle \theta^l \rangle</code> adds $\langle \theta^l, val_c(\theta^l) \rangle$ to <code>\@gtempa</code> by <code>\@cons</code> to rebuild Θ_c for a column c in <code>\@gtempa</code> .
	<pre>2318 \def\pcol@savecounters{\pcol@savectrelt} 2319 \def\pcol@savectrelt#1{\@cons\@gtempa{{#1}{\number\csname c@#1\endcsname}}}</pre>
\pcol@sscounters	The macro $\colorscounters \langle elt \rangle$ is invoked from \colorscounters with $\langle elt \rangle = \colorscounters$ or \colorscounters with $\langle elt \rangle = \colorscounters$ to build $\Theta_c = \colorscounters \cdot c$ for a column c . To do that, it lets $\colorscounters = ()$ and then apply $\langle elt \rangle$ to all $\theta^l \in \Theta^l = \colorscounters$ to have updated Θ_c in \colorscounters . Then finally, \colorscounters is moved into Θ_c by \colorscounters^{231} .
	<pre>2320 \def\pcol@sscounters#1{\begingroup 2321 \global\let\@gtempa\@empty 2322 \let\@elt#1\relax \pcol@counters 2323 \let\@elt\relax 2324 \expandafter\xdef\csname pcol@counters\number\pcol@currcol\endcsname{% 2325 \@gtempa}% 2326 \endgroup} 2327</pre>
\pcol@cmpctrelt	The macro $\coll{c}\end{c}\en$
\synccounter \pcol@com@synccounter	The macro $\condensity counter \langle \theta \rangle$, being the implementation of the environment-local API macro \synccounter , lets $val_c(\theta) = val(\theta)$ for all $c \in [0, C)$. That is, the value of the counter θ is broadcasted to all columns for the counter synchronization of θ . This broadcast is done by \coldsynccounter with an argument ℓ_{θ} so that it works only on θ . 2334 $\ell_{coldsynccounter#1{\coldsynccounter{\ell_{1}}}$
\pcol@synccounter \pcol@syncctrelt	The macro $\collogsynccounter\langle lst \rangle$ is invoked from $\collogsynccollogsynccounter\langle lst \rangle = \logsyncloses and from \collogsynccounter\langle ctr \rangle with \langle lst \rangle = \collogsynccollogsynccounter\langle ctr \rangle with \langle lst \rangle = \collogsyncloses and \col$
	231 It can be done by \global\let more efficiently but it is lengthy due to two \expandafter .

```
\let\@elt\relax \edef\reserved@a{#1}%
                 2336
                        \pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do{%</pre>
                 2337
                          \let\@elt\pcol@loadctrelt \@nameuse{pcol@counters\number\pcol@currcol}%
                 2338
                          \let\@elt\pcol@syncctrelt \reserved@a
                 2339
                 2340
                          \pcol@storecounters
                          \advance\pcol@currcol\@ne}}}
                 2341
                 2342
                     \def\pcol@syncctrelt#1{%
                          \expandafter\edef\csname pcol@ctr@#1\endcsname{\number\@nameuse{c@#1}}}
                 2343
                 2344
\syncallcounters The macro \pcol@com@syncallcounters, being the implementation of the environment-local
```

 $\collecom@syncallcounters API macro \syncallcounters, makes all local counters in all columns have the value in the current column. That is, for each <math>c \in [0, C)$, we invoke $\coll@savecounters$ to let $val_c(\theta^l) = val(\theta^l)$ for all $\theta^l \in \Theta^l$.

```
2345 \def\pcol@com@syncallcounters{{%
2346 \pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do{%
2347 \pcol@savecounters \advance\pcol@currcol\@ne}}}
2348</pre>
```

```
\label{eq:linear} $$ \int \frac{\partial^l \cdot c}{\partial t} \left( \frac{\partial^l \cdot c}{\partial t} \right)^l + \frac{\partial^l \cdot c}{\partial t} = \frac{\partial^l \cdot c}{\partial t} $$ fi
```

2349 \def\pcol@setctrelt#1#2{%

2350 \global\csname c@#1\endcsname#2\relax

2351 \expandafter\ifx\csname pcol@thectr@#1\number\pcol@currcol\endcsname\relax

2352 \expandafter\let\expandafter\reserved@a\csname pcol@thectr@#1\endcsname

- 2353 **\else**
- 2354 \expandafter\let\expandafter\reserved@a
- 2355 \csname pcol@thectr@#1\number\pcol@currcol\endcsname
- 2356 \fi
- 2357 \expandafter\let\csname the#1\endcsname\reserved@a} 2358

 $\begin{aligned} & \coll{0} tepcounter The macro \coll{0} tepcounter \langle \theta^g \rangle is invoked from \stepcounter \langle \theta^g \rangle for a global counter \\ & \coll{0} tercoll{0} tercoll{$

After the operations above, we apply $(\texttt{Ostpelt}(\theta) \text{ to each } \theta \in \zeta(\theta^g) \text{ for } \texttt{global zero-clearing.}$

2359 \def\pcol@stepcounter#1{\begingroup

```
2360 \pcol@currcol\z@ \@whilenum\pcol@currcol<\pcol@ncol\do{%
```

2361 \let\@elt\pcol@stpldelt \@nameuse{pcol@counters\number\pcol@currcol}%

```
\let\@elt\pcol@stpclelt \@nameuse{pcol@cl@#1}%
2362
        \pcol@savecounters
2363
       \advance\pcol@currcol\@ne}%
2364
2365
      \endgroup
      \let\@elt\@stpelt \@nameuse{pcol@cl@#1}}
2366
2367 \def\pcol@stpldelt#1#2{\csname c@#1\endcsname#2\relax}
2368 \def\pcol@stpclelt#1{\csname c@#1\endcsname\z@}
2369
```

15**Column-Switching Commands and Environments**

\pcol@par Before giving the definition of column-switching commands and environments, we define a commonly used macro \pcol@par, which do \par if necessary, i.e., we are not in vertical mode. The reason why we don't simply do par is that it may have some definition different from QQpar and thus an incautious repetition of \par may cause undesirable results. This macro is used in \pcol@com@switchcolumn, \pcol@sptext, \pcol@com@endcolumn, \pcol@flushclear, and \endparacol.

```
2370 %% Column-Switching Commands and Environments
2371
2372 \def\pcol@par{\ifvmode\else \par \fi}
2373
```

\switchcolumn The macro \pcol@com@switchcolumn[d], being the implementation of the environment-local \pcol@com@switchcolumn API macro \switchcolumn, switches to the column d if provided through its optional argument, \pcol@switchcolumn or to $d = (c+1) \mod C$ otherwise where c is the ordinal of the current column. After making \pcol@iswitchcolumn it sure to be in vertical mode by \pcol@par, it invokes \pcol@defcolumn to give \pcol@com@ column(*) their \definitions for occurrences not as the very first column-switching command or environment of the current paracol environment. Then, after calculating $d = (c+1) \mod C$, this macro simply invokes \pcol@switchcol[d] with or without the calculated d depending on the existence of the optional argument delimiter '['.

> The macro $\colorswitchcolumn[d]$ lets $\colorswitcol = d$ and confirms $0 \le d < C$ or abort the execution by \PackageError if it does not hold. Then it invokes \pcol@ iswitchcolumn if \switchcolumn[d] is followed by a '*', or \pcol@switchcol otherwise.

> The macro $\colorswitchcolumn[\langle text \rangle]$ invokes $\colorstext[\langle text \rangle]$ if the optional argument is provided, or $\col@switchcol otherwise$, after letting $\ifpcol@sync = true$ for explicit synchronization.

```
2374 \def\pcol@com@switchcolumn{\pcol@par
```

```
2375
      \pcol@defcolumn
```

- \@tempcnta\pcol@currcol \advance\@tempcnta\@ne 2376
- \ifnum\@tempcnta<\pcol@ncol\else \@tempcnta\z@ \fi 2377
- 2378 \@ifnextchar[%]

```
\pcol@switchcolumn{\pcol@switchcolumn[\@tempcnta]}}
2379
```

```
2380 \def\pcol@switchcolumn[#1] {%
```

\pcol@nextcol#1\relax 2381

```
\@tempswafalse
2382
```

```
2383
      \ifnum#1<\z@ \@tempswatrue \fi
```

```
2384
      \ifnum#1<\pcol@ncol\else \@tempswatrue \fi
```

```
2385
      \if@tempswa
```

```
2386
        \PackageError{paracol}{%
```

```
2387
          Column number \number#1 must be less than \number\pcol@ncol}\@eha
```

```
2388
        \pcol@nextcol\z@
```

```
2389 \fi
2390 \@ifstar\pcol@iswitchcolumn\pcol@switchcol}
2391 \def\pcol@iswitchcolumn{%
2392 \global\pcol@synctrue
2393 \@ifnextchar[%]
2394 \pcol@sptext\pcol@switchcol}
2395
```

\pcol@sptext The macro \pcol@sptext[$\langle text \rangle$] is invoked from \pcol@zparacol and \pcol@iswitchcolumn to put a spanning text $\langle text \rangle$ given as the optional argument of the former or that of \switchcolumn* and its relative environment openers for the latter. The macro has \long attribute because the spanning text may have \par. Since the text is put in the column-0 regardless of its physical position, we let \pcol@nextcol have 0 after saving the target column d =\pcol@nextcol in \@tempcnta. Then we switch to the column by \pcol@ switchcol, after turning \ifpcol@sync = true to set a synchronization point above the text and \ifpcol@sptextstart = true to tell \pcol@output@switch to prepare the capture of spanning text saving the pre-spanning-text stuff.

Next, we let \ifpcol@sptextstart = false and \ifpcol@sptext = true to indicate the main vertical list contains only the spanning text and it is to be captured by \output routine. Then the $\langle text \rangle$ is put in a group in which we let \columnwidth = \hsize = \textwidth and \linewidth = \textwidth - μ with \parshape to indent lines by \@totalleftmargin if $\mu > 0$, to let spanning text span across all columns reflecting the indentation in the list-like environments surrounding paracol if any. We also let \col@number = 1 to ensure again that \maketitle produces a title without \twocolumn if it is in the spanning text.

Then, after invoking $\col@par to ensure to be in vertical mode, we <math>\col@balize \@svsechd$ and $\@svsec which may be defined in a lower-level sectioning command such as <math>\paragraph$ in the spanning text so that they are properly expanded in \everypar inserted at the beginning of the first paragraph of the column to which we switch shortly, even when the sectioning command is used inappropriately in the spanning text. We also $\globalize \everypar$ by a sequence with three \everypar so that $\pcol@output@switch$ for the synchronized column-switching we make shortly broadcasts it to other columns. Finally after closing the group, we let $\pcol@nextcol = d$ and $\pcol@sync = true$ to set another synchronization point below the spanning text and to make the captured text combined with pre-spanning-text stuff, and then invoke $\pcol@switchcol$ to switch the column d.

```
2396 \long\def\pcol@sptext[#1]{%
2397 \@tempcnta\pcol@nextcol
```

```
2398 \global\pcol@synctrue \pcol@nextcol\z@
```

```
2399 \global\pcol@sptextstarttrue
```

```
2400 \pcol@switchcol
```

```
2401 \global\pcol@sptextstartfalse \global\pcol@sptexttrue
```

```
2402 \begingroup
```

```
2403 \columnwidth\textwidth \hsize\columnwidth
```

```
2404 \linewidth\columnwidth \advance\linewidth-\pcol@lrmargin
```

```
2405 \ifdim\pcol@lrmargin>\z@ \parshape\@ne\@totalleftmargin\linewidth \fi
```

2406 \col@number\@ne #1\pcol@par

```
2407 \global\let\@svsechd\@svsechd \global\let\@svsec\@svsec
```

 $\label{eq:loss} $$ $$ expandafter\global\expandafter\everypar\expandafter{\the\everypar}% $$$

```
2409 \endgroup
```

2410 \pcol@nextcol\@tempcnta \global\pcol@synctrue \pcol@switchcol}

```
2411
```

\pcol@switchcol The macro \pcol@switchcol is invoked from \pcol@switchcolumn, \pcol@iswitchcolumn,

 $\colored counters$ in the current column c into Θ_c by $\colored counters$. First, we save

Next, if $\ true$, we do the followings. At first we let $V_E = \$ vspace have the natural component of \pcol@ensurevspace which can have a glue specified by \ensurevspace, so that it is referred to by \pcol@sync as the minimum space required below the synchronization point we are now setting. Second, we invoke \pcol@visitallcols temporarily turning $\ for column-scanning to visit all columns but current$ one to give TFX's page builder the chance to break column-pages in the top page with page-wise footnotes which could have not been presented in the last visit of the columns. Third, we make an vutput request with $\operatorname{penalty} = \operatorname{pcol}@op@switch to invoke <math>\operatorname{pcol}@output@switch by$ \colline{line} vector with \ifty to the column vector with \ifty to the column vector d. This invocation may result in $\iftheta = true$ to mean the top page should be broken before setting the synchronization point. Therefore if so, since \pcol@output@switch switched to the tallest column rather than d, we put \vfil and \penalty-10000 to force page break, make column-scan with \newpage put into each column to have some floats in the column in the new top page, and then invoke \pcol@output@switch again until it returns ifpcol@flush = false telling us it successfully sets the synchronization point switching to the column d. Then as the last operation specific to synchronized column-switching, we invoke **\ensurevspace** with **\baselineskip** to give the default of V_E for the next synchronization.

Otherwise, i.e., if $\formula for \pcol@sync = false$, we simply make the $\output request$ for $\pcol@output@switch to switch to the column d.$

Then we scan Θ_d applying \pcol@setctrelt to each $\langle \theta^l, val_d(\theta^l) \rangle \in \Theta_d$ to let $val(\theta^l) = val_d(\theta^l)$. We also scan $T = \col@aconly applying \col@aconlyelt to each <math>\langle t_c, c \rangle \in T$ to inhibit \addcontentsline to the contents file of type t_d as specified so by \addcontentsonly $\langle t_d \rangle$. After that, we let \@elt = \relax to make it sure that any lists can be manipulated without unexpected application of a macro to their elements.

Finally – unless we process the implicit $\col@switchol from \endparacol – we invoke \col@colpream.c, where <math>c = -1$ if \ifpcol@sptextstart = true to mean the column-switching is for a spanning text, or c = d otherwise.

2412 \def\pcol@switchcol{%

2413	\pcol@savecounters
2414	\ifpcol@sync
2415	\@tempdima\pcol@ensurevspace\relax
2416	\edef\pcol@@ensurevspace{\number\@tempdima sp\relax}%
2417	\global\pcol@syncfalse \pcol@visitallcols\@@par \global\pcol@synctrue
2418	\pcol@invokeoutput\pcol@op@switch
2419	\@whilesw\ifpcol@flush%
2420	\vfil \penalty-\@M
2421	\global\pcol@syncfalse \pcol@visitallcols\newpage \global\pcol@synctrue
2422	\pcol@invokeoutput\pcol@op@switch}%
2423	\ensurevspace{\baselineskip}%
2424	\else
2425	\pcol@invokeoutput\pcol@op@switch
2426	\fi
2427	\let\@elt\pcol@setctrelt
2428	\csname pcol@counters\number\pcol@currcol\endcsname
2429	<pre>\let\@elt\pcol@aconlyelt \pcol@aconly \let\@elt\relax</pre>
2430	\@ifundefined{pcol@lastcol}{%
2431	$\label{eq:linear} \label{eq:linear} eq:$
2432	}{}}

2433

```
\colorisitallcols The macro \colorisitallcols (cs), invoked from \colorisitchcol and \colorishclear,
                 performs column-scanning putting \langle cs \rangle into the visited columns. That is, we repeat the in-
                 vocation of \col@output@switch to visit d through \col@invokeoutput with \penalty =
                  have a chance of or to force page break in each visited column-page. Finally we go back to c
                 to restore its column-context especially when we are leaving the column 0 for spanning text.
                 That is, \kappa_c(\sigma) and \kappa_c(\varepsilon) should be presented to \pcol@output@switch to broadcast them to
                 other columns.
```

```
2434 \def\pcol@visitallcols#1{\begingroup
2435
      \@tempcnta\z@ \@tempcntb\pcol@currcol
      \@whilenum\@tempcnta<\pcol@ncol\do{%
2436
        \ifnum\@tempcnta=\@tempcntb\else
2437
          \pcol@nextcol\@tempcnta \pcol@invokeoutput\pcol@op@switch #1%
2438
2439
        \fi
        \advance\@tempcnta\@ne}%
2440
      \pcol@nextcol\@tempcntb \pcol@invokeoutput\pcol@op@switch
2441
      \endgroup}
2442
2443
```

\column The macros \pcol@com@column(*), the implementations of the environment-local API com-\column* mands \column(*), starts the environment column(*). Basically, the macros do \switch \pcol@con@column column(*), but if the environment starts just after \begin{paracol} the macro have to switch \pcol@com@column* to the column 0. Therefore, the definitions for this very-beginning appearance are given in \pcol@defcolumn \pcol@zparacol to do (almost) nothing, and then those for other ones are given by \pcol@ defcolumn invoked in \pcol@com@switchcolumn to invoke \pcol@switchenv{column(*)}(*) which then invokes \switchcolumn. Note that the definition of non-starred \pcol@com@column has \relax after the invocation of \pcol@switchenv so that \@ifnextchar and \@ifstar to examine the existence of '[' and '*' definitely tells us no even if the body of the environment starts with a '[' or '*'.

```
2444 \def\pcol@defcolumn{%
2445
      \gdef\pcol@com@column{\pcol@switchenv{column}\relax}%
2446
      \global\@namedef{pcol@com@column*}{\pcol@switchenv{column*}*}}
2447
```

```
\ macros \ pcol@com@nthcolumn(*)\langle d \rangle, \ pcol@com@leftcolumn(*) and \ pcol@com@right
                                                 \mathbf{API} are the implementations of environment-local API macros \mathbf{API}
             \pcol@com@nthcolumn \leftcolumn(*) and \rightcolumn(*) respectively. They start corresponding environments
         \condent \
                                                 leftcolumn (*), where (env) is the name of each environment, giving it d, 0 and 1 respectively as its optional
                                             \leftcolumn* argument for the target column.
        \label{eq:local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_local_
    \pcol@com@leftcolumn* 2449 \@namedef{pcol@com@nthcolumn*}#1{\pcol@switchenv{nthcolumn*}[#1]*}
                                             \rightcolumn 2450 \def\pcol@com@leftcolumn{\pcol@switchenv{leftcolumn}[0]\relax}
                                        \rightcolumn* 2451 \@namedef{pcol@com@leftcolumn*}{\pcol@switchenv{leftcolumn*}[0]*}
   \pcol@com@rightcolumn 2452 \def\pcol@com@rightcolumn{\pcol@switchenv{rightcolumn}[1]\relax}
\pcol@com@rightcolumn* 2453 \@namedef{pcol@com@rightcolumn*}{\pcol@switchenv{rightcolumn*}[1]*}
                                                                                                        2454
```

\pcol@switchenv The macro \pcol@switchenv $\langle env \rangle$ is invoked from \pcol@com@ $\langle env \rangle$ where $\langle env \rangle \in \{$ column (*), nthcolumn(*), leftcolumn(*), rightcolumn(*)} to invoke \switchcolumn with the arguments following $\langle env \rangle$ given by the invoker macros. Before invoking switchcolumn, we save

```
it in \reserved@a for the invocation and re\define it so that it will complain the illegal usage
of column-switching commands/environments in the environment (env) by \PackageError.
2455 \def\pcol@switchenv#1{\let\reserved@a\switchcolumn
2456 \def\switchcolumn{\PackageError{paracol}{%}
```

```
2457 Column switching commands and environments cannot be used in #1}\@eha}
2458 \reserved@a}
2459
```

```
\endcolumn The macro \pcol@com@endcolumn is the implementation of the environment-local API macro
              \endcolumn* \endcolumn to close column environment. The macro makes it sure we are in verti-
      \coll{com} of the very par so that it is saved in \kappa_c(\varepsilon) of the
     \comeq context column c on the switch to another column. The macro also gives the com-
            \endnthcolumn mon definition of \pcol@com@endcolumn* for \endcolumn*, \pcol@com@endnthcolumn(*) for
           \endnthcolumn* \endnthcolumn(*), \pcol@com@endleftcolumn(*) for \endleftcolumn(*), and \pcol@com@
  \pcol@com@endnthcolumn endrightcolumn(*) for \endrightcolumn(*).
  \label{eq:linear} \label{eq:linear} $$ \coldcom@endnthcolumn* $_{2460} \def\pcol@com@endcolumn{\pcol@par} } \label{eq:linear} $$
           \endleftcolumn 2461
                                \expandafter\global\expandafter\everypar\expandafter{\the\everypar}}
          \endleftcolumn* 2462 \expandafter\let\csname pcol@com@endcolumn*\endcsname\pcol@com@endcolumn
 \pcol@com@endleftcolumn 2463 \let\pcol@com@endnthcolumn\pcol@com@endcolumn
\pcol@com@endleftcolumn* 2464 \expandafter\let\csname pcol@com@endnthcolumn*\endcsname\pcol@com@endcolumn
          \endrightcolumn 2465 \let\pcol@com@endleftcolumn\pcol@com@endcolumn
         \endrightcolumn* 2466 \expandafter\let\csname pcol@com@endleftcolumn*\endcsname\pcol@com@endcolumn
\pcol@com@endrightcolumn

\pcol@com@endrightcolumn

pcol@com@endrightcolumn

2467 \let\pcol@com@endrightcolumn

2468 \expandafter\let\csname pcol@com@endrightcolumn*\endcsname\pcol@com@endcolumn
\pcol@com@endrightcolumn*
                          2469
   for the column c or that for spanning texts if c = -1. After assigning c to \@tempcnta to ensure
                          c is a number, the macro \collecolpream c is \defined to have \langle pream \rangle.
                          2470 \def\definecolumnpreamble#1#2{\@tempcnta#1\relax
                          2471
                                \expandafter\gdef\csname pcol@colpream\number\@tempcnta\endcsname{#2}}
                          2472
            \ensurevspace The API macro \ensurevspace{space} is to declare that the synchronization point following
       \points the page has the vertical (space) below the synchro-
      \ pcol@ensurevspace nization point. The macro makes a dummy assignment of \langle space \rangle to \ dtempdima to ensure the
                          argument is a dimension including forced one, or in other words to raise an error if not in this
                          macro rather than at the time \langle space \rangle is evaluated in \pcol@switchcol. Then \langle space \rangle is kept in
                          \col@ensurevspace so that \langle space \rangle is evaluated in \col@switchcol</code> for the synchronization
                          in question to pass the value to \col@sync through the macro \col@densurevspace = V_E,
                          especially when it has register references, for example to \baselineskip. To give the default
                          of \pcol@ensurevspace, we invoke \ensurevspace at the top level with \baselineskip.
                          2473 \def\ensurevspace#1{{\@tempdima#1\relax \gdef\pcol@ensurevspace{#1}}}
                          2474 \ensurevspace{\baselineskip}
                          2475
```

16 Disabling \addcontentsline

\addcontentsonly The API macro \addcontentsonly $\langle t \rangle \langle c \rangle$ makes the type t contents file written by com-\pcol@aconly mands appearing only in the column c. The macro simply add the pair $\langle t, c \rangle$ to the list

```
and lot so far, by the fact \collac@def t is defined, or abort execution by \PackageError.
                                                                                                                                 2476 %% Disabling \addcontentsline
                                                                                                                                 2477
                                                                                                                                2478 \def\addcontentsonly#1#2{%
                                                                                                                                                              \@ifundefined{pcol@ac@def@#1}
                                                                                                                                2479
                                                                                                                                                                           {\PackageError{paracol}{Unknown contents type #1}\@eha}\relax
                                                                                                                                 2480
                                                                                                                                                                \cons\pcol@aconly{{#1}{#2}}
                                                                                                                                 2481
                                                                                                                                 2482 \gdef\pcol@aconly{}
                                                                                                                                 2483
                                              \collaconlyelt The macro \collaconlyelt \langle t_d \rangle \langle d \rangle is invoked solely in \collaconlyeltcoll for the column-
                                                                                                                                 switching to column c, and is applied to each \langle t_d, d \rangle \in T to enable \addcontentsline for t_d if
                                                                                                                                 d = c by the invocation of \pcol@ac@def@.t_d with an argument enable, or to disable if d \neq c
                                                                                                                                 with disable.
                                                                                                                                 2484 \def\pcol@aconlyelt#1#2{%
                                                                                                                                 2485
                                                                                                                                                                \ifnum#2=\pcol@currcol \@nameuse{pcol@ac@def@#1}{enable}%
                                                                                                                                                                \else \@nameuse{pcol@ac@def@#1}{disable}%
                                                                                                                                 2486
                                                                                                                                 2487
                                                                                                                                                                \fi}
                                   \colored colored col
              \pcol@addcontentsline ac@caption to make \addcontentsline \let-equal to this macro, which does nothing but dis-
                                                                                                                                 carding three arguments, for disabling. The macro \pcol@addcontentsline is the LATEX's orig-
                                                                                                                                 inal \addcontentsline and is used in the macros mentioned above to let \addcontentsline
                                                                                                                                 act as original.
                                                                                                                                 2488 \def\pcol@gobblethree#1#2#3{}
                                                                                                                                 2489 \let\pcol@addcontentsline\addcontentsline
                                                                                                                                 2490
                                        \col@ac@def@toc The macro \col@ac@def@toc \end{areal} is invoked solely in \col@aconlyelt{toc} \col@acon
                        \pcol@ac@enable@toc or disable \addcontentsline according to (eord) by making \@sect \let-equal to \pcol@
                    \pcol@ac@disable@toc ac@enable@toc which is the LATEX's original \@sect, or to \pcol@ac@disable@toc respec-
                                                                                                                                 tively. The macro \collarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcollarcol
                                                                                                                                  \addcontentsline by making it \let-equal to \pcol@gobblethree, then invokes the original
                                                                                                                                  \@sect saved in \pcol@ac@enable@toc giving it all arguments a_1 to a_8, and finally enables it
                                                                                                                                 by making it let-equal to pcol@addcontentsline. Note that the argument a_7 is surrounded
                                                                                                                                 by { and } on the invocation of \cell{eq:conceal} (]' in a_7.
                                                                                                                                 2491 \def\pcol@ac@def@toc#1{%
                                                                                                                                                              \expandafter\let\expandafter\@sect\csname pcol@ac@#1@toc\endcsname}
                                                                                                                                 2492
                                                                                                                                 2493 \let\pcol@ac@enable@toc\@sect
                                                                                                                                 2494 \def\pcol@ac@disable@toc#1#2#3#4#5#6[#7]#8{%
                                                                                                                                 2495
                                                                                                                                                                \let\addcontentsline\pcol@gobblethree
                                                                                                                                 2496
                                                                                                                                                                 \pcol@ac@enable@toc{#1}{#2}{#3}{#4}{#5}{#6}[{#7}]{#8}%
                                                                                                                                                                 \let\addcontentsline\pcol@addcontentsline}
                                                                                                                                  2497
                                                                                                                                 2498
                                        \collectline \co
                                        \col@ac@def@lot \col@aconlyelt(t)(c) when t is lof or lot respectively. They invoke \col@ac@caption@
    \collectline densities a constraint of the theorem and theorem and the theorem and theorem a
\colored colored constraints able \colored constraint of the set of the set
                    \pcol@ac@caption@def
    \pcol@ac@caption@if@lof
    \pcol@ac@caption@if@lot
```

 $T = \text{pcol@aconly being empty at initial, after confirming we know the type t, one of toc, lof$

```
to let \contact{lcaption} = \contact{lcaption} and \contact{lcaption} are \totact{lcaption} are \totact{lcaption} and \contact{lcaption} and \contact{lcaption} are \totact{lcaption} and \contact{lcaption} are \contact{lcaption} and \contact{lcaption} and \contact{lcaption} are \contact{lcaption} and \contact{lcaption} are \contact{lcaption} and \contact{lcaption} and \contact{lcaption} and \contact{lcaption} are \contact{lcaption} and \contact{lcaption} and \contact{lcaption} and \contact{lcaption} are \contact{lcaption} and \contact{lcaption}
                                                                        equal to \@tempswatrue in default. That is, \pcol@ac@catption@if@.t lets \if@tempswa =
                                                                         true iff \  for t is to be enable.
                                                                        2499 \def\pcol@ac@def@lof#1{\onameuse{pcol@ac@caption@#1}{lof}}
                                                                        2500 \def\pcol@ac@def@lot#1{\@nameuse{pcol@ac@caption@#1}{lot}}
                                                                        2501 \def\pcol@ac@caption@enable{\pcol@ac@caption@def\@tempswatrue}
                                                                        2502 \def\pcol@ac@caption@disable{\pcol@ac@caption@def\@tempswafalse}
                                                                        2504 \expandafter\let\csname pcol@ac@caption@if@#2\endcsname#1}
                                                                        2505 \let\pcol@ac@caption@if@lof\@tempswatrue
                                                                        2506 \let\pcol@ac@caption@if@lot\@tempswatrue
                  \colored control \col
\pcol@ac@caption@latex ac@caption@def to do what \@caption do but with enabling/disabling \addcontentsline. At
                                                                         first, it invokes \colored ac@cation@if@t where t = \colored type to let \if@tempswa be true or
                                                                        false according to the enable/disable status of t. Then, after letting \
                                                                         \pcol@gobblethree for disabling if false, we invoke \pcol@ac@caption@latex, being the
                                                                         LATEX's original \@caption, giving all three arguments of \pcol@ac@caption itself surround-
                                                                        ing \langle lcap \rangle with { and } for the concealment of ']'. Finally, we let \addcontentsline =
                                                                         \pcol@addcontentsline so that other macros uses it with its original definition.
                                                                        2507 \log\ellac0caption#1[#2]#3{%}
                                                                        2508
                                                                                           \@nameuse{pcol@ac@caption@if@\@nameuse{ext@#1}}%
                                                                        2509
                                                                                           \if@tempswa\else \let\addcontentsline\pcol@gobblethree \fi
                                                                                           \pcol@ac@caption@latex{#1}[{#2}]{#3}%
                                                                        2510
                                                                                           \let\addcontentsline\pcol@addcontentsline}
                                                                        2511
                                                                        2512 \let\pcol@ac@caption@latex\@caption
                                                                        2513
```

Page Flushing Commands 17

\flushpage The macros \pcol@com@flushpage, \pcol@com@clearpage and \pcol@com@cleardoublepage \pcol@com@flushpage are the implementations of environment-local API macro \flushpage, \clearpage and \clearpage \cleardoublepage respectively. The first two have a common structure in which we at first in-\pcol@com@clearpage voke \pcol@flushclear for column-scan and pre-flushing column height check, and then make \cleardoublepage an \output request by \pcol@invokeoutput with \penalty being \pcol@op@flush or \pcol@ \pcol@com@cleardoublepage op@clear according to the commands. On the other hand the last one simply invokes \pcol@ com@clearpage unconditionally, and then \pcol@com@flushpage²³² if two-sided paging is enabled by if@twoside = true, we are in an even-numbered page, and ifpcol@paired = falseto mean we are not doing non-paired parallel-paging.

```
2514 %% Page Flushing Commands
2515
2516 \def\pcol@com@flushpage{\pcol@flushclear\voidb@x
     \pcol@invokeoutput\pcol@op@flush}
2517
2518 \def\pcol@com@clearpage{\pcol@flushclear\voidb@x
      \pcol@invokeoutput\pcol@op@clear}
2519
2520 \def\pcol@com@cleardoublepage{\pcol@com@clearpage
      \if@twoside \ifodd\c@page\else \ifpcol@paired\else \pcol@com@flushpage
2521
2522
      fi fi fi
```

 $^{^{232}}$ Unlike IAT_EX's \cleardoublepage, it is unnecessary to put an empty \hbox before \flushpage because it is active even at the top of a page.
Then we repeat pre-flushing column height check invoking $\col@output@switch through \col@invokeoutput with \penalty = \pcol@op@switch and \ifpcol@clear = \ifpcol@sync = true until the special \output routine finishes with \ifpcol@flush = false and <math>\langle box \rangle = \bot$, where $\langle box \rangle = \Phi = \col@topfnotes$ if this macro is invoked from \endparacol with non-merged page-wise footnote typesetting. In the repetition, we put $\fill and \penalty-10000$ to force page break into the tallest column, temporarily turning \ifpcol@lastpage = false using \ifpcol@lastpagesave because the broken page is not last one, each time the pre-flushing column height check tells us to do it. That is, we repeat the check while we have too tall columns due to page-wise footnotes or, when closing paracol environment, deferred non-merged page-wise footnotes.

Finally we let \ifpcol@clear have its default setting, i.e., false.

```
2523 \def\pcol@flushclear#1{\pcol@par
      \pcol@nextcol\pcol@currcol
2524
      \pcol@visitallcols\@@par
2525
      \pcol@cleartrue \global\pcol@synctrue
2526
      \ifpcol@lastpage \pcol@lastpagesavetrue \else \pcol@lastpagesavefalse \fi
2527
2528
      \pcol@invokeoutput\pcol@op@switch \ifvoid#1\else \global\pcol@flushtrue \fi
2529
      \@whilesw\ifpcol@flush\fi{%
2530
        \pcol@lastpagefalse
2531
        \vfil \penalty-\@M \pcol@cleartrue \global\pcol@synctrue
2532
        \ifpcol@lastpagesave \pcol@lastpagetrue \fi
        \pcol@invokeoutput\pcol@op@switch
2533
        \ifvoid#1\else \global\pcol@flushtrue \fi}%
2534
      \pcol@clearfalse}
2535
2536
```

18 Commands for Footnotes

\footnoteplacement The API macro \footnoteplacement{l} is to determine that footnotes are column-wise (l = c), \footnotelayout page-wise without merging (l = p), or merged and page-wise (l = m). The macro examines if \pcol@fnlayout@c $l \in \{c, p, m\}$ by the existence of the corresponding macro \pcol@fnlayout@·l and invokes it, or \pcol@fnlayout@p complains if not by \PackageError.

 $\label{eq:linear} $$ \ \ f_s = \ f_s$

l	f_s	f_m	f_a	footnote
с	false	false	false	local
р	true	false	true	global
m	true	true	true	global

Note that turning ifpcol@fncounteradjustment is done by fncounteradjustment (*true*) or nofncounteradjustment (*false*). Also note that the setting of ifpcol@fncounteradjustment and the globalization/localization of footnote are just to give defaults and thus can be overridden by API macros giving non-default settings. Another remark is

\footnotelayout
\pcol@fnlayout@c
\pcol@fnlayout@p
\pcol@fnlayout@m
\multicolumnfootnotes
\singlecolumnfootnotes
\mergedfootnotes

that backward-compatible macros \multicolumnfootnotes, \singlecolumnfootnotes and \mergedfootnotes are \let-equal to \pcol@fnlayout@c, \pcol@fnlayout@p and \pcol@ fnlayout@m respectively. If the deprecated \footnotelayout is undefined \let it equal to \footnoteplacement and add a hook to undefine it if footmisc gets loaded; print an informational message in any case where our \footnotelayout is unavailable.

```
2537 %% Commands for Footnotes
2538
2539 \def\footnoteplacement#1{\@ifundefined{pcol@fnlayout@#1}%
2540
      {\PackageError{paracol}{Unknown footnote layout specifier #1}}%
2541
      {\@nameuse{pcol@fnlayout@#1}}}
2542 \def\pcol@fnlayout@c{\global\pcol@scfnotefalse \global\pcol@mgfnotefalse
      \localcounter{footnote}\nofncounteradjustment}
2543
2544 \def\pcol@fnlayout@p{\global\pcol@scfnotetrue \global\pcol@mgfnotefalse
2545
      \globalcounter{footnote}\fncounteradjustment}
2546 \def\pcol@fnlayout@m{\pcol@fnlayout@p\global\pcol@mgfnotetrue}
2547
2548 \let\multicolumnfootnotes\pcol@fnlayout@c
2549 \let\singlecolumnfootnotes\pcol@fnlayout@p
2550 \let\mergedfootnotes\pcol@fnlayout@m
2551 \@ifundefined{footnotelayout}{%
2552
      \let\footnotelayout\footnoteplacement
2553
      \AddToHook{package/footmisc/before}{\let\footnotelayout\relax}%
2554 }{}
2555 \AddToHook{package/footmisc/before}{\PackageNoteNoLine{paracol}{%
2556
     With footmisc loaded, paracol's
      \string\footnotelayout\space will be unavailable. Please use the
2557
     equivalent \string\footnoteplacement\space instead.\MessageBreak
2558
     Also note, that paracol's and footmisc's footnote handling may crash%
2559
2560 }}
2561
```

 $\times target the macro \times target the target the target the target the target target the target targe$ $\colored text \ boundary \colored text \ boundary \ boundary$ \pcol@fntexttop original and our own are made \let-equal by \pcol@zparacol, our own is active throughout \pcol@fntextother the environment. The customization is done to examine if the footnote should be deferred and to encapsulate the footnote in a \vbox.

> The deferred footnote insertion is in effect if the footnote typesetting is page-wise and \footnote or \footnotetext appears in a page $p < p_t$. If so, we put the footnote $\langle text \rangle$ encapsulated in a vbox by vcol@fntextbody to the tail of $\Phi =$ vcol@topfnotes with \penalty\interlinepenalty preceding it for the split in \pcol@deferredfootins, using \pcol@fntextother{text} whose sole user is this macro. Note that the decision of deferring is done based on $p = \ colorage$ which could be less than that of the page in which the footnoted text appears because the paragraph having the text will have a page break before the text. Therefore, p for the footnote can be p_t , but this misjudgment will not cause problems because the footnote will eventually be put in p_t through Φ when the page break occurs.

> Otherwise the footnote $\langle text \rangle$ is processed by \pcol@fntexttop{text}, also used solely in this macro, to \insert it through \footins as usual but after the encapsulation by \pcol@ fntextbody and with \penalty\interlinepenalty following it to allow TEX's page builder to split footnotes.

> may have two or more paragraphs.

2562 \def\pcol@fntext{%

```
2563
      \let\reserved@a\pcol@fntexttop
      \ifpcol@scfnote \ifnum\pcol@page<\pcol@toppage
2564
        \let\reserved@a\pcol@fntextother
2565
      \fi\fi
2566
      \reserved@a}
2567
2568 \long\def\pcol@fntexttop#1{%
      \pcol@Logfn{\pcol@fntexttop{\@thefnmark}}%
2569
      \insert\footins{\pcol@fntextbody{#1}\penalty\interlinepenalty}}
2570
2571 \long\def\pcol@fntextother#1{%
      \global\setbox\pcol@topfnotes\vbox{\unvbox\pcol@topfnotes
2572
        \penalty\interlinepenalty\pcol@fntextbody{#1}}}
2573
```

\pcol@fntextbody The macro \pcol@fntextbody{text}, invoked from \pcol@fntexttop and \pcol@fntext other, encapsulates the footnote $\langle text \rangle$ in a vbox whose height is $h_{\text{max}} = \text{textheight-\skip}$ \footins at tallest. The encapsulation is to inhibit page breaks in a footnote because the split by the break will make some skips and other items eliminated causing a weird result when split portions are *joined*. The height capping is thus required to find a page in which the footnote resides.

> The macro at first does operations done in $L^{A}TFX$'s \@footnotetext to put $\langle text \rangle$ in $\det p = \det r$ when page-wise footnote typesetting is in effect. Note that this part is blindly copied from the original though it should be meaningless to set \interlinepenalty, \splittopskip, splitmaxdepth and floatingpenalty because (text) is encapsulated.

> Then the height-plus-depth of the box is compared with $h_{\rm max}$ and, if it exceeds the limit, the height of the box is set h_{max} , the footnote is made followed by a \vss to avoid overfull, and a warning message of too tall is put by \PackageWarning. Finally, the box is put into **\footins** or Φ by the invoker of this macro.

```
2574 \long\def\pcol@fntextbody#1{\setbox\@tempboxa\vbox{%
```

2575	\reset@font\footnotesize
2576	\interlinepenalty\interfootnotelinepenalty
2577	\splittopskip\footnotesep
2578	\splitmaxdepth \dp\strutbox \floatingpenalty \@MM
2579	\hsize \ifpcol@scfnote \textwidth \else \columnwidth \fi
2580	\def\@currentcounter{footnote}%
2581	\protected@edef\@currentlabel{%
2582	\csname p@footnote\endcsname\@thefnmark
2583	}%
2584	\color@begingroup
2585	\@makefntext{%
2586	\rule\z@\footnotesep\ignorespaces#1\@finalstrut\strutbox}%
2587	\par
2588	\color@endgroup}%
2589	\@tempdima\ht\@tempboxa \advance\@tempdima\dp\@tempboxa
2590	\@tempdimb\textheight \advance\@tempdimb-\skip\footins
2591	\ifdim\@tempdima>\@tempdimb
2592	\setbox\@tempboxa\vbox to\@tempdimb{\unvbox\@tempboxa\vss}%
2593	\PackageWarning{paracol}{Too tall footnote}%
2594	\fi
2595	\box\@tempboxa}
2596	

\fncounteradjustment The API macros \fncounteradjustment and \nofncounteradjustment turns \ifpcol@ \nofncounteradjustment fncounteradjustment true or false, to enable or disable the footnote counter adjustment letting \c@footnote = $b_f + n_f$ in \end{paracol}, respectively. After the definition we disable the adjustment to give the default setting.

```
2599 \nofncounteradjustment
2600
```

\pcol@footnoterule The macros \pcol@footnoterule, \pcol@@footnote, \pcol@@footnotemark and \pcol@@ \pcol@@footnote footnotetext are to keep the original definitions of \footnoterule, \footnote, \footnote \pcol@footnotemark mark and \footnotetext in them, respectively, so that we define our own versions with refer-\pcol@@footnotetext ences to the originals.

> 2601 \let\pcol@footnoterule\footnoterule 2602 \let\pcol@@footnote\footnote 2603 \let\pcol@@footnotemark\footnotemark 2604 \let\pcol@@footnotetext\footnotetext

\footnote The macros \pcol@footnote and \pcol@footnotemark are the implementations of our own \pcol@footnote versions of \footnote and \footnotemark which are made \let-equal to them by \pcol@ \pcol@ifootnote zparacol, respectively. The reasons why we need to have our own are two-fold; to have \footnotemark starred version of them; and to maintain $n_f = \colOnfootnotes$ for the footnote counter \pcol@footnotemark adjustment.

\pcol@ifootnotemark

The implementations of the starred versions \footnote*[num]{text} and \footnotemark* [num] have common structure in which we invoke $\pcol@adjustfnctr(macro)[num]$ if '*' is given, to let c@footnote have the number relative to $b_f = pcol@footnotebase$ or to itself. Then the macros \pcol@ifootnote or \pcol@ifootnotemark are invoked from \pcol@ adjustfnctr or the else-part of \@ifstar to perform the operations common to both cases with and without '*', i.e., invoking the original version \pcol@@footnote or \pcol@@footnotemark after incrementing n_f . One caution is that $\langle macro \rangle = \pcol@ifootnote for \footnote,$ but $\langle macro \rangle = \{ \ collifortnotemark \ relax \}$ for $\ otherwise \ that \ line \ relax \ relax \}$ \pcol@footnotemark invoked from \pcol@ifootnotemark eats \relax to terminate space skipping and thus spaces following [num] are kept.

2605 \def\pcol@footnote{\@ifstar{\pcol@adjustfnctr\pcol@ifootnote}\pcol@ifootnote} 2606 \def\pcol@ifootnote{\global\advance\pcol@nfootnotes\@ne \pcol@@footnote} 2607 \def\pcol@footnotemark{\@ifstar {\pcol@adjustfnctr{\pcol@ifootnotemark\relax}}% 2608\pcol@ifootnotemark} 2609 \pcol@@footnotemark} 2611

 $\colored just factor The macro \colored just factor (macro) [num], invoked from the then-part of \Colored just factor in$ \pcol@iadjustfnctr \pcol@footnote and \pcol@footnotemark, calculates the number to be set into \c@footnote \clicalcfnctr by $\clicalcfnctr(num)\clicalcfnctr processing the optional argument (num) by <math>\clicalcfnctr$ iadjustfnctr with default '+1', and then invoke $\langle macro \rangle$ being \pcol@ifootnote or \pcol@ ifootnotemark/relax. Since \pcol@calcfnctr returns the number \c@footnote should have and the counter is incremented by \stepcounter in \pcol@@footnote or \pcol@@ footnotemark, we decrement the counter prior to invoke $\langle macro \rangle$.

> The macro $\colecalcfnctr(num)\$ culate m specified by $\langle num \rangle$ as follows, where $f = \c@footnote$, to return it through \@tempcnta.

$$m = \begin{cases} f+k & \langle num \rangle = +k \\ f-k & \langle num \rangle = -k \\ b_f+k & \langle num \rangle = k \end{cases}$$

```
2612 \def\pcol@adjustfnctr#1{\@ifnextchar[%]
      {\pcol@iadjustfnctr{#1}}{\pcol@iadjustfnctr{#1}[+1]}}
2613
2614 \def\pcol@iadjustfnctr#1[#2] {\pcol@calcfnctr#2\@nil
      \global\c@footnote\@tempcnta \global\advance\c@footnote\m@ne#1}
2615
2616 \def\pcol@calcfnctr#1#2\@nil{\@tempcnta\c@footnote
      \def\reserved@a{#1}\def\reserved@b{+}%
2617
      \ifx\reserved@a\reserved@b \advance\@tempcnta#2\relax
2618
      \else \def\reserved@b{-}%
2619
2620
      \ifx\reserved@a\reserved@b \advance\@tempcnta-#2\relax
      \@tempcnta\pcol@footnotebase \advance\@tempcnta#1#2\relax
2621
2622
      \fi\fi}
```

\footnotetext The macros \pcol@footnotetext is the implementation of our own versions of \footnotetext \pcol@footnotetext which is made \let-equal to it by \pcol@zparacol. The reasons why we need to have our \pcol@ifootnotetext own is to have the starred version. That is, if '*' is not given, we simply invoke the original \pcol@iifootnotetext version \pcol@@footnotetext. Otherwise we invoke \pcol@ifootnotetext which then examines if the optional argument [num] is presented. If so, we invoke $\pcol@iifootnotetext$ in which pcol@calcfnctr(num) @nil is invoked to have the value m being the footnote ordinalwith which we invoke $\col@@footnotetext[m]$ with two $\col@footnotetext[m]$ from \Ctempcnta. Otherwise, i.e., [num] is not given, we increment \cCfootnote by \stepcounter before invoking \pcol@footnotetext.

```
2623 \def\pcol@footnotetext{\@ifstar\pcol@ifootnotetext\pcol@dfootnotetext}
2624 \def\pcol@ifootnotetext{\@ifnextchar[%]
      \pcol@iifootnotetext{\stepcounter{footnote}\pcol@@footnotetext}}
2625
2626 \def\pcol@iifootnotetext[#1] {\pcol@calcfnctr#1\@nil
2627
      \expandafter\pcol@@footnotetext\expandafter[\number\@tempcnta]}
2628
```

19**Commands for Marginal Notes**

 $\mbox{marginpar}$ The API macro $\mbox{marginnote}[left]{right}[voffset]$ given by the package marginnote is emu-\pcol@marginpar lated using \marginpar[left] {right} and \pcol@addmarginpar in \output routine. The basic $\colored constraint}$ mechanism is to pass the vertical offset $\langle voffset \rangle$ to $\colored constraint}$ through $\dimen \langle b \rangle$ \@mn@@marginnote where b is the \insert to carry $\langle left \rangle$. The offset passing is implemented as follows.

- \marginpar is made \let-equal to our own version \pcol@marginpar in \pcol@zparacol so that it \let the macro \pcol@mparoffset be \z@ and then invoke LATEX's original version kept in \pcol@@marginpar, because the marginal note given by \marginpar will not be shifted.
 - The internal macro \@mn@@marginnote[left]{right}[voffset] defined in marginnote is made \let-equal to our own version \pcol@marginnote in \pcol@zparacol so that it \defines \pcol@mparoffset to have $\langle voffset \rangle$ and then invoke \pcol@marginpar[left] {right} for the emulation. In the invocation, marginnote's typesetting macros \margin font, raggedleftmarginnote and raggedrightmarginnote are attached to $\langle left \rangle$ and $\langle right \rangle$.
 - LATFX's internal macro \Cxympar for the last operations of \marginpar is made \letequal to our own version in \pcol@zparacol so that it assigns the offset in \pcol@ mparoffset to \dimen\@marbox for $\langle left \rangle$, if \@floatpenalty < 0 to mean other macros for \marginpar have not detected any errors.

\pcol@marginnote \pcol@mn@warning \@xympar \pcol@xympar \pcol@@xympar \pcol@mparoffset In addition, we raise a warning that \marginnote is emulated by \pcol@mn@warning, which is made \let-equal to \relax in the caller \pcol@marginnote after the invocation so that the warning message is put just once.

```
2629 %% Commands for Marginal Notes
2630
2631 \def\pcol@marginpar{\let\pcol@mparoffset\z@ \pcol@@marginpar}
2632
    \long\def\pcol@marginnote[#1]#2[#3]{\endgroup
      \pcol@mn@warning \global\let\pcol@mn@warning\relax
2633
      \def\pcol@mparoffset{#3}%
2634
      \pcol@@marginpar[\marginfont\raggedleftmarginnote#1]%
2635
                       {\marginfont\raggedrightmarginnote#2}}
2636
2637 \def\pcol@mn@warning{%
2638
      \PackageWarning{paracol}{\string\margninnote\space is emulated by
2639
        \string\marginpar.}}
2640 \def\pcol@xympar{%
2641
      \ifnum\@floatpenalty<\z@ \global\dimen\@marbox\pcol@mparoffset\relax \fi
2642
      \pcol@@xympar}
2643
```

20 Two-Sided Typesetting

\twosided The API macro \twosided[T] where $T = t_1 t_2 \cdots$ is to enable/disable two-sided paging with \pcol@twosided \if@twoside = true/false ($p \in /\notin T$), two-sided column-swapping with \ifpcol@swapcolumn \pcol@twosided@p = true/false ($c \in /\notin T$), two-sided marginal note placement with \ifpcol@swapmarginpar = \pcol@twosided@c true/false ($m \in /\notin T$), and/or two-sided background painting with \ifpcol@bg@swap = \pcol@twosided@m true/false ($b \in /\notin T$) individually, or to enable all of them as a whole when the optional \pcol@twosided@b argument is not given.

\pcol@twosided@p
 \pcol@twosided@c
 \pcol@twosided@m
 \pcol@twosided@b
 \swapcolumninevenpages
 \noswapcolumninevenpages

\swapcolumninevenpages The macro invokes \pcol@twosided with the optional argument T if provided, or with \noswapcolumninevenpages T = pcmb otherwise to enable all features. Then \pcol@twosided at first turns all the switches false an then scans all non-space tokens $t \in T$ invoking \pcol@twosided@t if it is defined and thus $t \in \{p, c, m, b\}$ to turn the corresponding switch true, or complains that the feature t is unknown.

Note that backward-compatible API macros \swapcolumninevenpages and \noswapcolumn inevenpages are still available to turn \ifpcol@swapcolumn true an false respectively.

```
2644 %% Column Swapping
2645
2646 \def \twosided {\@ifnextchar [%]
      {\pcol@twosided}{\pcol@twosided[pcmb]}}
2647
    \def\pcol@twosided[#1]{%
2648
      \global\@twosidefalse \global\pcol@swapcolumnfalse
2649
      \global\pcol@swapmarginparfalse \global\pcol@bg@swapfalse
2650
2651
      \@tfor\reserved@a:=#1\do{%
        \@ifundefined{pcol@twosided@\reserved@a}%
2652
          {\PackageError{paracol}{Unknown two-siding feature \reserved@a}}%
2653
          {\@nameuse{pcol@twosided@\reserved@a}}}
2654
2655 \def\pcol@twosided@p{\global\@twosidetrue}
2656 \def\pcol@twosided@c{\global\pcol@swapcolumntrue}
2657 \def\pcol@twosided@m{\global\pcol@swapmarginpartrue}
2658 \def\pcol@twosided@b{\global\pcol@bg@swaptrue}
2659
2660 \def\swapcolumninevenpages{\global\pcol@swapcolumntrue}
```

2661 \def\noswapcolumninevenpages{\global\pcol@swapcolumnfalse} 2662

\pcol@swapcolumn The macro \pcol@swapcolumn $\langle c_1 \rangle \langle c_2 \rangle \langle C^0 \rangle \langle C^1 \rangle$ converts the column ordinal c or position c' \pcol@colsepid in the \count register²³³ c_1 to the position or ordinal to set it in the \count register c_2 , for a parallel-page having columns $c \in [C^0, C^1)$. That is, we let $c_2 = (C^1 - 1) - (c_1 - C^0)$ if $\times column = true$ to mean the column-swapping is in effect and $\column = true$ is even, while $c_2 = c_1$ otherwise. We also let $c^g = \collecolsepid = c_2 - 1$ if swapped, or $c^g = c_2$ otherwise, so that it has the ordinal of the column-separating gap *physically* following the column c_2 .

> The macro is used in \pcol@ioutputelt, \pcol@addmarginpar, \pcol@imakeflushedpage and $\colored colored colored$ with $(c_1, c_2) = (c, c')$. Note that in the uses in the macros above except for \pcol@ addmarginpar, \copage definitely has the page number for the page to be shipped out. As for \pcol@addmarginpar on the other hand, \c@page can be different from the ship-out page number to produce a weird result if their parities are different, due to page jump. However this problem is not so severe because it just affects the position of marginal notes which LATEX itself may misplace.

```
2663 \def\pcol@swapcolumn#1#2#3#4{%
      \edef\pcol@colsepid{\number#1}%
2664
      \ifpcol@swapcolumn
2665
2666
        \ifodd\c@page\relax #2#1\relax
2667
        \else
          #2#4\relax \advance#2-#1\relax \advance#2#3\relax \advance#2-\tw@
2668
          \edef\pcol@colsepid{\number#2}%
2669
          \advance#2\@ne
2670
2671
        \fi
      \else #2#1\relax
2672
2673
      \fi}
2674
```

\marginparthreshold The API macro \marginparthreshold $\{t_i\}$ [t_r] determines the smallest ordinal t_i of columns \pcol@marginparthreshold in left parallel-pages whose marginal notes go to the right margin in fundamental setting of \pcol@mpthreshold@l marginal note positioning, while the threshold in right parallel-pages is given by t_r if provided \pcol@mpthreshold@r or by t_l otherwise. That is, marginal notes given in a column c in a page p s.t. $c \in [0, C_L)$ (resp. $[C_L, C)$ go left if $c < t_l$ (resp. $c < t_r$) while they go right if $c \ge t_l$ (resp. $c \ge t_r$), providing

 $(\ifty col@swapmarginpar \land page(p) \mod 2 = 0) \not\equiv \ifty col@swapmarginpar = false$

or the margins are swapped otherwise.

The macro \defines \pcol@mpthreshold@l to let it have t_l after a assigning t_l to \@tempcnta to ensure t_l gives some number, and then do the same for \pcol@mpthreshold@ **r** with t_r by \pcol@marginparthreshold if t_r is provided, or let the macro have t_l otherwise. Note that at the top level we do \marginparthreshold{1} to give defaults. Also note that \pcol@mpthreshold@l and \pcol@mpthreshold@r are referred to solely in \pcol@ addmarginpar.

```
2675 \def\marginparthreshold#1{\@tempcnta#1\relax
      \xdef\pcol@mpthreshold@l{\number\@tempcnta}%
2676
2677
      \@ifnextchar[%]
        \pcol@marginparthreshold{\xdef\pcol@mpthreshold@r{\number\@tempcnta}}}
2678
```

 $^{^{233}}$ Or the \dimen register \z0.

```
2679 \def\pcol@marginparthreshold[#1] {\@tempcnta#1\relax
      \xdef\pcol@mpthreshold@r{\number\@tempcnta}}
2680
2681 \mbox{marginparthreshold}{1}
2682
```

$\mathbf{21}$ Commands for Text Coloring

 $\operatorname{columncolor}$ The API macro $\operatorname{columncolor}[mode]{color}[c]$ defines the default color specified by $\langle color \rangle$ \pcol@xcolumncolor optionally with color (mode) of the column c being the current column or that speci-\pcol@ycolumncolor fied by the optional argument. After \defining \pcol@colorcommand being the \string **\pcol@columncolor** of this macro itself, and processing two optional arguments $\langle mode \rangle$ and c through macros \pcol@xcolumncolor, \pcol@ycolumncolor and \pcol@columncolor, the macro \pcol@ icolumncolor{cmd}[c] is invoked to perform real operations with the coloring command $\langle cmd \rangle = \operatorname{color}[mode] \{ color \}.$ 2683 %% Commands for Text Coloring 2684

```
2685 \def\columncolor{\def\pcol@colorcommand{\string\columncolor}%
2686
     \ [\%]
        \pcol@xcolumncolor\pcol@ycolumncolor}
2687
2688 \def\col@xcolumncolor[#1]#2{\pcol@columncolor{\color[#1]{#2}}}
2689 \def\pcol@ycolumncolor#1{\pcol@columncolor{\color{#1}}}
2690 \def\pcol@columncolor#1{\@ifnextchar[%]
     {\pcol@icolumncolor{#1}}{\pcol@icolumncolor{#1}[\number\pcol@currcol]}}
2691
```

 $\$ normal column color The API macro $\$ normal column color [c] defines the default color of the column c, being the current column or that specified by the optional argument, is \normalcolor. That is, after \defining \pcol@colorcommand being the \string of this macro itself, this macro simply invokes \pcol@icolumncolor{cmd}[c] to perform real operations with the coloring command $\langle cmd \rangle =$ \normalcolor.

```
2692 \def\normalcolumncolor{\def\pcol@colorcommand{\string\normalcolumncolor}%
      \@ifnextchar[%]
2693
        {\pcol@icolumncolor\normalcolor}%
2694
        {\pcol@icolumncolor\normalcolor[\number\pcol@currcol]}}
2695
```

 $\colored column color The macro \colored column color {cmd}[c], invoked from \colored column color and \normal$

 \clicolumncolor columncolor, performs the operations to define the default color of the column c with the col- $\colorscancst@shadow oring command (cmd) \in \{\color[mode] \{ color \}, \colorscancst@shadow oring command (cmd) \in \{\color[mode] \} \}$ if \set@color is not \relax and we are in non-internal vertical or non-restricted horizontal mode and, if not, we complain the command whose name is in \pcol@colorcommand is ineffective by \PackageWarning and do nothing.

> Otherwise and if we are not in a paracol environment, i.e., \paracol is not \let-equal to \pcol@paracol, we simply invoke \pcol@iicolumncolor to let $\hat{\gamma}_0^c = \$ have the color χ specified by $\langle cmd \rangle$ so that the next \begin{paracol} will let γ_0^c have the coloring \special for χ . If we are in a paracol environment but in a column $c' \neq c$, on the other hand, we also let $\hat{\gamma}_0 = \chi$ but in addition let $\gamma_0^c = \text{pcol@columncolor@box} \cdot c$ have the coloring **\special** for χ immediately so that it is effective in the next column-switching to c. This immediate setting of γ_0^c is done by invoking $\langle cmd \rangle$ with the original \set@color saved in \pcol@set@color and the nullification of \aftergroup, after acquiring an \insert for it if necessary,

> Otherwise, i.e., if we are in a paracol environment and in the column c, at first we invoke \pcol@scancst@shadow to rewind $\hat{\Gamma}^c$ applying \@elt = \reset@color to $\hat{\gamma}_i \in \hat{\Gamma}^c$. Then, after

letting $\hat{\gamma}_0^c = \chi$, we invoke \pcol@scancst@shadow again to reestablish $\hat{\Gamma}^c$ with the new $\hat{\gamma}_0^c$ so that $\hat{\gamma}_0^c$ is at the bottom of the color stack in .tex. In this scan \@elt $\langle \hat{\gamma}_i \rangle$ \defines \current@ color to let it have $\hat{\gamma}_i$ and then invokes \pcol@set@color to put the coloring \special for $\hat{\gamma}_i$ nullifying \aftergroup. Then we \insert a \vbox, whose height and depth are 1pt and width is 0, having the coloring \special for χ so that \output will let γ_0^c have the \special in a synchronous manner. After that we put a \penalty = 10000 if \if@nobreak = true to keep the \insertion from being followed by a page break.

The macro \pcol@iicolumncolor $\langle cmd \rangle \langle c \rangle$ at first invokes $\langle cmd \rangle$ to let \current@color have the printer-specific color information χ of $\langle color \rangle$ or what \normalcolor specifies, temporarily letting \set@color be \relax to let \color or \normalcolor just do the \definition of \current@color without putting coloring \specials nor preparing color stack popping. Then we \xdefine $\hat{\gamma}_0^c = \pcol@columncolor \cdot c$ to have χ .

The macro $\collocalcost@shadow applies \@elt to <math>\hat{\gamma}_0^c$ to put a coloring or uncoloring $\special for it if it is defined, and then do the same for all <math>\hat{\gamma}_i \in \hat{\Gamma} = \col@colorstack@shadow.$ 2696 \def\pcol@icolumncolor#1[#2]{%

```
2697
      \@tempswafalse
2698
      \ifpcol@inner \@tempswatrue \fi
2699
      \ifinner
                     \@tempswatrue \fi
      \ifmmode
                     \@tempswatrue \fi
2700
      \ifx\set@color\relax
2701
        \PackageWarning{paracol}{\pcol@colorcommand\space is not effective
2702
          without some coloring package}%
2703
2704
      \else\if@tempswa
        \PackageWarning{paracol}{\pcol@colorcommand\space is not effective
2705
          when not in outer par mode}%
2706
2707
      \else
2708
        \begingroup
2709
        \let\@elt\relax
2710
        \ifx\pcol@paracol\paracol
           \pcol@iicolumncolor{#1}{#2}%
2711
        \else\ifnum#2=\pcol@currcol
2712
          \def\@elt##1{\reset@color}\pcol@scancst@shadow
2713
2714
           \pcol@iicolumncolor{#1}{#2}%
2715
           \def\@elt##1{\def\current@color{##1}\let\aftergroup\@gobble
             \pcol@set@color}%
2716
          \pcol@scancst@shadow
2717
2718
           \setbox\@tempboxa\vbox{\let\set@color\pcol@set@color
2719
            \let\aftergroup\@gobble #1}%
          \ht\@tempboxa1sp \dp\@tempboxa1sp \wd\@tempboxa\z@\relax
2720
          \insert\pcol@colorins{\box\@tempboxa}%
2721
          \ifvmode\if@nobreak \nobreak \fi\fi
2722
2723
        \else
          \pcol@iicolumncolor{#1}{#2}%
2724
2725
          \pcol@currcol#2\relax
2726
          \ifvoid\pcol@ccuse{@box}%
            \@next\@currbox\@freelist{}\pcol@ovf
2727
            \pcol@ccxdef{\@currbox}%
2728
2729
          \fi
           \global\setbox\pcol@ccuse{@box}\vbox{\let\set@color\pcol@set@color
2730
            \let\aftergroup\@gobble #1}%
2731
        \fi\fi
2732
2733
        \endgroup
2734
      \fi\fi
```

```
2735 \ignorespaces}
2736 \def\pcol@iicolumncolor#1#2{{\let\set@color\relax #1%
2737 \expandafter\xdef\csname pcol@columncolor#2\endcsname{\current@color}}}
2738 \def\pcol@scancst@shadow{%
2739 \pcol@ifccdefined{\@elt{\pcol@ccuse{}}\relax
2740 \pcol@colorstack@shadow}
2741
```

\pcol@mcpushlimit The macro \pcol@set@color@push is invoked whenever LATEX's counterpart \set@color ap-\set@color pears in a paracol environment through coloring commands such as \color, because \pcol@ \pcol@set@color zparacol replaces LATEX's macro with it saving the original version in \pcol@set@color, if \pcol@set@color@push the original \set@color is not \relax to mean some coloring package is in use. This original version is used through \pcol@set@color by \pcol@bg@paintregion@i, \pcol@output@ start and \pcol@icolumncolor besides this macro \pcol@set@color@push, while \output lets \set@color = \pcol@set@color for the references outside of our control.

The macro at first invokes its original version being \pcol@set@color to put an appropriate coloring \special to .dvi and reserve the invocation of \reset@color by \aftergroup. Then, it performs one of two different operations depending on TeX's mode, i.e., math mode or not. If we are in math mode and not in a \vbox, at first we increment $m = \pcol@mcid$ and examine if $m > \pcol@mcpushlimit = 1000$, and if so we stop the execution with $\pcol@reset@color@mpop@.m$ are defined²³⁵. Otherwise, i.e., if $m \le \pcol@mcpushlimit$, we reserve the invocation of the macro $\pcol@reset@color@mpop@.i$ for our own pop by \aftergroup defining the macro as $\pcol@reset@color@mpop{m}$. If we are not in math mode, on the other hand, and neither in a \box{vbox} nor in restricted horizontal mode, we simply reserve the invocation of the macro.

Then, regardless that we are in math mode or not, we push the contents of \current@color, which \set@color should refer to as the color information to be set, into the shadow color stack $\hat{\Gamma} = \col@colorstack@shadow$ for the stack rewinding/reestablishing in \columncolor and \normalcolumncolor. Since this push is done non-\globally with \edef, we save/restore the definition of \@elt to/from \pcol@elt@save before/after the push, respectively²³⁶. Then we \insert a \vbox through \pcol@colorins for the push of γ_i or $\gamma_{i,m}$ to Γ_r synchronous with a page break or column-switching. The height of the \vbox is 1 pt, depth is 0 and width is m sp if we are in math mode or 0 otherwise, and its contents is the coloring \special given by \pcol@ set@color so that the \special is what the macro put at the beginning of this macro but without the reservation of \reset@color. After the insertion, we put \pcol@fcwhyphenate, being \hskip\z@ when \coloredwordhyphenated is effective, to split the coloring \special from the first colored word so that the word may be hyphenated if we are in horizontal mode. If we are in vertical mode, on the other hand, we do \nobreak if \if@nobreak = true to keep the \insertion from being followed by a page break.

```
2742 \def\pcol@mcpushlimit{1000}
```

```
2743 \def\pcol@set@color@push{\pcol@set@color
```

```
2744 \ifmmode\else\ifinner \pcol@innertrue \fi\fi
```

```
2745 \ifpcol@inner\else
```

```
2746 \ifmmode
```

```
2747 \global\advance\pcol@mcid\@ne
```

²³⁴And let m = 1 to allow a user to continue the execution bravely.

```
^{236}\mathrm{Just} in case.
```

 $^{^{235}}$ We could make the number of math-mode coloring operations virtually unlimited by putting all digits of the decimal representation of m followed by a terminator by multiple \aftergroups so that \pcol@reset@color@mpop is put by \aftergroup prior to them to capture them as its argument, but limiting with $2^{31} - 1$ is still necessary and that with 1000 is reasonable.

2748	\ifnum \pcol@mcid>\pcol@mcpushlimit\relax
2749	\PackageError{paracol}{Too many coloring commands in math mode}\@ehb
2750	\global\pcol@mdid\@ne
2751	\fi
2752	\@tempdima\pcol@mcid sp\relax
2753	\expandafter\aftergroup
2754	\csname pcol@reset@color@mpop@\number\pcol@mcid\endcsname
2755	\expandafter\xdef
2756	\csname pcol@reset@color@mpop@\number\pcol@mcid\endcsname
2757	{\noexpand\pcol@reset@color@mpop{\number\pcol@mcid}}%
2758	\else
2759	\aftergroup\pcol@reset@color@pop \@tempdima\z@
2760	\fi
2761	\let\pcol@elt@save\@elt \let\@elt\relax
2762	\edef\pcol@colorstack@shadow{\pcol@colorstack@shadow\@elt{\current@color}}%
2763	\let\@elt\pcol@elt@save
2764	\setbox\@tempboxa\vbox{\let\aftergroup\@gobble \pcol@set@color}%
2765	\ht\@tempboxa1sp \dp\@tempboxa\z@ \wd\@tempboxa\@tempdima
2766	\insert\pcol@colorins{\box\@tempboxa}\ifhmode \pcol@fcwhyphenate \fi
2767	\ifvmode\if@nobreak \nobreak \fi\fi
2768	\fi}
2769	

\pcol@reset@color@pop The macro \pcol@reset@color@pop and its math-mode relative \pcol@reset@color@pop $\coloreset@color@mpop {m} are invoked by \aftergroup mechanism in \col@set@color@push, directly for the former$ and through the macro $\color@mpop@.m$ for the latter. They \insert a \box{vbox} for γ_i^- or $\gamma_{i,m}^-$ to add it to Γ_r synchronously with a page break or column-switching. Therefore, the height and depth of the \vbox are 0 and width is 0 for γ_i^- or $m \operatorname{sp}$ for $\gamma_{i,m}^-$. The contents of the \vbox is an uncoloring \special given by \reset@color but this is done just for debugging to show what \pcol@colorins has by, for example, \pcol@ShowBox. Then if we are in vertical mode and if@nobreak = true, we do nobreak to keep the insertion from being followed by a page break even in \pcol@reset@color@mpop because its corresponding \pcol@set@color@ push may have been in a displayed math construct after which we are in vertical mode.

> One caution is that \pcol@reset@color@pop can be invoked outside the paracol environment in which the corresponding \pcol@set@color@push appears. In this case with ifpcol@output = false, we don't need to do the pop operation and cannot make the \insertion for it because \output is not for paracol.

```
2770 \def\pcol@reset@color@pop{%
```

```
2771
      \ifpcol@output
```

```
2772
        \setbox\@tempboxa\vbox{\reset@color}%
```

```
\ht\@tempboxa\z@ \dp\@tempboxa\z@ \wd\@tempboxa\z@
2773
```

```
2774
        \insert\pcol@colorins{\box\@tempboxa}%
```

```
2775
        \ifvmode\if@nobreak \nobreak \fi\fi
```

```
2776
       \fi}
```

```
2777 \def\pcol@reset@color@mpop#1{%
```

```
\setbox\@tempboxa\vbox{\reset@color}%
2778
```

```
\ht\@tempboxa\z@ \dp\@tempboxa\z@ \wd\@tempboxa#1sp\relax
2779
```

```
\insert\pcol@colorins{\box\@tempboxa}%
2780
```

```
\ifvmode\if@nobreak \nobreak \fi\fi
2781
```

```
2782 }
```

```
2783
```

\coloredwordhyphenated The API macro \coloredwordhyphenated \defines the macro \pcol@fcwhyphenate being \nocoloredwordhyphenated \hskip\z@ so that the null space is inserted after the coloring \special and \insert put by \pcol@fcwhyphenate \pcol@set@color@push if we are in horizontal mode, so that the word following them can be hyphenated. The other API macro \nocoloredwordhyphenated makes \pcol@fcwhyphenate =

> \relax to inhibit the insertion. Since the null skip is a line break candidate, the skip might cause an unexpected and undesirable line break. However, this demerit is less important than the merit of making it possible to hyphenate the first word in multi-column documents with narrow lines, and thus we make \coloredwordhyphenated effective in default while giving users a means to disable the insertion (occasionally) by \nocoloredwordhyphenated.

 $2784 \def\coloredwordhyphenated{\def\pcol@fcwhyphenate{\hskip\z@}}$ $2786 \coloredwordhyphenated$ 2787

22Commands for Column-Separating Rule Color and **Background Painting**

colseprulecolor The macro $colseprulecolor[mode]{color}[c] \ defines \ pcol@colseprulecolor to have$ $\colordef{cseprulecolorder}$ the $\langle color \rangle$ optionally with coloring $\langle mode \rangle$ of all column-separating rules if the optional argu- $\colored efficiency ment c is not provided, or \colored efficience of the rule drawn between a particu \coll def cseprule color lar column pair c and c+1.$ After $\defining \coll color command to be \colseprule color in$ \normalcolseprulecolor case we have to give a warning, the macro invokes \pcol@defcseprulecolor@x[mode]{color} \pcol@defcseprulecolor@i or \pcol@defcseprulecolor@y{color} according to the provision of the optional argument $\color delta color della col$ so that this macro invokes $\color@i{cmd}[c]$ where $c = \emptyset$ if the optional argument c is not provided.

> The macro $\mbox{normalcolseprulecolor}[c]$, on the other hand, defines $\pcol@colseprule$ $color[\cdot c]$ with whatever \normalcolor gives, and thus it invokes \pcol@defcseprulecolor@i letting $\langle cmd \rangle =$ \normalcolor, after \defining \pcol@colorcommand to be \normalcolsep rulecolor.

> The macro $\cole def cseprule color @i{cmd}[c] examines if <math>\cole color = \cole to$ mean no coloring packages have been loaded and, if so, do nothing giving a warning the command in \colorcommand is not effective. Otherwise, we examine if $\langle cmd \rangle$ has proper arguments by invoking it but temporally nullifying \set@color and then \define $\colecolseprulecolor[\cdot c]$ to be $\langle cmd \rangle$.

> Note that at the top level we \define \pcol@colseprulecolor to be \normalcolor to give the default for all column-separating rules. Also note that macros $\colecolseprulecolor c$ are referred to solely in \pcol@fil which also uses \pcol@colseprulecolor for columns for which $\col@colseprulecolor.c$ is not defined.

2788 %% Commands for Column-Separating Rule Color and Background Painting 2789

```
2790 \def\colseprulecolor{\def\pcol@colorcommand{\string\colseprulecolor}%
      \@ifnextchar[%]
2791
        \pcol@defcseprulecolor@x\pcol@defcseprulecolor@y}
2792
```

```
2793 \def\pcol@defcseprulecolor@x[#1]#2{\pcol@defcseprulecolor{\color[#1]{#2}}}
```

```
2794 \def\pcol@defcseprulecolor@y#1{\pcol@defcseprulecolor{\color{#1}}}
```

```
2795 \def\pcol@defcseprulecolor#1{\@ifnextchar[%]
```

```
{\pcol@defcseprulecolor@i{#1}}{\pcol@defcseprulecolor@i{#1}[]}}
2796
```

```
2797 \def\normalcolseprulecolor{%
```

```
\def\pcol@colorcommand{\string\normalcolseprulecolor}%
2798
      \@ifnextchar[%]
2799
        {\pcol@defcseprulecolor@i\normalcolor}%
2800
        {\pcol@defcseprulecolor@i\normalcolor[]}}
2801
2802
    \def\pcol@defcseprulecolor@i#1[#2]{%
      \ifx\set@color\relax
2803
        \PackageWarning{paracol}{\pcol@colorcommand\space is not effective
2804
          without some coloring package }%
2805
2806
      \else
        {\let\set@color\relax #1}%
2807
        \global\@namedef{pcol@colseprulecolor#2}{#1}%
2808
2809
      \fi}
2810 \gdef\pcol@colseprulecolor{\normalcolor}
2811
```

 \backgroundcolor The macro $\backgroundcolor{region}[mode]{color}$ defines the $\langle color \rangle$ optionally with $\backgroundcolor \langle mode \rangle$ of the $\langle region \rangle$ whose syntax is specified as follows.

\nobackgroundcolor
\pcol@backgroundcolor@e
 \pcol@backgroundcolor@i
 \pcol@backgroundcolor@ii
 \pcol@backgroundcolor@iii
 \pcol@backgroundcolor@iv
 \pcol@backgroundcolor@iv

```
 \begin{array}{l} \langle region \rangle ::= \langle regionid \rangle \langle extension \rangle \\ \langle regionid \rangle ::= \langle a \rangle \mid \langle corg \rangle [c] \\ \langle a \rangle ::= \langle corg \rangle \mid \mathbf{s} \mid \mathbf{S} \mid \mathbf{t} \mid \mathbf{T} \mid \mathbf{l} \mid \mathbf{L} \mid \mathbf{r} \mid \mathbf{R} \mid \mathbf{f} \mid \mathbf{F} \mid \mathbf{n} \mid \mathbf{N} \mid \mathbf{p} \mid \mathbf{P} \\ \langle corg \rangle ::= \mathbf{c} \mid \mathbf{C} \mid \mathbf{g} \mid \mathbf{G} \\ \langle extension \rangle ::= \emptyset \mid (x_0, y_0) \mid (x_0, y_0) (x_1, y_1) \end{array}
```

On the other hand, the counterpart macro \oldsymbol{region} undefines the color of $\langle region \rangle$. Both macros invoke $\clossed{pcollbackgroundcolor}$ giving all arguments to it to parse the argument $\langle region \rangle$, after letting $f_{def} = \ifletempswa = true$ and $\clossed{pcollbackgroundcolor} = \close{pcollbackgroundcolor} = \close{pcollbackgroundcollbackgroundcollba$

Then the macro $\colobackgroundcolor examines if \colobg@@.a is defined, and if$ not, raises an error that a is invalid and then, in case the user dare to continue the exe $cution, invokes <math>\colobackgroundcolor@e to throw all arguments away after letting a' =$ $<math>\colobg@region = xx$ so that the undefining $\colobg@color.a'$ does not cause any troubles. Otherwise, i.e., if $\colobg@@.a$ is defined, it invokes $\colobackgroundcolor@i[c]$ or $\colobackgroundcolor@i[c]$ or $\colobackgroundcolor@i[c]$ or $\colobackgroundcolor@i[c]$, after $\colobg@may$ havecol@.a is defined, and if not, raises an error again in a similar way, or otherwise invokes $\colobackgroundcolor@ii after re<math>\colobackgroundcolor@i]$ after $\colobackgroundcolor@i]$ after $\colobackgroundcolor@i]$ after re \colobac

Then if $f_{def} = true$, the macro \pcol@backgroundcolor@ii examines if \set@color = \relax, and if so it complains that any coloring packages have not been loaded and invokes \pcol@backgroundcolor@w just for throwing away optional arguments for extension and $[mode]\{color\}$. Otherwise, i.e., if \set@color \neq \relax, it invokes \pcol@backgroundcolor@ just for throwing away optional arguments for extension and $[mode]\{color\}$. Otherwise, i.e., if \set@color \neq \relax, it invokes \pcol@backgroundcolor@ just for throwing away optional arguments for extension and $[mode]\{color\}$. Otherwise, i.e., if \set@color \neq \relax, it invokes \pcol@backgroundcolor@ just for throwing away optional arguments for extension and $[mode]\{color\}$. Otherwise, i.e., if \set@color \neq \relax, it invokes \pcol@backgroundcolor@ just for throwing away optional arguments for extension and $[mode]\{color\}$. Otherwise, i.e., if \set@color \neq \relax, it invokes \pcol@backgroundcolor@ just for throwing away optional arguments for extension and $[mode]\{color\}$. Otherwise, i.e., if \set@color \neq \relax, it invokes \pcol@backgroundcolor@ just for throwing away optional arguments for extension and $[mode]\{color]\}$. Otherwise, i.e., if \set@color \neq \relax, it invokes \pcol@backgroundcolor@ just for throwing away optional arguments for extension and $[mode]\{color]\}$.

The macro $\clickgroundcolor@iii at first invokes <math>\clickgroundcolor@iii at first invokes \clickgroundcolor@ive for all <math>d \in \{1, r, t, b\}$ to have default (no) extensions. Then if (x_0, y_0) is provided, $\clickgroundcolor@ive for all <math>d \in \{1, r, t, b\}$ but with $e = x_0$ for $d \in \{1, r\}$ and with $e = y_0$ for $d \in \{t, b\}$. Further, if (x_1, y_1) is also provided, $\clickgroundcolor@ive for all <math>d \in \{1, r, t, b\}$ but with $e = x_0$ for $d \in \{t, b\}$.

bg@defext is invoked once again by \pcol@backgroundcolor@v for all $(d, e) \in \{(\mathbf{r}, x_1), (\mathbf{b}, y_1)\}$. Finally \pcol@backgroundcolor@v invokes \pcol@backgroundcolor@x, which is also invoked from \pcol@backgroundcolor@iii and \pcol@backgroundcolor@iv if they find no (further) extensions.

```
2812 \def\backgroundcolor#1{\@tempswatrue
2813
      \let\pcol@backgroundcolor@e\pcol@backgroundcolor@w
      \pcol@backgroundcolor#1\@nil}
2814
2815 \def\nobackgroundcolor#1{\@tempswafalse
2816
      \let\pcol@backgroundcolor@e\pcol@backgroundcolor@z
2817
      \pcol@backgroundcolor#1\@nil}
2818 \def\pcol@backgroundcolor#1{%
      \@ifundefined{pcol@bg@@#1}%
2819
        {\PackageError{paracol}%
2820
           {Invalid background coloring region identifier #1}%
2821
2822
         \def\pcol@bg@region{xx}\pcol@backgroundcolor@e}%
2823
        {\def\pcol@bg@region{#1}%
2824
         \[\%]
2825
           \pcol@backgroundcolor@i \pcol@backgroundcolor@ii}}
2826 \def\pcol@backgroundcolor@i[#1]{%
2827
      \@ifundefined{pcol@bg@mayhavecol@\pcol@bg@region}%
2828
        {\PackageError{paracol}%
           {Column number \number#1 is not effective for background coloring region
2829
            \pcol@bg@region}%
2830
         \def\pcol@bg@region{xx}\pcol@backgroundcolor@e}%
2831
2832
        {\edef\pcol@bg@region{\pcol@bg@region @#1}%
2833
         \pcol@backgroundcolor@ii}}
2834 \def\pcol@backgroundcolor@ii{%
      \if@tempswa
2835
        \ifx\set@color\relax
2836
2837
          \PackageWarning{paracol}{\string\backgroundcolor\space is not effective
2838
            without some coloring package}%
2839
          \let\reserved@b\pcol@backgroundcolor@w
2840
        \else
          \let\reserved@b\pcol@backgroundcolor@iii
2841
          \@cons\pcol@bg@defined{{\pcol@bg@region}}%
2842
        \fi
2843
2844
      \else
        \let\reserved@b\pcol@backgroundcolor@z
2845
      \fi
2846
      \reserved@b}
2847
2848 \def\pcol@backgroundcolor@iii{%
      \pcol@bg@defext{l}\z@ \pcol@bg@defext{r}\z@
2849
      \pcol@bg@defext{t}\z@ \pcol@bg@defext{b}\z@
2850
      \@ifnextchar(%)
2851
        \pcol@backgroundcolor@iv \pcol@backgroundcolor@x}
2852
2853 \def\pcol@backgroundcolor@iv(#1,#2){%
2854
      \pcol@bg@defext{1}{#1}\pcol@bg@defext{r}{#1}%
2855
      \pcol@bg@defext{t}{#2}\pcol@bg@defext{b}{#2}%
2856
      \langle 0ifnextchar(\%)
        \pcol@backgroundcolor@v \pcol@backgroundcolor@x}
2857
2858 \def\pcol@backgroundcolor@v(#1,#2){%
2859
      \pcol@bg@defext{r}{#1}\pcol@bg@defext{b}{#2}%
2860
      \pcol@backgroundcolor@x}
```

```
\pcol@backgroundcolor@x The macro \pcol@backgroundcolor@x is used in \pcol@backgroundcolor@iii, \pcol@
  \pcol@backgroundcolor@y backgroundcolor@iv and \pcol@backgroundcolor@v to define the color for background
                                                                   painting of the region a' = \text{pcol@bg@region}. Since the macro is followed by the argu-
                                                                    ments [mode] { color } of \backgroundcolor, the macro invokes \color to let it \define
                                                                    \operatorname{current@color} but without real coloring operations by letting \operatorname{set@color} = \operatorname{pcol@}
                                                                   backgroundcolor@y. Therefore \pcol@backgroundcolor@y is invoked in \color and it
                                                                   xdefines \pcol@bg@colpr.a' to let it have whatever \current@color has.
                                                                    2861 \def\pcol@backgroundcolor@x#1\@nil{\begingroup
                                                                                   \let\set@color\pcol@backgroundcolor@y \color}
                                                                   2862
                                                                   2863 \def\pcol@backgroundcolor@y{%
                                                                                   \expandafter\xdef\csname pcol@bg@color@\pcol@bg@region\endcsname
                                                                   2864
                                                                   2865
                                                                                      {\current@color}%
                                                                                   \endgroup
                                                                   2866
  \pcol@backgroundcolor@z The macro \pcol@backgroundcolor@z is invoked from \pcol@backgroundcolor@ii directly
  \colorebackgroundcolorebackgroundcolor to disable the background painting for a region <math>a' =
\pcol@backgroundcolor@wi \pcol@bg@region, or from \pcol@backgroundcolor and \pcol@backgroundcolor@i through
                  \colorge colorge colorge when they find an error in the argument (region) of \colorge colorge when they find an error in the argument (region) of \colorge colorge c
                                                                   color. Similarly the macro \pcol@backgroundcolor@w is invoked from \pcol@background
                                                                   color@ii directly when it finds no coloring packages have not been loaded, or \pcol@
                                                                   backgroundcolor and \pcol@backgroundcolor@i through \pcol@backgroundcolor@e on er-
                                                                   ror too but in the argument of \backgroundcolor. Both macros throw away whatever
                                                                   remains in (region) unprocessed and then invoke \pcol@backgroundcolor@wi, but \pcol@
                                                                   backgroundcolor@z gives it a dummy argument pair, while \pcol@backgroundcolor@w passes
                                                                    [mode] { color } to it.
                                                                            Then \col@backgroundcolor@wi throw all arguments away and lets <math>\col@bg@color@.a'
                                                                    =  \relax so that the region a' is untouched in background painting macros. Note that since
                                                                   a' = xx being an absolutely non-existent region when this macro is used for error recovery,
                                                                    undefining \pcol@bg@color@xx is not harmful.
                                                                   2867 \def\pcol@backgroundcolor@z#1\@nil{\pcol@backgroundcolor@wi[]{}}
                                                                   2868 \def\pcol@backgroundcolor@w#1\@nil{\@ifnextchar[%]
                                                                   2869
                                                                                   \pcol@backgroundcolor@wi{\pcol@backgroundcolor@wi[]}}
                                                                   2870 \def\pcol@backgroundcolor@wi[#1]#2{%
                                                                                   \expandafter\global\expandafter\let
                                                                   2871
                                                                   2872
                                                                                         \csname pcol@bg@color@\pcol@bg@region\endcsname\relax}
                                                                   2873
       \colorsymbol{pcolorsymbol{D}} a where a \in \{c, C, g, G\} are used in \colorsymbol{D} a where because a \in \{c, C, g, G\} are used in \colorsymbol{D} a where because a \in \{c, C, g, G\} are used in \colorsymbol{D} a where a \in \{c, C, g, G\} are used in \colorsymbol{D} a where a \in \{c, C, g, G\} are used in \colorsymbol{D} a where a \in \{c, C, g, G\} are used in \colorsymbol{D} a where a \in \{c, C, g, G\} are used in \colorsymbol{D} a where a \in \{c, C, g, G\} are used in \colorsymbol{D} a where 
       \colordiantering backgroundcolor or \nobackgroundcolor or \nobac
       \coll bg dmay have coll g ground color is followed by optional [c], so that the invoker macro examines if a can have the
       \pcol@bg@mayhavecol@G optional column ordinal. Therefore, the macros just need not to be \relax and thus commonly
                                                                   have empty bodies.
                                                                   2874 \def\pcol@bg@mayhavecol@c{}
                                                                   2875 \def\pcol@bg@mayhavecol@C{}
                                                                   2876 \def\pcol@bg@mayhavecol@g{}
                                                                   2877 \def\pcol@bg@mayhavecol@G{}
                                                                   2878
                        \colorgedefext The macro \colorgedefext{d}e is used by \colorgedefextgroundcolorgedefext.
                                                                    groundcolor@iv and \pcol@backgroundcolor@v to \define \pcol@bg@ext@d·@\cdot a' be e=0
                                                                   for all d \in \{1, \mathbf{r}, \mathbf{t}, \mathbf{b}\} in the first, be e = x_0 for d \in \{1, \mathbf{r}\} and e = y_0 for d \in \{\mathbf{t}, \mathbf{b}\} in the
```

```
second, and be e = x_0, x_1, y_0 and y_1 for d being l, r, t, b respectively in the last. The macro at first lets \@tempdima have e to confirm e is a proper dimension and then \xdefines \pcol@bg@ext@·d·@·a' to let it have the integer representation of e followed by sp.
```

```
2879 \def\pcol@bg@defext#1#2{%
2880 \@tempdima#2\relax
2881 \expandafter\xdef\csname pcol@bg@ext@#1@\pcol@bg@region\endcsname{%
2882 \number\@tempdima sp}}
2883
```

\resetbackgroundcolor The API macro \resetbackgroundcolor disables background painting of all regions whose \pcol@resetbackgroundcolor colors have been specified by \backgroundcolor. Since the region specifiers a'_1 , a'_2 , \pcol@bg@defined ..., a'_n for which background painting is specified are recorded in \pcol@bg@defined =

 $\ensuremath{\colordensuremath{a_2'\colcetta_n'\colce$

```
2884 \def\resetbackgroundcolor{{%
2885 \let\@elt\pcol@resetbackgroundcolor \pcol@bg@defined
2886 \gdef\pcol@bgdefined{}}
2887 \def\pcol@resetbackgroundcolor#1{%
2888 \expandafter\global\expandafter\let\csname pcol@bg@color@#1\endcsname\relax}
2889 \gdef\pcol@bg@defined{}
2890
```

23 Closing Environment

 $\label{eq:logical_stocl} \endparacol The macro \endparacol is invoked from \end{paracol} to close paracol environment. After \pcol@lastcol making it sure to be in vertical mode by \pcol@par, we switch to the column 0 by \pcol@ switchcol to let local counter have the values for the column 0 so that they are referred to outside the environment, after saving the current column c in \pcol@lastcol to be referred to in \pcol@output@end so that $\kappa_c(\sigma)$ and $\kappa_c(\varepsilon)$ are passed to post-environment stuff. In \pcol@switchcol, we make sure, not to add the preamble for column 0 by checking whether \pcol@lastcol is set.$

Then we invoke $\pcol@flushclear$ for pre-flushing column height check, turning $\fipcol@lastpage = true$ to tell $\pcol@output@switch$ for the check that it works on the last page, and giving \perp to $\pcol@flushclear$ as its argument, unless footnote typesetting is page-wise but not merged for which we give Φ to ensure all deferred footnotes are put in the checking process. Note that the argument for column-wise footnote typesetting is Φ but it is definitely \perp in this mode. After that we make an $\pcol@lastpage = true$ to build the last page.

Next, we let $\columnwidth = \textwidth$ and $\ifOtwocolumn = false$ for single-column typesetting, and also let $\textwidth = \pcolOtopskip$ to make it sure that the parameter has the value used outside in paracol environment. Finally, if the footnote counter adjustment is required by $\ifpcolOfncounteradjustment = true$, we let $\cofootnote = b_f + n_f$.

```
2891 %% Closing Environment
```

2892

 $2893 \ endparacol{\pcol@par}$

2894 \edef\pcol@lastcol{\number\pcol@currcol}%

2895 \pcol@nextcol\z@ \pcol@switchcol

```
\pcol@lastpagetrue
2896
      \ifpcol@mgfnote \pcol@flushclear\voidb@x
2897
      \else \pcol@flushclear\pcol@topfnotes
2898
2899
      \fi
      \pcol@invokeoutput\pcol@op@end
2900
      \global\columnwidth\textwidth
2901
      \global\@twocolumnfalse
2902
2903
      \global\topskip\pcol@topskip
2904
      \ifpcol@fncounteradjustment
        \global\c@footnote\pcol@footnotebase
2905
        \global\advance\c@footnote\pcol@nfootnotes
2906
2907
      \fi}
2908
```

\pcol@restoreeveryvbox The macro \pcol@restoreeveryvbox is invoked just after \end{paracol} by \aftergroup mechanism activated by \pcol@zparacol. It examines if \pcol@everyvbox has tokens different from \pcol@dummytoken which \pcol@zparacol \globally assigned to the register. Since the dummy token cannot be assigned to \everyvbox²³⁷, the difference means the \everyvbox has been \globally updated with the value that \pcol@everyvbox has now. Therefore if so, we globally update \everyvbox with \pcol@everyvbox to reflect the global update in the environment.

2909 \def\pcol@restoreeveryvbox{%

- 2911 \def\reserved@b{\pcol@dummytoken}%
- 2912 \ifx\reserved@a\reserved@b\else \global\everyvbox\pcol@everyvbox \fi}

 $^{^{-237}}$ Unless a very surprising coincidence happens or a user intentionally violates the coherence of the implementation.

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The author thanks to Yacine Daddi Addoun who gave the author the motivation to write the style for his bilingual document. He also thanks to the following people; Robin Fairbairns who kindly invited the style to CTAN after the author's lazy six years failing to upload the style; Joseph G. Rosenstein and Dieter Köhler who suggested the author adding the function of unbalanced column width incorporated in version 1.1; Joaquín Blas who motivated the author to challenge page-wise footnotes; Olivier Vogel who pointed out the compatibility problem with coloring packages; Heiner Richter who asked for the possibility of swapping unbalanced columns, revealed two bugs in version 1.22 related to coloring and float pages, showed the necessity of **\coloredwordhyphenated**, and finally found the necessity of **\globalcounter***; an anonymous user who reported a very rare-case but severe bug in the version 1.1 by which a page can be lost (whoops!); Olivier Gerard who found another terrible bug fixed in version 1.21 but hidden in paracol for two years by which a column disappears or moves to a wrong page (another whoops!), suggested to implement \setcolumnwidth, \marginparthreshold and \thecolumn introduced in version 1.3, and kindly proofread this manual; George Kamel who let the author know the coloring function newborn in version 1.2 had a bug fixed in version 1.22 to which he also made a great contribution testing many tentative versions with his own colored documents; another anonymous user who pointed out version 1.22 had yet another coloring bug fixed in version 1.24; Jean Druel who motivated the author to implement an advanced functionality parallel-paging; Tilo Arens and other patient users who had wished paracol would have the capability of rule drawing in the gaps separating columns and painting backgrounds of columns and so on; Michael Bolin who gave the author motivated examples showing the necessity of \ensurevspace. Tigran Aivazian who reported a memory leak problem fixed in version 1.32; Marcus Zelezny and Touhami Mamouni who found an incompatibility with LATEX itself (2015/01/10 or later) and enlighten the author on the cause of the problem; Manuel Kuehner who reported a bug in text coloring which had hidden for five years until the version 1.34was released; ZongXian Wang who found that the paracol misbehaves when an environment starts with an unusually tall item; and Frank Mittelbach who pointed out bugs in \marginpar implementation and vertical spacing with \trivlist-like environments, and suggested new functionality with \marginnote, \belowfootnoteskip and \definecolumnpreamble.

For the implementation of the style file, the author referred to the base implementations of $\operatorname{Voutput}$ and othe many macros of $\operatorname{IAT}_{EX} 2_{\varepsilon}$ written by Leslie Lamport, Johannes Braams and other authors. The author also referred to color written by David Carlisle and marginnote written by Markus Kohm to make the package working well with them.

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Underlined number refers to the page where the implementation or the definition of the corresponding entry is described, while italicized number is for the page in which the specification or usage of the entry is explained. To find a control sequence, remove prefixes \@, \if@, \pcol@ and \ifpcol@ from its name if it has one of them.

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Revision History

v0.9	
General: The style paracol is born. (2005/01/28)	. 1
v0.91	
General: The style is included in CTAN with a very small modification. $(2011/09/16)$. 1
v1.0	
General: Add this document and fix the following problems on the author's 30th wedding	
anniversary. $(2011/10/10)$	1
\pcol@toppage: Renamed from \pcol@maxpage.	130
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\ifpcol@outputflt: Renamed from \ifpcol@stopoutput with the reversal	132
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\pcol@invokeoutput: Add logging.	226
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\pcol@ifootnotetext: Introduced for \footnotetext*.	257
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General: Modify the description about \linewidth reflecting the fact that paracol may be
included in a list-like environment
(pcolummargin: introduced to let (linewidth for each column has the value according to w_c
and the list-like environment surrounding paracor environment
λ_c (b) (in the setting of λ_c is the setting of
(peoreinvokeoucput, wove the setting of (inewidth and (hsize from (peoregetcurred) to
this macro and add (parsnape
(properly set in and after) real deutrut detart
Add the setting of \maplelsmargin
\pcolezparacol. Add setting of \cclummidth \linewidth and \perchanges to have indepted
(procesprext: Add setting of (columnwidth, (linewidth and (parshape to have indented
\endparagel: Remove \glebal assignment of \heige and \linewidth because assignments of
them in paracol are new perfectly local
w1.2.6
$Conoral: Add \local counter (2013/05/11)$
Viocal counter: Introduced to remove the argument counter from Θ^g
\ncol@remctrelt: Recode to use newly introduced \ncol@remove.counter 246
\pcol@removecounter: Introduced for the counter removal operation in \localcounter and
\ncol@remetrelt 246
\pcol@iremctrelt: Add the first argument Θ' as the counter list from which the second
argument θ is removed 245
v1.2-7
General: Bug fixes and minor revisions as follows. (2013/05/11)
General: Remove \nosy from verbatim example of Table 1 shown in the right column.
General: Correct a few words in German and English libretti.
General: Add the section "Known and Unknown Problems" to summarize a few typesetting
issues and warn users of the possibility of bugs
\ifpcol@output: Introduced to solve the \output request sneaking
\ifpcol@lastpagesave: Introduced to fix the bug that \@makecol and \pcol@makefcolumn in
\pcol@flushcolumn misunderstand that non-last pages are last
\pcol@output: Add the examination of \ifpcol@output and LATFX's original sequence for
\output request sneaked from outside of paracol environment
\pcol@output: Add the assignment of \@maxdepth to \maxdepth to nullify the temporary
setting done by \@addtobot 145
\pcol@@makecol: Introduced to cope with the careless implementation of \@makecol in
pLATEX
\pcol@makecol: Remove unnecessary check of \ifpcol@lastpage on the redefinition of
\@textbottom
$\verb col@combinefloats: Add the assignment of \verb @maxdepth to \verb maxdepth to nullify the $
temporary setting done by $\columnwidth{\columnwidth\columnwi$
\pcol@combinefloats: Introduced to solve the \output request sneaking 146
\pcol@cflt: Replace \maxdepth with \@maxdepth
\pcol@nextpage: Remove unnecessary scan of $\pi(p_t)$
$\verb+pcol@outputelt: Add \verb+boxmaxdepth = \verb+Qmaxdepth for depth capping 155$
\pcol@output@start: Add \pcol@outputtrue to solve the \output request sneaking 174
\pcol@output@start: Include the effect of the separation of pre-environment bottom floats and
columns in the starting page into the check of too large pre-environment stuff 174
$\verb pcol@makenormalcol: Turn \ifpcol@lastpage be {true temporarily for \pcol@combinefloats} $
to separate bottom floats in pre-environment stuff and the multi-column stuff in paracol
environment by \textfloatsep 178
\pcol@output@switch: Modify broadcasting of $\kappa_c(\sigma)$ so that \@afterindent is broadcasted
with $\mbox{Qnobreak}$

\pcol@flushcolumn: Save \ifpcol@lastpage into \ifpcol@lastpagesave and turn \ifpcol@lastpage false temporarily during the macro works on non-top and thus nor pages to fix the bug that \@makecol and \pcol@makefcolumn misunderstand the page	n-last they
work on is last	204
<code>\Coutputbox</code> by <code>\Cmaxdepth</code> even with $pIAT_EX$	204
\pcol@flushcolumn: Add the restore of \ifpcol@lastpage from \ifpcol@lastpagesave.	206
\pcol@makefcolumn: Replace the sequence of operations to make a usual float column wit	h
$\times the newly introduced \pcol@makefcolpage$	207
\pcol@makefcolpage : Introduced to implement the operations to make a float column performed in three macros.	208
\pcol@synccolumn: Add an shrink of 1/10000 fil to the bottom of flushed column pages cancel finite shrinks just below synchronization points.	to 211
\pcol@output@flush: Add \boxmaxdepth = \@maxdepth for depth capping.	214
\pcol@output@flush: Add \boxmaxdepth = \@maxdepth for depth capping	214
\pcol@output@clear: Add \boxmaxdepth = \@maxdepth for depth capping	214
\pcol@imakeflushedpage: Enclose the column-page building process in a group to fix the	bug
which lets \topfigrule = \relax affecting to another column.	220
\pcol@imakeflushedpage: Replace the sequence of operations to make a usual float colum	nn
with \Ctoplist with the newly introduced \pcolCmakefcolpage.	220
\pcol@imakeflushedpage: Replace \@makecol with \pcol@@makecol to cap the depth of	220
\period and Add \period and a local Country of the loutry tradest sneeking	220
<pre>\pcol@output@end: Add \boxmaxdepth = \@maxdepth for depth capping knowing it is redundent</pre>	222
requindant	222
$\$	$\dots 249$
the list which caused a bur	011 III 949
vil 21	242
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\pcol@outputelt : Revise reflecting the new page context element $\pi^m(p)$	154
\pcol@ioutputelt: Add a logic to cope with non-uniform column-separating gaps	156
\pcol@buildcolseprule: Introduced for non-uniform column-separating gaps	158
\pcol@buildcselt: Introduced for non-uniform column-separating gaps.	158
\pcol@hfil: Introduced for non-uniform column-separating gaps.	160
\pcol@Coutputpage: Introduced keep the original definition of \Coutputpage	160
\Coutputpage: Redefined for marginal note placement.	160
\pcol@output@start: Add initialization of $\pi^m(0)$.	176
\pcol@output@switch: Add $\pi^m(p) = \pcol@mparbottom to the argument of$	
\pcol@defcurrpage.	180
\pcol@iigetcurrcol: Remove the argument for $\kappa_c(\mu) = \mbox{Comparbottom}$ because it is no longer	r
in the column context.	185
\pcol@setcurrcol: Remove $\kappa_c(\mu) = \mbox{Conversion}$ from the body of \pcol@col.c because it i	is
no longer in the column context.	186
General: Add this section "Marginal Notes".	194
\Caddmarginpar: Made \let-equal to \pcolCaddmarginpar in paracol environments	194
\pcol@addmarginpar: Introduced to make a margin sharable by marginal notes from different	;
columns.	194
\pcol@addmarginpar: Introduced to keep the original definition of \@addmarginpar.	194
\pcol@getmparbottom: Introduced to find the space where a marginal note is placed.	197
\pcol@getmparbottom@i: Introduced to find the space where a marginal note is placed	197
\pcol@getmphelt: Introduced to find the space where a marginal note is placed	197
(peolegetemphelt: Introduced to undate $\pi^m(n)$	198
\pcolosetmpbeltoi: Introduced to update $\pi^{m}(p)$.	198
\pcol@mparbottom@zero: Introduced to give the default of \pcol@mparbottom@out	198
(peotemparbottometric). Introduced to give the default of (peotemparbottometric). \dots	198
vector method to do specified operations on M and its element M^x according	100
to the side margin for marginal notes outside paracol environments	190
λ ncol@do@mphout@i: Introduced to do specified operations on M and its element M_{x}^{x} according	ng
to the side margin for marginal notes outside $paracol$ environments	100
$\$	190
λ pcolledomphout@elem: Introduced to do a specified operation on an element M_{x}^{x} in M_{y}^{x}	100
$\ \$	100
\pcol@bias@mpbout@i: Introduced to perform coordinate transformation of the elements in	100
M	100
λ ncol@getmorpattem@last: Introduced to let M have the occupancy information of the	199
bottom marginal note in each margin	200
\ncol@rotmnarbattam@lact@i: Introduced to lat M have the accumancy information of the	200
bottom marginal note in each margin	200
bottom marginar note in each margin.	200
\pcol@cotmport.infordated to implement \pcol@blasempbout and	200
\pcol@decmph@all@i. Introduced to implement \pcol@bicc@mpheut and	200
\pcoledualer: Informed to implement \pcoledualerempbolt and	200
\pcolugetmparbottomulast.	200
\pcoledowmpbearler: infoduced to implement \pcolebiasempbout and	200
	200
\pcol@imakeriushedpage: Implement variable-width column-separating gaps.	218
Approximation of the second se	220
Approximation to pass M to the next paracol environment and	000
\u00ed \u	222
vpcoreoutputwend: And letting vemparbottom = 0 and $\mathcal{M} = \mathcal{M}_0$ for the simple empty page	004
case	224

\pcol@zparacol: Revise the mechanism to define the width of columns and column-separating gaps, and add local overriding definition of \@addmarginpar	g 229
prolograma col: Add new API inactivation for \prol@twosided	231
General: Add the section "Column Width Setting" mainly to discuss the new API	-01
\setcolumnwidth.	234
\setcolumnwidth: Introduced to specify column widths and column-separating gaps more	-01
detailedly.	234
\pcol@isetcolumnwidth: Introduced to process the optional second argument of	
\setcolumnwidth	234
\pcol@colwidthspecleft: Introduced to keep column width specifications for left	
parallel-pages.	234
\pcol@colwidthspecright: Introduced to keep column width specifications for right	
parallel-pages.	234
\pcol@setcolumnwidth: Move original functions to \pcol@setcolumnwidth@r and redefine thi	is
macro to switch \pcol@setcolumnwidth@r and \pcol@setcolumnwidth@s	235
\pcol@setcolwidth@r: Renamed from \pcol@setcolumnwidth to make it clear what the mach	ro
works for.	235
$\climits coll width @s: Introduced to calculate w_c and g_c.$	236
$\column black \column \col$	
\pcol@setcolwidth@s	236
\pcol@setcw@s: Introduced to process column-separating gap components in the argument	
(spec) of \pcol@setcolwidth@s	236
\pcol@setcw@filunit: Introduced to define the unit of infinite stretch factors in the argumen	ıt
(spec) of \pcol@setcolwidth@s	236
$\col@setcw@scan: Introduced to scan the argument (spec) of \col@setcolwidth@s$	237
$\colored colored col$	
\pcol@setcolwidth@s	237
$\coldsetcw@getspec@i: Introduced to parse an element in the argument (spec) of$	~~~
\pcol@setcolwidth@s	237
\pcol@setcw@fill: Introduced to extract \fill factor from an element in the argument (spec	$c\rangle$
of \pcol@setcolwidth@s.	237
\pcol@setcw@accumwd: Introduced to accumulate natural and fill factors of the element in the))
argument (spec) of \pcol@setcolwidth@s	238
$\column{blue}{lllllllllllllllllllllllllllllllllll$	
(spec) of \pcol@setcolwidth@s.	238
\pcol@setcw@calcfactors: Introduced to calculate scaling and stretch factors from the	
argument (spec) of \pcol@setcolwidth@s	239
\pcol@setcw@calcf: Introduced to calculate scaling or stretch factor from the argument (spec	$c\rangle$
of \pcol@setcolwidth@s.	239
\pcol@setcw@scale: Introduced to have the scaling factor of w_c and g_c	239
$\coll def kw:$ Introduced to define $\coll kw @ k$ where $k \in \{pt, plus, minus, fil\}$	240
\pcol@kw@pt: Introduced to have the keyword pt	240
\pcol@kw@plus: Introduced to have the keyword plus.	240
\pcol@kw@minus: Introduced to have the keyword minus	240
\pcol@kw@fil: Introduced to have the keyword fil	240
\pcol@def@extract@fil: Introduced to define \pcol@extract@fil	241
\pcol@extract@fil: Introduced to extract infinite stretch factor from a skip if any	. 241
\pcol@extract@fil@i: Introduced to extract the factor of fil from the stretch factor in a ski	ıp
it any.	241
\pcol@extract@fil@ii: Introduced to extract the factor of fil from the stretch factor in a	o
skip if any.	241
\pcol@det@extract@fil@iii: Introduced to define \pcol@extract@fil@iii	241
\pcol@extract@fil@iii: Introduced to extract the factor of fil from the stretch factor in a	o
skip	241

\pcol@def@extract@pt: Introduced to define \pcol@extract@pt	241
\pcol@extract@pt: Introduced to extract the factor of pt from the \the representation of a	0.41
dimension.	241
\pcol@switchcol: Remove setting \if@firstcolumn and the invocation of \pcol@swapcolumn	n 0.47
for it because the position of marginal notes are now controlled by \pcol@addmarginpar.	247
\twosided: Add two-sided marginal note placement.	258
\pcol@twosided@m: Introduced for two-sided marginal note placement.	258
\pcol@swapcolumn: Add a user \pcol@addmarginpar and remove \paracol, \pcol@sptext an \pcol@switchcol	1d 259
\marginparthreshold: Introduced to specify the smallest ordinal of columns whose marginal	250
\pcol@marginparthreshold: Introduced to implement \marginparthreshold.	$259 \\ 259$
\pcol@mpthreshold@1: Introduced to keep the value specified by \marginparthreshold for columns in left parallel-pages.	259
\pcol@mpthreshold@r: Introduced to keep the value specified by \marginparthreshold for	
columns in right parallel-pages.	259
v1.3-5	
General: Introduce \thecolumn and \ensurevspace, \footnotelayout, \twosided and \closed and closed	1
Conoral: Add description of \thecolumn	18
General: Add description of Vensurevspace	10
General: Add the sub-section "Commands for Two-Sided Typesetting and Marginal Note	- 10
Placement ⁷ .	. 21
General: Add description of \[ma] current compared but montion they are still	21
available.	. 22
General: Rename the sub-section title from "Single-Columned Footnotes" to "Page-Wise	
Footnotes" following new naming.	. 24
$General: Remove \ description \ of \ \verb+multicolumnfootnotes, \ \verb+singlecolumnfootnotes, \ end{tabular}$	
\mergedfootnotes but mention they are still available.	. 25
General: Add description of \cleardoublepage .	29
General: Rename the section title from "Numbering and Placement of Single-Columned	
Footnotes" to "Numbering and Placement of "Page-Wise Footnotes" following new naming	; <u>30</u>
General: Add the section "Two-Sided Typesetting and Parallel-Paging".	38
General: Change the subsection title from "Coloring" to "Text Coloring" to distinguish it from background painting clearly.	m . 70
\pcol@zparacol: Add new API inactivation for \footnotelayout	231
\thecolumn: Introduced to let users know which column they are working in	233
\pcol@localcommands: Add \@elt{cleardoublepage} for \cleardoublepage	233
(peoplessification of $V_E = (people ensure vspace and reinitialization of V_E = (people ensure vspace)$	947
\pcoluensurevspace for avoidance of post-synchronization inconsistent page break	241
(ensurevspace: introduced to declare the minimum space v_E below a synchronization point let it sterv in a page	250
Let it stay in a page. \dots let it stay in a page. \dots dealared by hereinergapes	200
$\$	200
routing	250
\closedoublopege: Added as a member of local commands and made \lot equal to	200
\real@com@cloardoublepage.	252
\pcol@com@cleardoublepage. Introduced as the implementation of \cleardoublepage.	- 202 - 259
\footnotelayout: Introduced for easier declaration of footnote layout	202
\ncol@fnlavout@c: Introduced for easier declaration of column_wise footnotes	- 253 - 253
\ncol@fnlavout@n: Introduced for easier declaration of page-wise footnotes	253
\pcol@fnlavout@m: Introduced for easier declaration of merged footnotes	253
General: Rename the section title from "Column-Swapping" to "Two-Sided Typesetting"	258

\twosided: Introduced as an easier API for various two-sided typesetting
\pcol@twosided: Introduced to implement \twosided
\pcol@twosided@p: Introduced to implement \twosided with [p]
\pcol@twosided@c: Introduced to implement \twosided with [c]
\pcol@twosided@m: Introduced to implement \twosided with [m]
\pcol@twosided@b: Introduced to implement \twosided with [b]
v1.3-6
General: Fix a few problems mainly related to synchronization and ordinary footnotes.
General: Add comments about usage of \paragraph etc. in spanning texts
General: Change the title from "Single-Columned and Merged Footnotes" to "Page-Wise and
Merged Footnotes" according to the new naming.
\ipcol@bibottom: Introduced to know which column-wise footnotes or bottom floats are put
at the bottom of a column.
(lipcol@diloats: introduced to know if the last page has deferred column-wise hoats 130
\pcol@ShowBox: Change \unvcopy to \copy to copy to make sure the argument box causes overfull if its
neight is positive and even if it has nothing
(pcoluumakecol: Add an argument a to be assigned to (boxmaxdepth to let it have 0 rather
than \umaxdeptn for last page 144
(peolecombine floats: Add special operations for columns having synchronization point to
them
140
(pcolenextpert: Fix the bug that π (q) is not referred correctly
\pcol@makenormalcol to \@makecol because the page should be built by the ordinary
mechanism
\pcol@output@start: Delete the argument of \pcol@makenormalcol because now it is not used too tall pre-environment stuff
\pcol@makenormalcol: Completely redesigned to use \@makecol if pre-environment stuff has bottom floats
\pcolCoutputCswitch : Modify the condition of broadcasting $\kappa_0(\sigma)$ and $\kappa_0(\varepsilon)$ accompanied with \ifpcolCsystem \ifpcolCsystem to $c = 0$ so that the broadcast is made in the first
column-switching in column-scanning. 182
$\colloutput@switch: Modify the code structure to let \if@tempswa = true according to the madification of the head destrict of u_{(z)} and u_{(z)}$
modification of the broadcast of $\kappa_0(\sigma)$ and $\kappa_0(\varepsilon)$
for ordinary column-wise footnotes from below the main text to below the footnotes 183
General: Move commands outside \output routine to the newly introduced section Commands
hor fext Coloring to distinguish macros inside and outside (output routine 10/
(clean plan b which was modified unconditionally
\pcol@deferredfootins: Fix the bug that the height cap was underestimated by the duplicated
subtraction of $\skip\footins$ if the page has already have non-deferred footnotes 192
\pcol@putfootins: Remove \pcol@output@end from users
$\colorsymbol{pcolQsync:}$ Add the initialization of $\ifpcolQdfloats = false$ before invoking
\pcol@measurecolumn 201
\pcol@sync: Modify the flushing condition of synchronized column switching from $V > \pi^h(p)$
to $\max(V, V - D_T + V_E) > \pi^n(p)$ to avoid page break just below the synchronization point
as much as possible
\pcol@flushcolumn: Fix the problem that a flushed column in a non-top page causes overfull
due to its hight-plus-depth greater than $\pi^n(p)$
\pcol@flushcolumn: Add \@maxdepth as the first argument of \pcol@@makecol 204

\pcol@measurecolumn: Revise the mechanism to tell \pcol@makeflushedpage and \pcol@output@end that a column in a last page has deferred column-wise floats with new	vly
introduced \ifpcol@dfloats.	210
\pcol@makeflushedpage: Revise the mechanism of special care about last page introducing	
\ifpcol@dfloats	215
\pcol@makeflushedpage: Revise the condition of leaving page-wise floats as ordinary	
post-environment floats using \if@tempswa with \ifpcol@dfloats	217
\pcol@makeflushedpage: Remove empty column scan for \if@fcolmade because it is now	
unnecessary thanks to \ifpcol@dfloats.	217
\pcol@makeflushedpage: Revise the condition of column-page building and setting of \@colht	217
\pcol@makeflushedpage : page-wise footnotes for the last page followed by pages for deferred column-wise floats are now put by this macro	l 218
\ncol@imakeflushednage: Add \@maxdenth or 0 as the argument of \ncol@@makecol to fix t	the
problem that the last page is too large due to \Omaxdepth by the latter	220
problem that the last page is too have the examination of $\kappa_c(\lambda_d)$ for \ifefcolmade because it is	;
made unnecessary now by \ifpcol@dfloats.	220
\pcol@output@end: Simplify the case with deferred floats thanks to \ifpcol@dfloats and	
redesign of \pcol@makeflushedpage.	223
\pcol@output@end: Remove \unskip from the operation to let page-wise floats be ordinary	
ones because \pcol@makeflushedpage does it.	224
\pcol@zparacol: Add operations for the vertical skips at the beginning of a list-like	
environment.	228
\pcol@sptext: Add globalization of \@svsechd and \@svsec	. 247
General: Add the section "Commands for Text Coloring" to distinguish macros inside and	0.00
outside \output routine and describe the latter in this section.	260
\pcol@set@color@push: Change the second argument of \pcol@color@invokeoutput from	0.00
hskip/z@ to /pcol@icwhyphenate to make null skip insertion conditional.	262
\coloredwordnyphenated: Introduced to enable null skip insertion before the first word after	a a
coloring command not always but conditionally.	264
\nocoloredwordnypnenated: Introduced to disable null skip insertion before the first word an	ter
a coloring command.	204
(produced component company but conditionally and produced to enable num skip insertion before the first word after a	9 <i>C</i> 4
vi 21	204
Concred: Add passing parameters related sectioning commands beyond \ordfaparacel > and	d
fy miscalls in error messages $(2013/10/10)$	1u 1
\ncol@output@ond: Add \ncol@rot.currcol for the column specified by \ncol@loct.col to p	••• 1
\if@nobrook \if@afterindent and \everyper of the column to post environment stuff	200 206
\ncol@setcu@calcf: Canitalize the first word of the error message for consistency	220
\pcol@suitchcolumn: Add a space before the number of columns in the error message	. 205 246
\pcol@switchcorumn. Add a space before the number of columns in the error message	· 240
\pcol@twosided: Fix spelling "twosiding" replacing it with "two-siding" in the error message	243 258
\pcol@backgroundcolor: Fix the misspelling "colorling" in the error message	265
\endparacel: Add saving c into \ncol@lastcol to let \ncol@output@end know the column	. 200
visited last	268
\pcol@last.col: Introduced to keep the column visited last to pass its typesetting parameter	200
to post-environment	268
v1 32-1	200
General: Add σ counters to make all counters global (2015/10/10)	1
General: Add descriptions of \globalcounter*	··· 1 23
\globalcounter: Modified according to the introduction of \globalcounter*	242
\pcol@globalcounter@s: Added for \globalcounter*.	. 242

\pcol@globalcounter: Renamed from \globalcounter according to the introduction of
\globalcounter*
V1.52-2 Company Figure a memory leads in $h = 16$
General: Fix a memory leak in (pcolestartcolumn. (2013/10/10)
\pcol@F@write: introduced for debugging memory leak problems
\pcoluer: Introduced for debugging memory leak problems
\pcol@FF: Introduced for debugging memory leak problems
\pcol@F@count: Introduced for debugging memory leak problems
\pcol@F@n: Introduced for debugging memory leak problems
\pcol@Fb: Introduced for debugging memory leak problems
\pcol@Fe: Introduced for debugging memory leak problems
\pcol@makecol: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@cflt: Add \pcol@Fb/\pcol@Fe pair(s) 14
\pcol@opcol: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@startpage: Add \pcol@Fb/\pcol@Fe par(s)
\pcol@outputelt: Add \pcol@Fb/\pcol@Fe par(s)
\pcol@ioutputelt: Add \pcol@Fb/\pcol@Fe par(s) 15
\pcol@ioutputelt: Add \pcol@Fb/\pcol@Fe par(s) 15
\pcol@ioutputelt: Add \pcol@Fb/\pcol@Fe par(s) 150
\pcol@startcolumn: Fix the memory leak caused by mistakingly preserving $\pi^{J}(p)$ when
$p = p_t. \qquad 164$
\pcol@startcolumn: Add \pcol@Fb/\pcol@Fe $pair(s)$
\pcol@output@start: Add \pcol@Fb/\pcol@Fe $pair(s)$
\pcol@output@start: Add \pcol@Fb/\pcol@Fe $\operatorname{pair}(s)$
\pcol@output@start: Add \pcol@Fb/\pcol@Fe $\operatorname{pair}(s)$
\pcol@makenormalcol: $\operatorname{Add} \operatorname{pcol@Fb/\pcol@Fe} pair(s).$
\pcol@output@switch: $Add \pcol@Fb/\pcol@Fe pair(s).$
$\pcol@restartcolumn: Add \pcol@Fb/\pcol@Fe pair(s) 186$
$\pcol@restartcolumn: Add \pcol@Fb/\pcol@Fe pair(s). \dots \dots \dots \dots \dots \dots \dots \dots 18$
\pcol@flushcolumn: Add \pcol@Fb/\pcol@Fe $pair(s)$
\pcol@flushcolumn: Add \pcol@Fb/\pcol@Fe $pair(s)$
\pcol@flushcolumn: Add \pcol@Fb/\pcol@Fe $pair(s)$
\pcol@makefcolpage: ${ m Add}$ \pcol@Fb/\pcol@Fe ${ m pair(s)}$
\pcol@synccolumn: Add \pcol@Fb/\pcol@Fe pair(s)
\pcol@makeflushedpage: $Add \pcol@Fb/\pcol@Fe pair(s)$
\pcol@makeflushedpage: Add \pcol@Fb/\pcol@Fe pair(s).
$\pcol@imakeflushedpage: Add \pcol@Fb/\pcol@Fe pair(s) $
\pcol@output@end: Add \pcol@Fb/\pcol@Fe $pair(s)$
\pcol@output@end: Add \pcol@Fb/\pcol@Fe $pair(s)$
\pcol@output@end: Add \pcol@Fb/\pcol@Fe $pair(s)$
v1.32-3
General: Fix a page-wise float problem. $(2015/10/10)$
General: Add footnote to mention the page-wise float problem.
General: Add comments about the out-of-order appearance of page-wise floats even with
$\mathbb{I}^{\mathbb{A}}$ 1EX-2015/01/10 or later
General: Add the section "Page-wise Float Placement" to discuss the page-wise float problem. 7
$\colored line \colored line \colored line \colored \col$
\@dblfloatplacement
\pcol@startpage: Modify the code to apply \@sdblcolelt to \@dbldeferlist so as to work
with both 2015 (or newer) and 2014 (or older) versions of IAT_{EX} 15.
\pcol@output@start: Add depth clearing of imported deferred floats in case that some of them
has 1sp
$\colored line \colored line \colored line \colored \col$
$\$

\pcol@zparacol: Add replacement of \end@dblfloat with \pcol@end@dblfloat	229 233
\pcol@end@dblfloat: Added to go back to old mechanism	233
General: Fix a marginal note problem. (2016/11/19)	. 1
\pcol@getmpbelt: Fix the bug by which t_k such that $t_k \ge t$ and $t_k - t \ge h$ but $t_k - b_{k-1} < h$ found.	is 197
v1.33-2	
General: Non-logical modifications to obey the coding convention, for clarification, etc (2016/11/19)	. 1
\pcol@output: Add a space after \@opcol to obey the coding convention.	143
\pcol@makecol: Move down the \definition of \pcol@currfoot with \perp to place it just before the \ifpcol@scfnote/\fi construct to make it clear how \pcol@currfoot is \defined.	145
\pcol@cflt: Add % to the end of the line to open \vbox for \@outputbox to obey the coding	1/0
\pcol@opcol: Add % to the end of the line to open \vbox for \@currbox to obey the coding	140
convention.	148
$\collectropy $ Add $\let\ensuremath{\collectropy}$ before $\ensuremath{\collectropy}$ for the sake of clarity. \pcollectropy collectropy beta the height of \pcolleprespan if it is not \perp , or 0 if \perp	149
for the sake of clarity.	180
$\colored line to open \vbox for \pcol@prespan to obey the line to open \vbox for \vbox for \pcol@prespan to obey the line to open \vbox for \pcol@prespan to obey the line to open \vbox for \vbox for$	е
coding convention.	186
\pcol@makefcolumn: Remove a space after the \vbox to be assigned to \@currbox to obey the	•
coding convention.	207
\pcol@makefcolpage: Add % to the end of the line to open \vbox to obey the coding convention.	208
\pcol@synccolumn: Add % to the end of the line to open \vbox for \pcol@float to obey the	
coding convention.	212
\vboxes in it to obey the coding convention.	or 213
v1.34	
General: Fix a text coloring problem in non-breakable sequences of vertical items. $(2018/05/07)$	() 1
General: Revise the description of $\$1.6.1$ according to the new implementation with \insert .	70
General: Revise the description of §1.6.2 according to the new implementation with \insert.	71
General: Split the description of \columncolor from §1.6.2 to have new §1.6.3 "Changing Default Column Color" because we have several new issues in the new implementation wit	h
\insert	72
General: Revise the description of §1.6.4 according to the new implementation with \insert. \pcol@mcid: Change its meaning and operations with it a little bit according to the new text	73
coloring with \insert .	130
$\colorstack@saved:$ Introduced as Γ_s to keep the color stack Γ^c until a column-page of	c
becomes non-empty.	139
\pcol@tempboxa: Renamed from \pcol@tempbox because its relative \pcol@tempboxb is introduced.	139
\pcol@temphoxa: Add usage in \pcol@scancst and \pcol@iscancst	139
$\color stack \Gamma \Gamma_{r}$ or Γ_{c}	139
General: Add \$3.6 "\insert Register Set" for \pcol@colorins	140
\pcol@colorins: Introduced to present text-coloring operations to \output synchronously wit	th
column-pages.	140
\pcol@ShowBox: Add messaging (VOID) if $\langle b \rangle = \bot$, $\forall fuzz \leftarrow 0$ to ensure overfull, and $\forall skip$	140
of 1 pt if $\langle 0 \rangle$ s field is 0 to ensure overfull too.	140
\pcol@buildcolseprule: Rename \pcol@tempbox as \pcol@tempboxa	150
\pcol@bfil: Rename \pcol@tempbox as \pcol@tempboxa	160
veorentitt. Mename veoretempoor as veoretempoora.	100

\Coutputpage: Rename \pcolCtempbox as \pcolCtempboxa	160 162
\insert.	173
General: \pcol@op@cpop is removed according to the change of text coloring from \output to	
\insert.	173
General: \pcol@op@cpop is removed according to the change of text coloring from \output to	
Vinsert	173
General: \pcol@op@mcpush is removed according to the change of text coloring from \output to	0
\insert.	174
General: \pcol@on@mcnush@pone is removed according to the change of text coloring from	
Voltant to Vinsert	174
General: \pcol@op@mcpop is removed according to the change of text coloring from \output to	
\insert	174
General: \ncollon@mcnon@none is removed according to the change of text coloring from	111
Voltant to Vincort	174
$\{ a \in [a] \}$	174
$\gamma \in \{c, c, c$	178
$\Gamma_{0} = \Gamma_{0} = \Gamma_{0} = \Gamma_{0}$	110
(protection of $f_s = 0$) where $f_s = 0$	186
Constal: $\$ Constal: Cons	100
Voltent to Vinsort	187
Constal: \pcol@output@icpush is removed according to the change of text coloring from	101
Sentral, to bincont	107
Concercle \nccl@output@monuple is removed according to the change of taxt coloring from	101
General, proceeding to the change of text coloring from	107
Concerls \neel@cutrut@imenueh is removed according to the shares of tout coloring from	101
Ceneral. Approximate the line could be according to the change of text coloring from	107
Comput to Ainsert.	101
General: \pcolleoutput@cpop is removed according to the change of text coloring from \output	5 107
Compared A parallelistic removed according to the sharpe of text coloring from	101
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